

Chapter 1
SIMILARITY

LONG QUESTIONS

Q. 1

Base of a triangle is 9 and height is 5. Base of another triangle is 10 and height is 6. Find the ratio of areas of these triangles.

SOLUTION:

Let the base, height and area of the first triangle be b_1 , h_1 , and A_1 respectively.

Let the base, height and area of the second triangle be b_2 , h_2 and A_2 respectively.

$$\frac{A_1}{A_2} = \frac{(b_1 \times h_1)}{(b_2 \times h_2)}$$

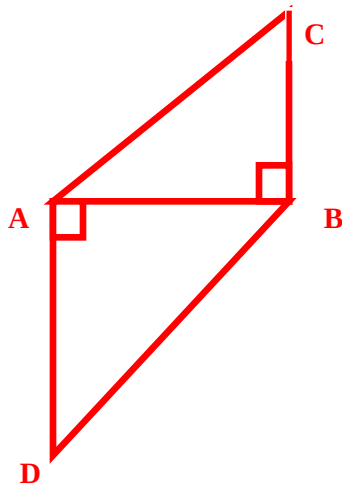
$$\frac{A_1}{A_2} = \frac{9 \times 5}{10 \times 6} = \frac{45}{60}$$

$$\frac{A_1}{A_2} = \frac{3}{4}$$

Ans.: The ratio of areas of triangles is 3:4

Q. 2

In the adjoining figure, $BC \perp AB$, $AD \perp AB$, $BC = 4$, $AD = 8$, then find $\frac{A(\Delta ABC)}{A(\Delta ADB)}$



SOLUTION:

ΔABC and ΔADB have same base AB .

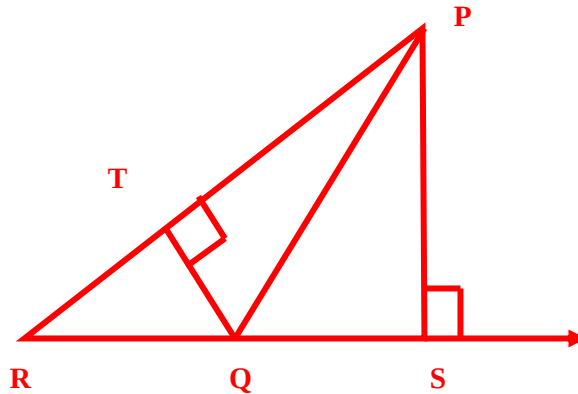
$$\frac{A(\Delta ABC)}{A(\Delta ADB)} = \frac{BC}{AD} = \frac{4}{8}$$

$$\frac{A(\Delta ABC)}{A(\Delta ADB)} = \frac{1}{2}$$

Ans.: Ratio of area of ΔABC to ΔADB is 1:2

Q. 3

In the figure, $\text{seg } PS \perp \text{seg } RQ$, $\text{seg } QT \perp \text{seg } PR$. If $RQ = 6$, $PS = 6$ and $PR = 12$, then find QT .



SOLUTION:

In $\triangle PQR$, PR is the base and QT is the corresponding height.

Also, RQ is the base and PS is the corresponding height.

$$\frac{A(\triangle PQR)}{A(\triangle PQR)} = \frac{PR \times QT}{RQ \times PS}$$

[Ratio of areas of two triangles is equal to the ratio of the product of their bases and corresponding heights]

$$\therefore \frac{1}{1} = \frac{PR \times QT}{RQ \times PS}$$

$$\therefore PR \times QT = RQ \times PS$$

$$\therefore 12 \times QT = 6 \times 6$$

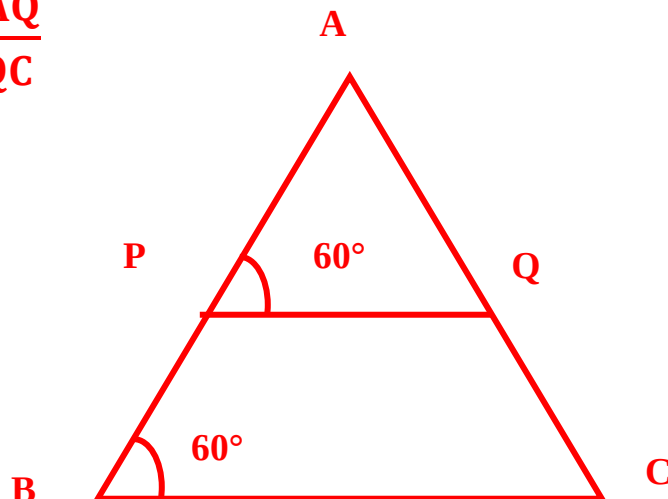
$$\therefore QT = \frac{36}{12} = 3$$

Ans.: $QT = 3$ units

Q. 4

Measures of some angles in the figure are given.

Prove that $\frac{AP}{PB} = \frac{AQ}{QC}$



SOLUTION:**Proof**

$$\angle APQ = \angle ABC = 60^\circ \text{ [Given]}$$

$$\therefore \angle APQ \cong \angle ABC$$

$$\therefore \text{side PQ} \parallel \text{side BC (i) [Corresponding angles test]}$$

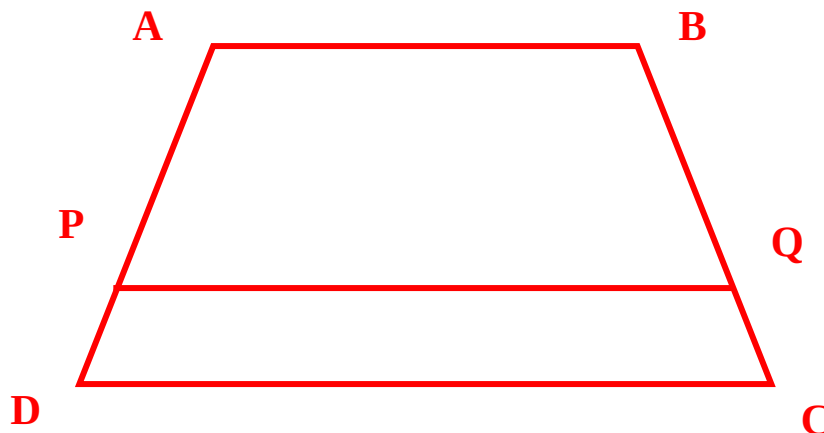
In $\triangle ABC$,

$$\text{side PQ} \parallel \text{side BC [From (i)]}$$

$$\therefore \frac{AP}{PB} = \frac{AQ}{QC} \text{ [Basic proportionality theorem]}$$

Q. 5

In trapezium ABCD, side $AB \parallel$ side $PQ \parallel$ side DC ,
 $AP = 15$, $PD = 12$, $QC = 14$, find BQ .



SOLUTION:

side AB $\parallel$ side PQ $\parallel$ side DC [Given]

$\therefore AP/PD = BQ/QC$ [Property of three parallel lines and their transversals]

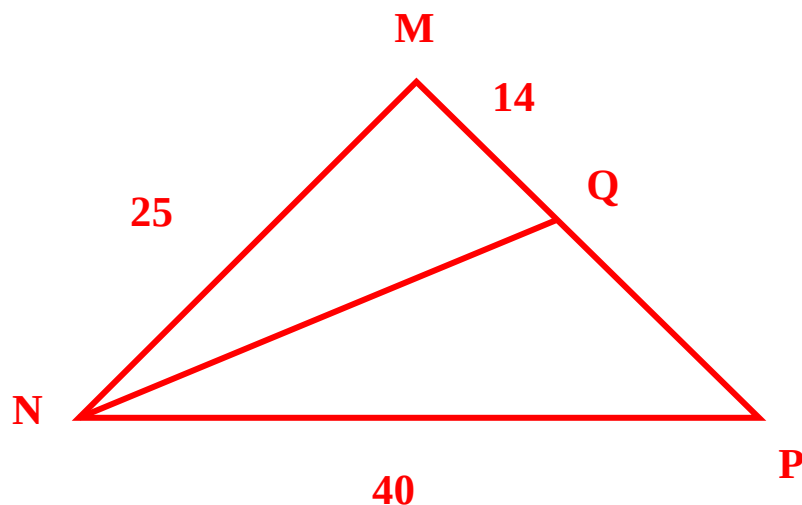
$$\therefore 15/12 = BQ/14$$

$$\therefore BQ = 15 \times 14 / 12$$

$$\therefore BQ = 17.5 \text{ units}$$

Q. 6

Find QP using given information in the figure.



SOLUTION:

In $\triangle MNP$, seg NQ bisects $\angle N$ [Given]

$$\therefore \frac{PN}{MN} = \frac{QP}{MQ}$$

[Property of angle bisector of a triangle]

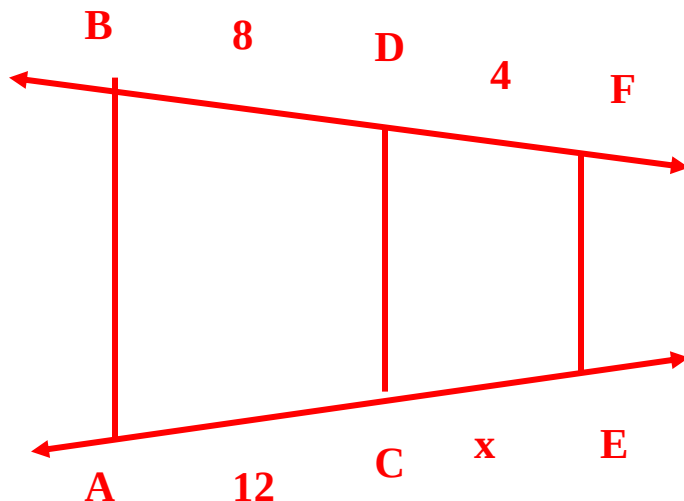
$$\therefore \frac{40}{25} = \frac{QP}{14}$$

$$\therefore QP = \frac{(40 \times 14)}{25} = 22.4$$

$$\therefore QP = 22.4 \text{ units}$$

Q. 7

In the adjoining figure, if $AB \parallel CD \parallel FE$, then find x and AE .



SOLUTION:

line $AB \parallel$ line $CD \parallel$ line FE [Given]

$$\therefore \frac{BD}{DF} = \frac{AC}{CE}$$

[Property of three parallel lines and their transversals]

$$\therefore 84 = 12x$$

$$\therefore x = 12 \times 48$$

$$\therefore x = 6 \text{ units}$$

Now, $AE = AC + CE$ [A – C – E]

$$= 12 + x$$

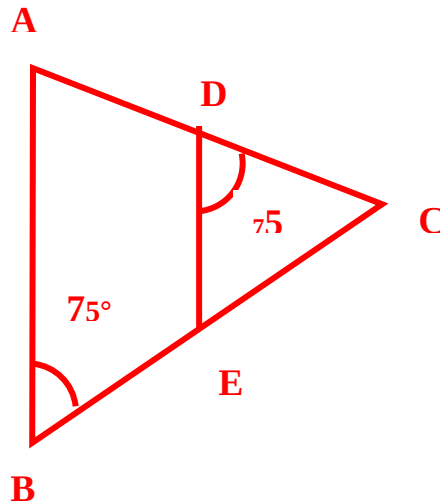
$$= 12 + 6$$

$$= 18 \text{ units}$$

$$\therefore x = 6 \text{ units and } AE = 18 \text{ units}$$

Q. 8

In the adjoining figure, $\angle ABC = 75^\circ$, $\angle EDC = 75^\circ$. State which two triangles are similar and by which test? Also write the similarity of these two triangles by a proper one to one correspondence.

**SOLUTION:**

In $\triangle ABC$ and $\triangle EDC$,

$\angle ABC \cong \angle EDC$ [Each angle is of measure 75°]

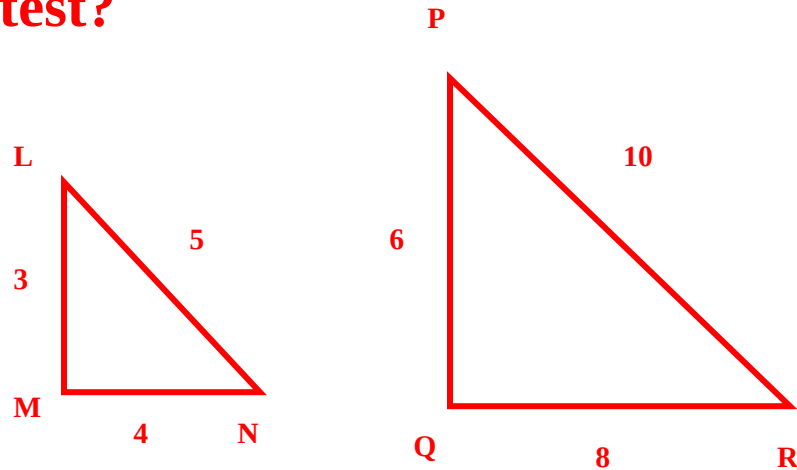
$\angle ACB \cong \angle ECD$ [Common angle]

$\therefore \triangle ABC \sim \triangle EDC$ [AA test of similarity]

One to one correspondence is $ABC \leftrightarrow EDC$

Q. 9

Are the triangles in the adjoining figure similar? If yes, by which test?

**SOLUTION:**

In $\triangle PQR$ and $\triangle LMN$,

$$\frac{PQ}{LM} = \frac{6}{3} = \frac{2}{1} \quad \text{(i)}$$

$$\frac{QR}{MN} = \frac{8}{4} = \frac{2}{1} \quad \text{(ii)}$$

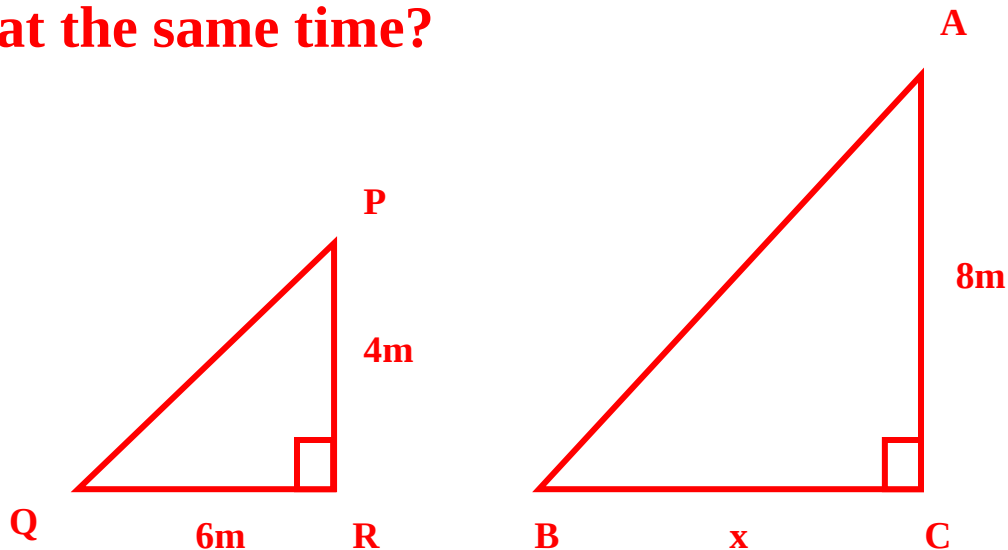
$$\frac{PR}{LN} = \frac{10}{5} = \frac{2}{1} \quad \text{(iii)}$$

$$\therefore \frac{PQ}{LM} = \frac{QR}{MN} = \frac{PR}{LN} \quad \text{[From (i), (ii) and (iii)]}$$

$\therefore \triangle PQR \sim \triangle LMN$ [SSS test of similarity]

Q. 10

As shown in the adjoining figure, two poles of height 8 m and 4 m are perpendicular to the ground. If the length of shadow of smaller pole due to sunlight is 6 m, then how long will be the shadow of the bigger pole at the same time?

**SOLUTION:**

Here, AC and PR represents the bigger and smaller poles, and BC and QR represents their shadows respectively.

Now, $\triangle ACB \sim \triangle PRQ$ [$\because$ Vertical poles and their shadows form similar figures]

$$\therefore \frac{CB}{RQ} = \frac{AC}{PR} \text{ [Corresponding sides of similar triangles]}$$

$$\therefore \frac{x}{6} = \frac{8}{4}$$

$$\therefore x = \frac{8 \times 6}{4}$$

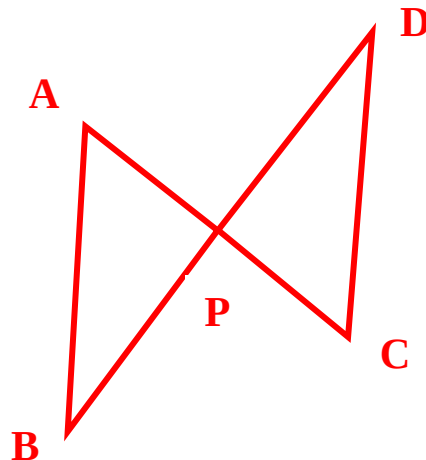
$$\therefore x = 12 \text{ m}$$

$\therefore$ The shadow of the bigger pole will be 12 meters long at that time.

Q. 11

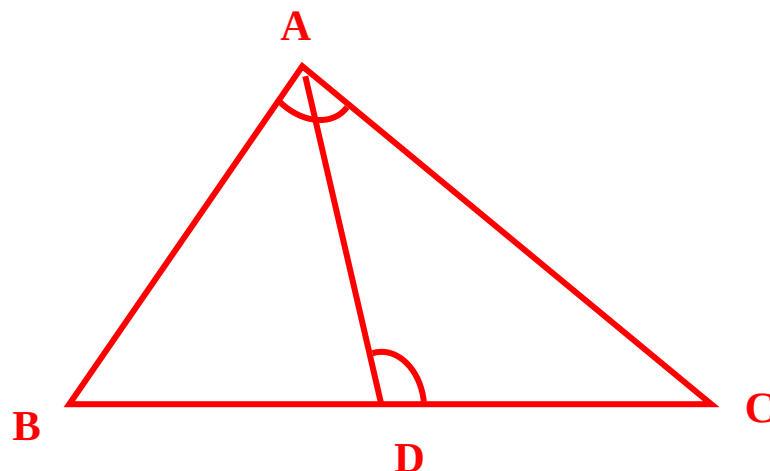
In the adjoining figure, seg AC and seg BD intersect each other in point P and $APCP = BPDP$ Prove that,

$$\triangle ABP \sim \triangle CDP$$



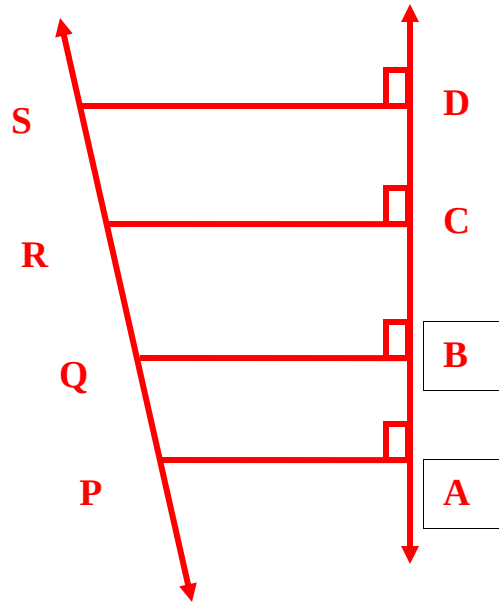
SOLUTION:**Proof:****In $\triangle ABP$ and $\triangle CDP$,** **$APCP = BPDP$ [Given]** **$\angle APB \cong \angle CPD$ [Vertically opposite angles]** **$\therefore \triangle ABP \sim \triangle CDP$ [SAS test of similarity]****Q. 12**

In the adjoining figure, in $\triangle ABC$, point D is on side BC such that, $\angle BAC = \angle ADC$. Prove that, $CA^2 = CB \times CD$,



SOLUTION:**Proof:****In $\triangle BAC$ and $\triangle ADC$,** **$\angle BAC \cong \angle ADC$ [Given]** **$\angle BCA \cong \angle ACD$ [Common angle]** **$\therefore \triangle BAC \sim \triangle ADC$ [AA test of similarity]** **$\therefore \frac{CA}{CD} = \frac{CB}{CA}$ [Corresponding sides of similar triangles]** **$\therefore CA \times CA = CB \times CD$** **$\therefore CA^2 = CB \times CD$** **Q. 13**

In the figure, seg PA, seg QB, seg RC and seg SD are perpendicular to line AD. $AB = 60$, $BC = 70$, $CD = 80$, $PS = 280$, then find PQ, QR and RS.



SOLUTION:

seg PA, seg QB, seg RC and seg SD are perpendicular to line AD. [Given]

$\therefore$ seg PA $\parallel$ seg QB $\parallel$ seg RC $\parallel$ seg SD (i) [Lines perpendicular to the same line are parallel to each other]

Let the value of PQ be x and that of QR be y. PS = PQ + QS [P – Q – S]

$$\therefore 280 - x + QS$$

$$\therefore QS = 280 - x \text{ (ii)}$$

Now, seg PA $\parallel$ seg QB $\parallel$ seg SD [From (i)]

$\therefore \frac{AB}{BD} = \frac{PQ}{QS}$ [Property of three parallel lines and their transversals]

$$\therefore \frac{AB}{BC+CD} = \frac{PQ}{QS} \quad [B - C - D]$$

$$\therefore \frac{60}{70+80} = \frac{x}{280-x}$$

$$\therefore \frac{60}{150} = \frac{x}{280-x}$$

$$\therefore \frac{2}{5} = \frac{x}{280-x}$$

$$\therefore 5x = 2(280 - x)$$

$$\therefore 5x = 560 - 2x$$

$$\therefore 7x = 560$$

$$\therefore x = \frac{560}{7} = 80$$

$$\therefore PQ = 80 \text{ units}$$

$$QS = 280 - x \text{ [From (ii)]}$$

$$= 280 - 80$$

$$= 200 \text{ units}$$

$$\text{But, } QS = QR + RS \text{ [Q – R – S]}$$

$$\therefore 200 = y + RS$$

$$\therefore RS = 200 - y \text{ (ii)}$$

Now, seg QB || seg RC || seg SD [From (i)]

$$\therefore \frac{BC}{CD} = \frac{QR}{RS} \text{ [Property of three parallel lines and their transversals]}$$

$$\therefore \frac{70}{80} = \frac{y}{200-y}$$

$$\therefore \frac{7}{8} = \frac{y}{200-y}$$

$$\therefore 8y = 7(200 - y)$$

$$\therefore 8y = 1400 - 7y$$

$$\therefore 15y = 1400$$

$$\therefore y = \frac{1400}{15} = \frac{280}{3}$$

$$\therefore QR = \frac{280}{3} \text{ units}$$

$$RS = 200 - 7 \quad \text{[From (iii)]}$$

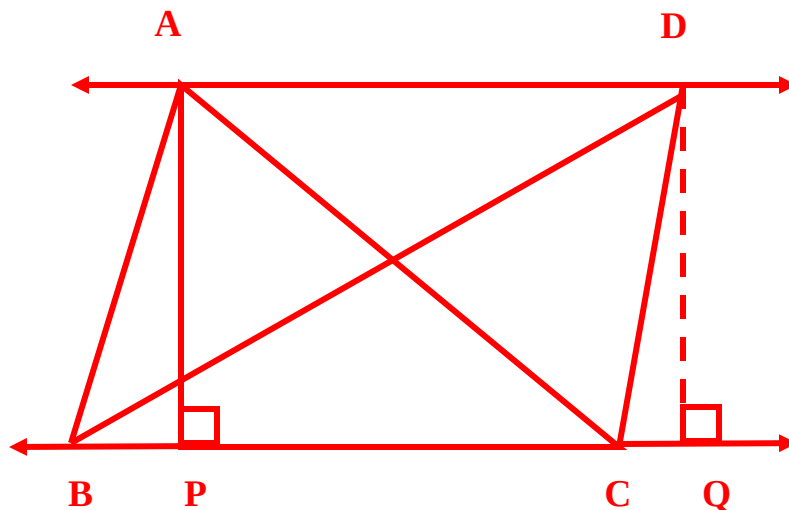
$$\begin{aligned}
 &= 200 - \frac{280}{3} \\
 &= \frac{(200 \times 3 - 280)}{3} \\
 &= \frac{(600 - 280)}{3} = \frac{320}{3}
 \end{aligned}$$

$$\therefore RS = 320/3 \text{ units}$$

Ans.: PQ = 80 units, QR = 280/3 units, RS = 320/3 units

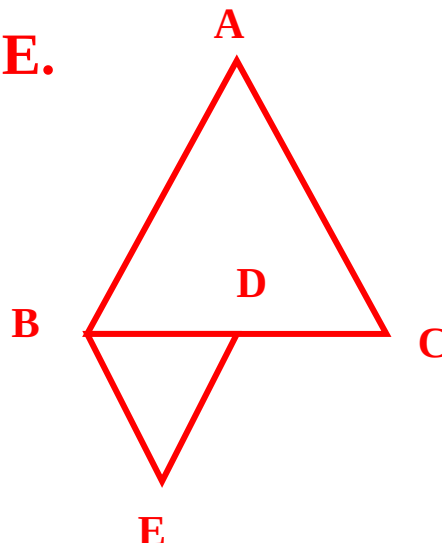
Q. 14

In the adjoining figure, $AP \perp BC$, $AD \parallel BC$, then find $A(\triangle ABC) : A(\triangle BCD)$.



SOLUTION:**Draw $DQ \perp BC$, $B - C - Q$** **$AD \parallel BC$ [Given]** **$\therefore AP = DQ$ [Perpendicular distance between two parallel lines is the same]** **$\triangle ABC$ and $\triangle BCD$ have same base BC .**

$$\frac{A(\triangle ABC)}{A(\triangle BCD)} = \frac{AP}{DQ} = \frac{AP}{AP} = 1$$

Ans.: $A(\triangle ABC): A(\triangle BCD) = 1:1$ **Q. 15** **ABC and BDE are two equilateral triangles such that D is mid-point of BC . Find the ratio of the areas of triangles ABC and BDE .**

SOLUTION:

$$\frac{A(\Delta ABC)}{A(\Delta BDE)} = \frac{BC^2}{BD^2}$$

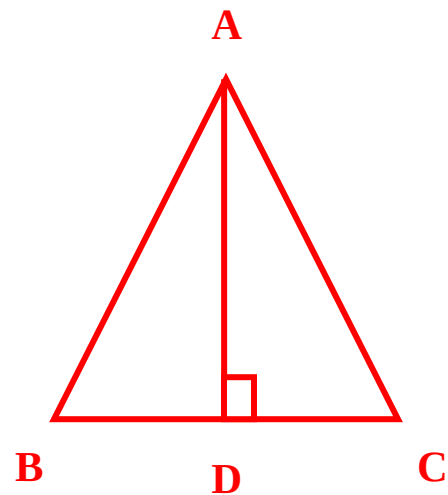
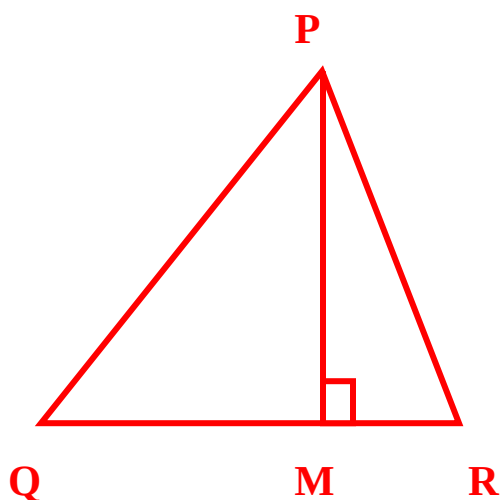
$$= \frac{2(BD)^2}{BD^2} \quad [\text{Since } BC = 2BD]$$

$$\frac{A(\Delta ABC)}{A(\Delta BDE)} = 4:1$$

$$\text{Ans.: } \frac{A(\Delta ABC)}{A(\Delta BDE)} = 4:1$$

Q. 16

$\Delta ABC \sim \Delta PQR$. Area of $\Delta ABC = 64 \text{ cm}^2$ and area of $\Delta PQR = 144 \text{ cm}^2$. Find the altitude PM, if $AD = 8 \text{ cm}$.



SOLUTION:

$$\frac{A(\Delta ABC)}{A(\Delta PQR)} = \frac{AD^2}{PM^2}$$

Ratio of areas of two triangles is equal to the ratio of the squares of corresponding heights.

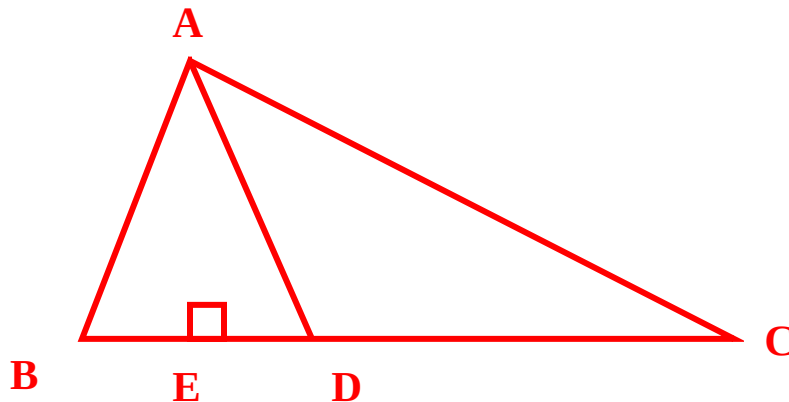
$$\frac{81}{121} = \frac{9^2}{PM^2}$$

Ans.: PM = 11

Q. 17

In ΔABC , B-D-C and BD = 7, BC = 20, then find

following ratio: $\frac{A(\Delta ABD)}{A(\Delta ABC)}$, $\frac{A(\Delta ABD)}{A(\Delta ADC)}$, $\frac{A(\Delta ADC)}{A(\Delta ABC)}$



SOLUTION:**Draw $AE \perp BC$, $B - E - C$**

$BC = BD + DC$ [$B - D - C$]

$\therefore 20 = 7 + DC$

$\therefore DC = 20 - 7 = 13$

i. $\triangle ABD$ and $\triangle ADC$ have same height AE .

$$\frac{A(\triangle ABD)}{A(\triangle ADC)} = \frac{BD}{DC} \text{ [Triangles having equal height]}$$

$$\therefore \frac{A(\triangle ABD)}{A(\triangle ADC)} = \frac{7}{13}$$

ii. $\triangle ABD$ and $\triangle ABC$ have same height AE .

$$\frac{A(\triangle ABD)}{A(\triangle ABC)} = \frac{BD}{BC} \text{ [Triangles having equal height]}$$

$$\therefore \frac{A(\triangle ABD)}{A(\triangle ABC)} = \frac{7}{20}$$

iii. $\triangle ADC$ and $\triangle ABC$ have same height AE .

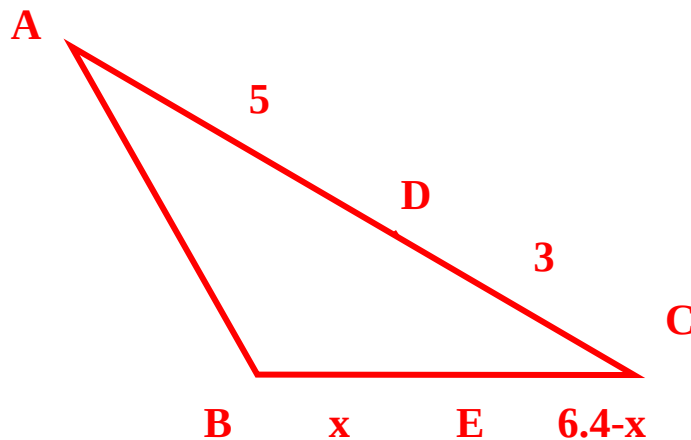
$$\frac{A(\triangle ADC)}{A(\triangle ABC)} = \frac{DC}{BC} \text{ [Triangles having equal height]}$$

$$\therefore \frac{A(\triangle ADC)}{A(\triangle ABC)} = \frac{13}{20}$$

$$\text{Ans.: } \frac{A(\Delta ABD)}{A(\Delta ADC)} = \frac{7}{13}, \frac{A(\Delta ABD)}{A(\Delta ABC)} = \frac{7}{20}, \frac{A(\Delta ADC)}{A(\Delta ABC)} = \frac{13}{20}$$

Q. 18

In the adjoining figure, $A - D - C$ and $B - E - C$. seg $DE \parallel$ side AB . If $AD = 5$, $DC = 3$, $BC = 6.4$, then find BE .



SOLUTION:

In ΔABC , seg $DE \parallel$ side AB [Given]

$$\therefore \frac{DC}{AD} = \frac{EC}{BE} \text{ [Basic proportionality theorem]}$$

$$\therefore \frac{3}{5} = \frac{(6.4 - x)}{x}$$

$$\therefore 3x = 5(6.4 - x)$$

$$\therefore 3x = 32 - 5x$$

$$\therefore 8x = 32$$

$$\therefore x = 32/8$$

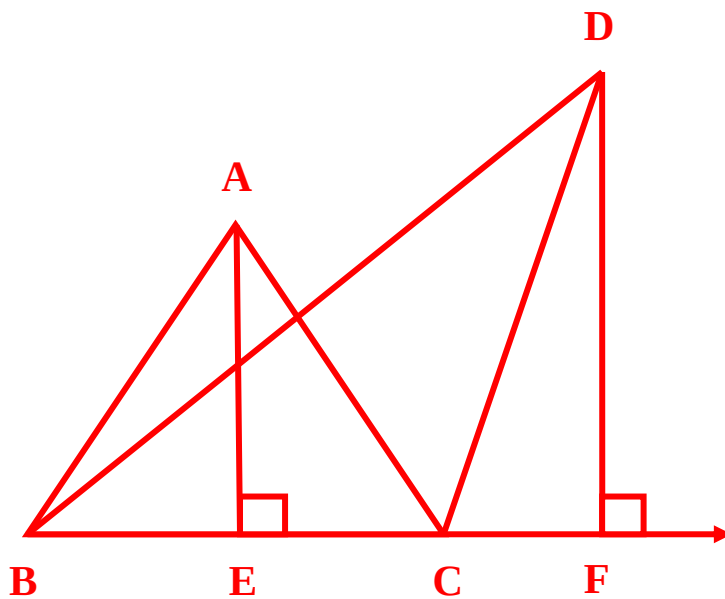
$$\therefore x = 4$$

$$\therefore BE = 4 \text{ units}$$

Q. 19

In the given figure, $AE \perp \text{seg } BC$, $\text{seg } DF \perp \text{line } BC$,

$AE = 4$, $DF = 6$, then find $\frac{A(\triangle ABC)}{A(\triangle DBC)}$



SOLUTION:

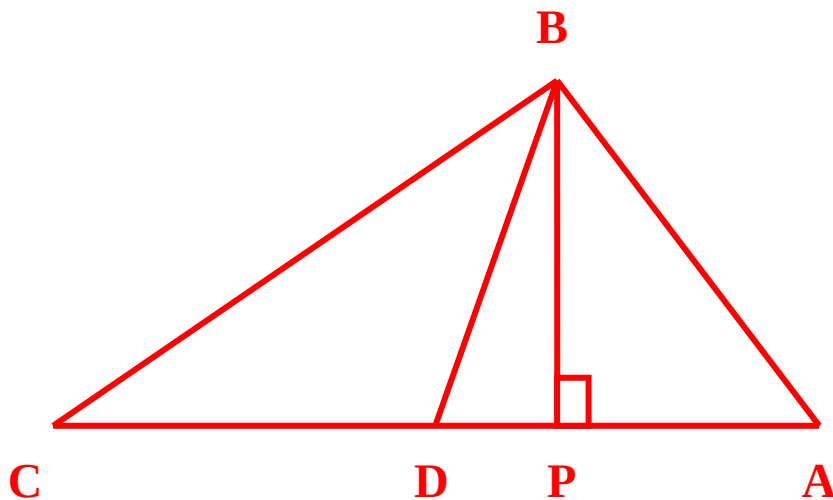
$\frac{A(\Delta ABC)}{A(\Delta DBC)} = \frac{AE}{DF} \dots\dots\dots$ (bases are equal; hence areas are proportional to heights)

$$\frac{A(\Delta ABC)}{A(\Delta DBC)} = \frac{4}{6} = \frac{2}{3}$$

Q. 20

In the following figure in ΔABC , point D is on side AC. If $AC = 16$, $DC = 9$ and $BP \perp AC$, then find the following ratios:

$$\frac{A(\Delta ABD)}{A(\Delta ABC)}, \frac{A(\Delta BDC)}{A(\Delta ABC)}, \frac{A(\Delta ABD)}{A(\Delta BDC)}$$



SOLUTION:

In ΔABC , point P and D are on side AC, hence B is the common vertex of ΔABD , ΔBDC , ΔABC and ΔAPB and their sides AD, DC, AC, and AP are collinear. Heights of all the triangles are equal. Hence, areas of these triangles are proportional to their bases. $AC = 16$, $DC = 9$

$$\therefore AD = 16 - 9 = 7$$

$$\therefore \frac{A(\Delta ABD)}{A(\Delta ABC)} = \frac{AD}{AC} = \frac{7}{16}$$

$$\frac{A(\Delta ABD)}{A(\Delta ABC)} = \frac{DC}{AC} = \frac{9}{16}$$

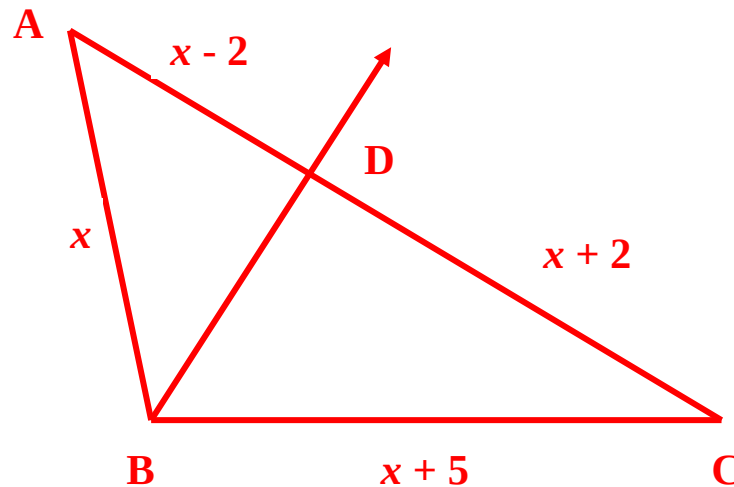
$$\frac{A(\Delta ABD)}{A(\Delta ABC)} = \frac{AD}{DC} = \frac{7}{9}$$

Triangles having

Equal heights

Q. 21

In ΔABC , seg BD bisects $\angle ABC$. If $AB = x$, $BC = x + 5$, $AD = x - 2$, $DC = x + 2$, then find the value of x .



SOLUTION:

In $\triangle ABC$, ray BD bisects $\angle ABC$

$\therefore$ by property of angle bisector of triangle,

$$\frac{AB}{BC} = \frac{AD}{DC}$$

$$\therefore \frac{x}{x+5} = \frac{x-2}{x+2}$$

$$\therefore x(x+2) = (x-2)(x+5)$$

$$\therefore x^2 + 2x = x(x+5) - 2(x+5)$$

$$\therefore \cancel{x^2} + 2x = \cancel{x^2} + 5x - 2x - 10$$

$$\therefore 2x = 3x - 10$$

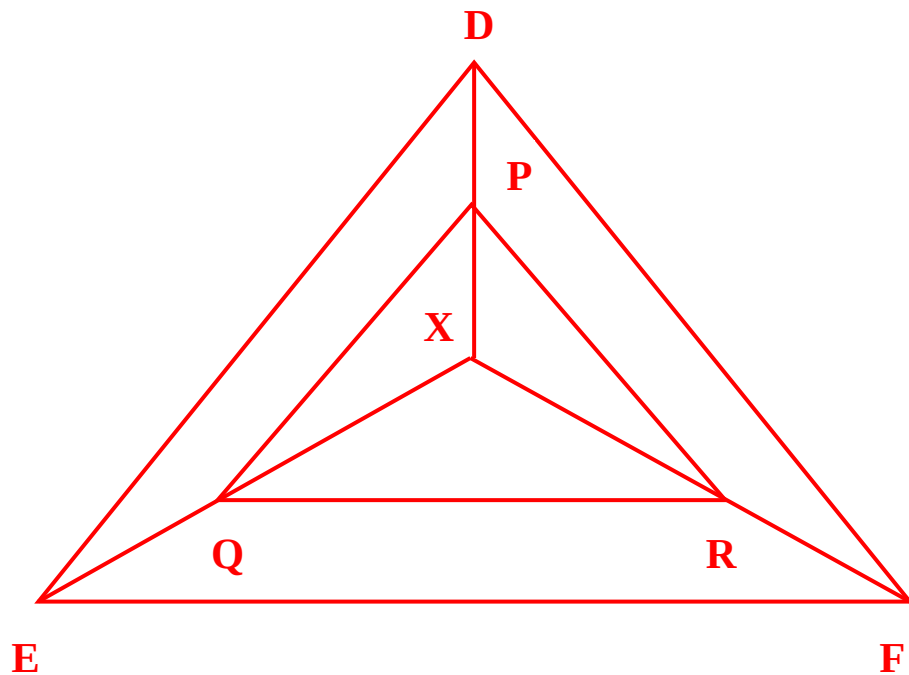
$$\therefore 2x - 3x = -10$$

$$\therefore -x = -10$$

$$\therefore x = 10$$

Q. 22

In the figure, X is any point in the interior of triangle. $\text{seg PQ} \parallel \text{seg DE}$, $\text{seg QR} \parallel \text{seg EF}$. Prove that $\text{seg PR} \parallel \text{seg DF}$.



SOLUTION:

In $\triangle XDE$, $PQ \parallel DE$... Given

$$\therefore \frac{XP}{PD} = \frac{XQ}{QE} \quad \dots \text{(I) (Basic proportionality theorem)}$$

In $\triangle XEF$, $QR \parallel EF$... Given

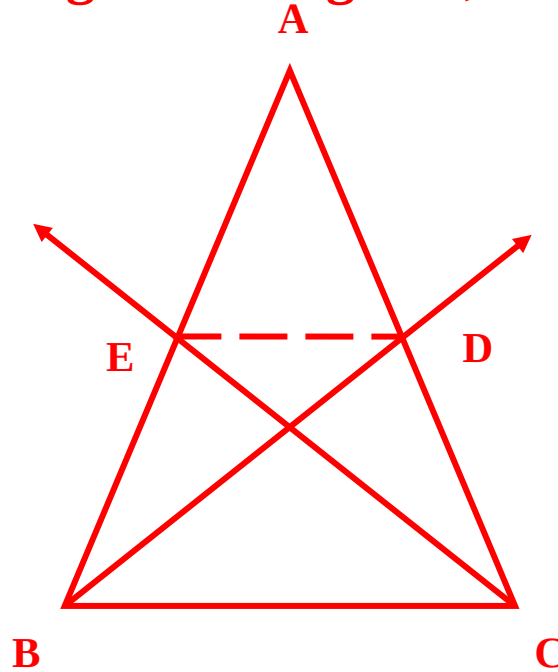
$$\therefore \frac{XQ}{QE} = \frac{XR}{RF} \quad \dots \text{(II) (Basic proportionality theorem)}$$

$$\therefore \frac{XP}{PD} = \frac{XR}{RF} \quad \dots \text{From (I) \& (II)}$$

$\therefore$ seg $PR \parallel$ seg DF ... (Converse of basic proportionality theorem)

Q. 23

In $\triangle ABC$, ray BD bisects $\angle ABC$ and ray CE bisects $\angle ACB$. If $\text{seg } AB \cong \text{seg } AC$; then prove that $ED \parallel BC$.



SOLUTION:

In $\triangle ABC$, ray BD is the bisector of $\angle ABC$

$\therefore$ by property of angle bisector of a triangle,

$$\frac{AB}{BC} = \frac{AD}{DC} \quad \dots (1)$$

In $\triangle ABC$, ray CE is the bisector of $\angle ACB$

$\therefore$ by property of angle bisector of a triangle,

$$\frac{AC}{BC} = \frac{AE}{EB} \quad \dots (2)$$

$$\text{seg } AB \cong \text{seg } AC \text{ (Given)} \quad \dots (3)$$

$$\therefore \frac{AB}{BC} = \frac{AC}{BC} \dots \text{From (1), (2) \& (3)} \dots (4)$$

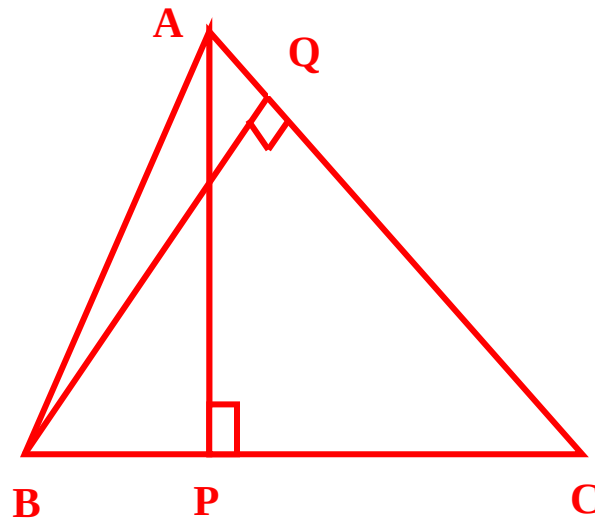
$$\text{In } \triangle ABC, \frac{AE}{EB} = \frac{AD}{DC} \dots \text{From (1), (2) \& (4)}$$

**By converse of basic proportionality theorem, seg
 $ED \parallel$ side BC**

i.e. $ED \parallel BC$

Q. 24

In $\triangle ABC$, $AP \perp BC$, $BQ \perp AC$. $B - P - C$, $A - Q - C$; then prove that $\triangle CPA \sim \triangle CQB$. If $AP = 7$, $BQ = 8$, $BC = 12$; then find AC .

**SOLUTION:**

In $\triangle CPA$ and $\triangle CQB$,

$\angle CPA \cong \angle CQB$... (Each measures 90°)

$\angle ACP \cong \angle BCQ$... (Common angle)

$\therefore \triangle CPA \cong \triangle CQB$... (AA test of similarity)

$\therefore \frac{AP}{BQ} = \frac{AC}{BC}$... (Corresponding sides of similar

triangles are in proportion)

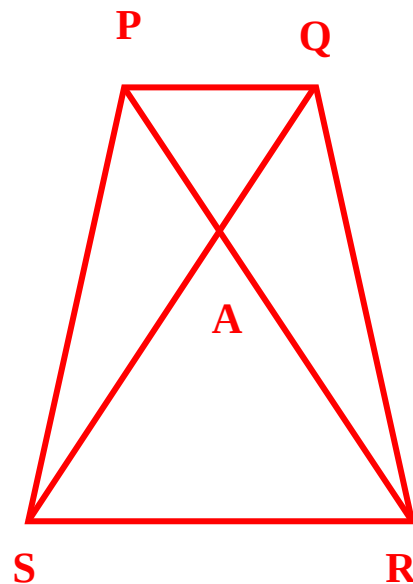
$$\therefore \frac{7}{8} = \frac{AC}{12}$$

$$\therefore AC \times 8 = 7 \times 12$$

$$\therefore AC = 10.5$$

Q. 25

In trapezium PQRS, side PQ $\parallel$ side SR, AR = 5AP, AS = 5AQ; then prove that, SR = 5PQ.



SOLUTION:

Side PQ $\parallel$ side SR and line QS is the transversal

$\therefore \angle PQS \cong \angle RSQ \quad \dots$ (Alternate angles theorem)

$$\text{i.e. } \angle PQA \cong \angle RSA \quad \dots (\text{Q} - \text{A} - \text{S}) \quad \dots (1)$$

In $\triangle PQA$ and $\triangle RSA$,

$$\angle PQA \cong \angle RSA \quad \dots \text{from (1)}$$

$$\angle PAQ \cong \angle RAS \quad \dots (\text{Vertically opposite angles})$$

$$\therefore \triangle PQA \sim \triangle RSA \quad \dots (\text{AA test of similarity})$$

$$\therefore \frac{PQ}{RS} = \frac{AQ}{AS} = \frac{AP}{AR} \quad \dots (\text{Corresponding sides of similar triangles are in proportion}) \quad \dots (2)$$

$$AR = 5AP \quad \dots (\text{Given}) \quad \dots (3)$$

Substituting (3) in (2) we get,

$$\frac{PQ}{SR} = \frac{AQ}{AS} = \frac{\cancel{AP}}{\cancel{5AP}}$$

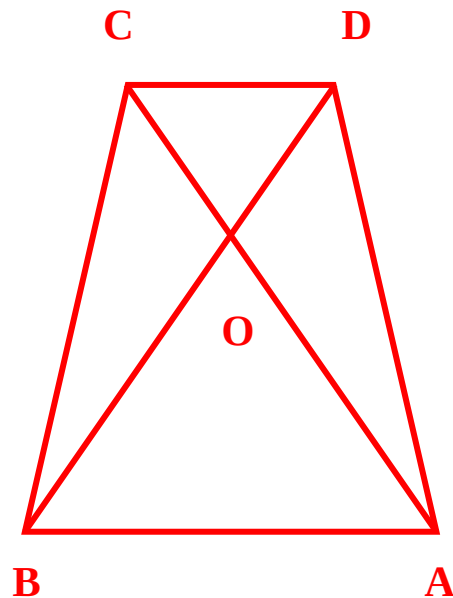
$$\therefore \frac{PQ}{SR} = \frac{AQ}{AS} = \frac{1}{5} \quad \dots (4)$$

$$\therefore \frac{PQ}{SR} = \frac{1}{5} \quad \dots \text{From (4)}$$

$$\therefore SR = 5PQ$$

Q. 26

In trapezium ABCD, side $AB \parallel$ side DC , diagonals AC and BD intersect in point O . If $AB = 20$, $DC = 6$, $OB = 15$, then find OD .

**SOLUTION:**

Side $AB \parallel$ side DC and line DB is the transversal,

$\angle CDB \cong \angle ABD$... (Alternate angles theorem)

i.e. $\angle CDO \cong \angle ABO$... (B – O – D) ... (1)

In $\triangle COD$ and $\triangle AOB$,

$$\angle CDO \cong \angle ABO \quad \dots \text{From (1)}$$

$$\angle COD \cong \angle AOB \quad \dots \text{(Vertically opposite angles)}$$

$$\therefore \triangle COD \sim \triangle AOB \quad \dots \text{(AA test of similarity)}$$

$$\therefore \frac{OD}{OB} = \frac{DC}{AB} \quad \dots \text{(Corresponding sides of similar triangles are in proportion)}$$

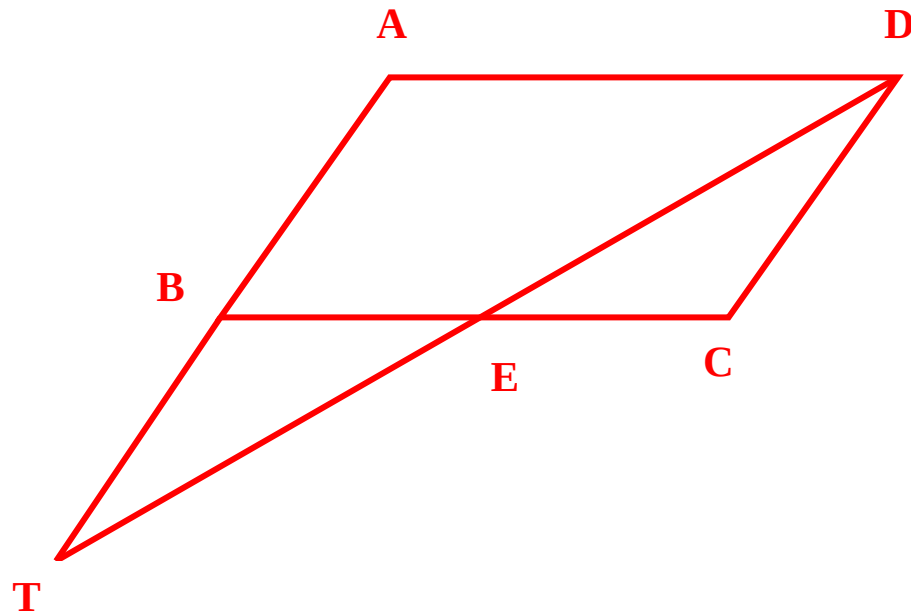
$$\therefore \frac{OD}{15} = \frac{6}{20}$$

$$\therefore OD \times 20 = 6 \times 15$$

$$\therefore OD = 4.5$$

Q. 27

□ ABCD is a parallelogram point E is on side BC. Line DE intersects ray AB in point T. Prove that $DE \times BE = CE \times TE$



SOLUTION:

Seg AB $\parallel$ seg CD ... (Opposite sides of parallelogram are parallel)

i.e. seg AT $\parallel$ seg CD ... (A – B – T)

Line TD is the transversal,

$\therefore \angle ATD \cong \angle CDT$... (Alternate angles theorem)

i.e. $\angle BTE \cong \angle CDE$... (A – B – T, T – E – D) ... (1)

In $\triangle BET$ & $\triangle CED$,

$\angle BTE \cong \angle CDE$... From (1)

$\angle BET \cong \angle CED$... (Vertically opposite angles)

$\therefore \triangle BET \sim \triangle CED$... (AA test of similarity)

$\therefore \frac{BE}{CE} = \frac{TE}{DE}$... (Corresponding sides of similar triangles are in proportion)

$$\therefore BE \times DE = CE \times TE$$

Q. 28

The ratio of corresponding sides of similar triangles is 3 : 5; then find the ratio of their areas.

SOLUTION:

Let the corresponding sides of two similar triangles be s_1 and s_2 and their respective areas be A_1 and A_2

$$s_1 : s_2 = 3 : 5 \quad \dots \text{(Given)}$$

$$\therefore \frac{s_1}{s_2} = \frac{3}{5} \quad \dots (1)$$

The two triangles are similar

$$\therefore \frac{A_1}{A_2} = \frac{s_1^2}{s_2^2} \quad \dots \text{(Theorem of areas of similar triangles)}$$

$$\therefore \frac{A_1}{A_2} = \left(\frac{s_1}{s_2}\right)^2$$

$$\therefore \frac{A_1}{A_2} = \left(\frac{3}{5}\right)^2 \dots (\text{From 1})$$

$$\therefore \frac{A_1}{A_2} = \frac{9}{25}$$

$$\therefore A_1 : A_2 = 9 : 25$$

Ans.: The ratio of the areas of the two similar triangles is 9 : 25

Q. 29

Areas of two similar triangles are 225 sq.cm. and 81 sq.cm. If a side of the smaller triangle is 12 cm, then find corresponding side of bigger triangle.

SOLUTION:

Let the areas of two similar triangles be A_1 and A_2 and their respective sides be s_1 and s_2 .

$A_1 = 225$ sq.cm., $A_2 = 81$ sq.cm. and $s_2 = 12$ cm

The two triangles are similar

$\therefore$ by theorem of areas of similar triangles,

$$\frac{A_1}{A_2} = \frac{s_1^2}{s_2^2}$$

$$\therefore \frac{225}{81} = \frac{s_1^2}{12^2}$$

$$\therefore s_1^2 = \frac{225 \times 12^2}{81}$$

$\therefore s_1 = \frac{15 \times 12}{9} \quad \dots \text{(Taking square roots on both the sides)}$

$$\therefore s_1 = 20 \text{ cm}$$

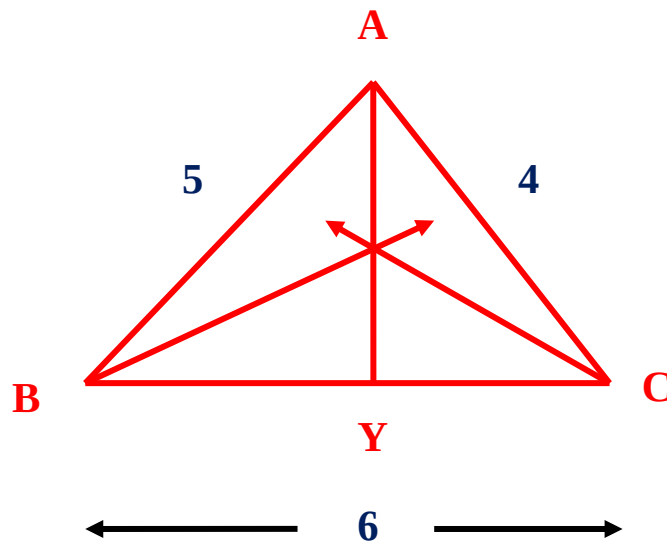
Ans.: The corresponding side of the bigger triangle is 20 cm.

Q. 30

In the figure, bisectors of $\angle B$ and $\angle C$ of ΔABC intersect each other in point X. Line AX intersects

side BC in point Y. $AB = 5$, $AC = 4$, $BC = 6$ then find

$$\frac{AX}{XY}$$



SOLUTION:

In $\triangle ABY$, ray BX bisects $\angle ABY$

$\therefore$ by property of angle bisector of triangle,

$$\frac{AB}{BY} = \frac{AX}{XY} \quad \dots (1)$$

In $\triangle ACY$, ray CX bisects $\angle ACY$

$\therefore$ by property of angle bisector of triangle,

$$\frac{AC}{CY} = \frac{AX}{XY} \quad \dots (2)$$

$$\frac{AB}{BY} = \frac{AC}{CY} = \frac{AX}{XY} \quad \dots \text{From (1) and (2)}$$

$$\therefore \frac{5}{BY} = \frac{4}{CY} = \frac{AX}{XY}$$

By theorem on equal ratios,

$$\frac{5 + 4}{BY + CY} = \frac{AX}{XY}$$

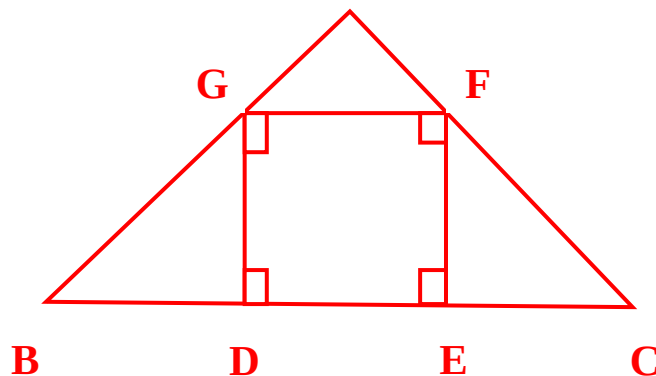
$$\therefore \frac{9}{BC} = \frac{AX}{XY} \quad \dots (B - Y - C)$$

$$\therefore \frac{9}{6} = \frac{AX}{XY}$$

$$\therefore \frac{AX}{XY} = \frac{3}{2}$$

Q. 31

In figure, the vertices of square DEFG are on the sides of $\triangle ABC$. $\angle A = 90^\circ$. Then prove that $DE^2 = BD \times EC$.



SOLUTION:

□ DEFG is a square

$$\therefore DE = EF = GF = GD \dots (\text{Sides of square}) \dots (1)$$

$$\angle GDE = \angle DEF = 90^\circ \dots (\text{Angles of a square})$$

$$\therefore \text{seg } GD \perp \text{side } BC \text{ and seg } EF \perp \text{side } BC$$

In $\triangle BAC$ and $\triangle BDG$,

$$\angle BAC \cong \angle BDG \dots (\text{Each measures } 90^\circ)$$

$$\angle ABC \cong \angle DBG \dots (\text{Common angle})$$

$$\therefore \triangle BAC \sim \triangle BDG \dots (\text{AA test of similarity}) \dots (2)$$

$$\text{Similarly } \triangle BAC \sim \triangle FEC \dots (3)$$

$$\therefore \triangle BDG \sim \triangle FEC \dots \text{From (2) and (3)}$$

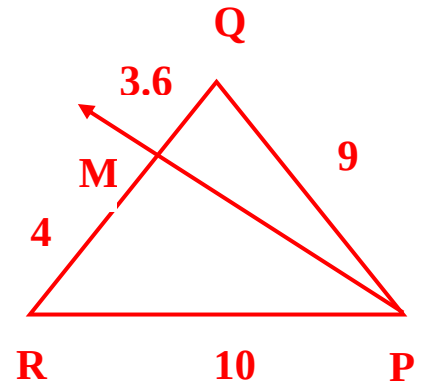
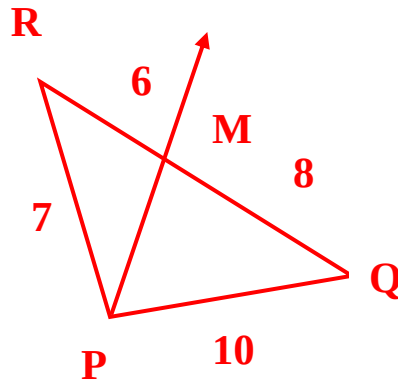
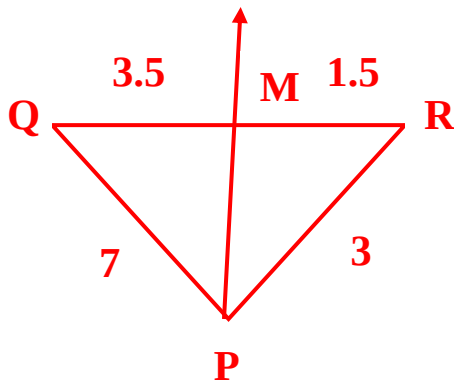
$$\therefore \frac{BD}{EF} = \frac{GD}{EC} \dots (\text{Corresponding sides of similar triangles are in proportion})$$

$$\therefore \frac{BD}{DE} = \frac{DE}{EC} \dots \text{From (1)}$$

$$\therefore DE^2 = BD \times EC$$

Q. 32

Given below are some triangles and lengths of line segments. Identify in which figures, ray PM is the bisector of $\angle QPR$.



SOLUTION:

(i) In $\triangle PQR$,

$$\frac{PQ}{PR} = \frac{7}{3} \quad \dots (i)$$

$$\frac{QM}{RM} = \frac{3.5}{1.5} = \frac{35}{15} = \frac{7}{3} \quad \dots (ii)$$

$$\therefore \frac{PQ}{PR} = \frac{QM}{RM} \quad \dots \text{From (i) \& (ii)}$$

$\therefore$ Ray RM is the bisector of $\angle QPR$. (Converse of angle bisector theorem)

(ii) In ΔPQR ,

$$\frac{PQ}{PR} = \frac{10}{7} \quad \dots (i)$$

$$\frac{QM}{RM} = \frac{8}{6} = \frac{4}{3} \quad \dots (ii)$$

$$\therefore \frac{PQ}{PR} \neq \frac{QM}{RM} \quad \dots \text{From (i) \& (ii)}$$

$\therefore$ Ray RM is not the bisector of $\angle QPR$.

(iii) In ΔPQR ,

$$\frac{PQ}{PR} = \frac{9}{10} \quad \dots (i)$$

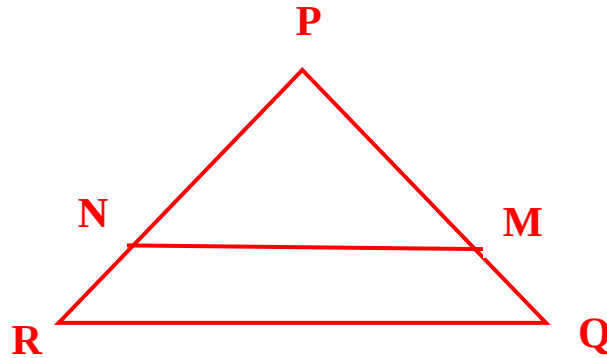
$$\frac{QM}{RM} = \frac{3.6}{4} = \frac{36}{40} = \frac{9}{10} \quad \dots (ii)$$

$$\therefore \frac{PQ}{PR} = \frac{QM}{RM} \quad \dots \text{From (i) \& (ii)}$$

$\therefore$ Ray RM is the bisector of $\angle QPR$ (Converse of angle bisector theorem)

Q. 33

In $\triangle PQR$, $PM = 15$, $PQ = 25$, $NR = 8$. State whether line NM is parallel to side RQ . Give reason.



SOLUTION:

$$PN + NR = PR \text{ [P - N - R]}$$

$$\therefore PN + 8 = 20$$

$$\therefore PN = 12$$

$$\text{Also, } PM + MQ = PQ \text{ [P - M - Q]}$$

$$\therefore 15 + MQ = 25$$

$$\therefore MQ = 10$$

$$\frac{PN}{NR} = \frac{12}{8} = \frac{3}{2} \quad \dots \text{ (i)}$$

$$\frac{PM}{MQ} = \frac{15}{10} = \frac{3}{2} \quad \dots \text{ (ii)}$$

In $\triangle PQR$,

$$\frac{PN}{NR} = \frac{PM}{MQ}$$

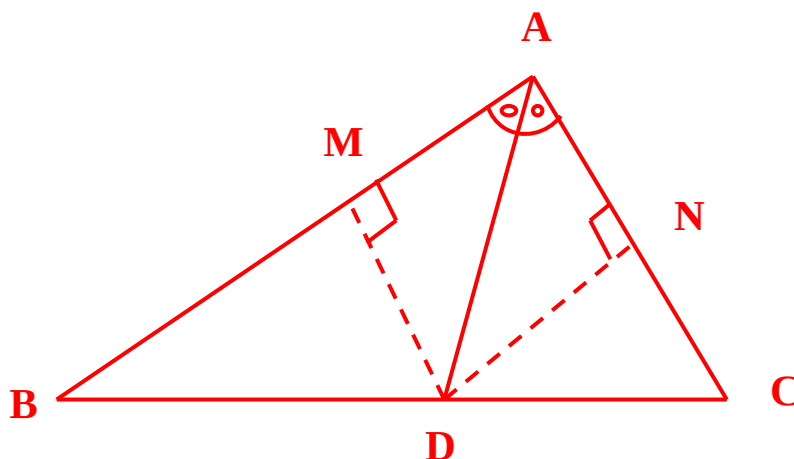
... From (i) & (ii)

$\therefore$ Line $NM \parallel$ side RQ (Converse of basic proportionality theorem)

Q. 34

Use the following properties and write the proof as per the given diagram.

- i. The areas of two triangles of equal height are proportional to their bases.
- ii. Every point on the bisector of an angle is equidistant from the sides of the angle.



SOLUTION:**Given:** In $\triangle CAB$, ray AD bisects $\angle A$ **To prove:** $\frac{AB}{AC} = \frac{BD}{DC}$ **Construction:** Draw seg DM $\perp$ seg AB A – M – B and seg DN $\perp$ seg AC, A – N – C.**Proof:**In $\triangle ABC$, Point D is on angle bisector of $\angle A$. [Given] $\therefore$ DM = DN [Every point on the bisector of an angle is equidistant from the sides of the angle]
$$\frac{A(\triangle ABD)}{A(\triangle ACD)} = \frac{AB \times DM}{AC \times DN}$$

[Ratio of areas of two triangles is equal to the ratio of the product of their bases and corresponding heights] ... (i)

$$\therefore \frac{A(\triangle ABD)}{A(\triangle ACD)} = \frac{AB}{AC}$$

... (ii) [From (i)]

Also, $\triangle ABD$ and $\triangle ACD$ have equal height.
$$\therefore \frac{A(\triangle ABD)}{A(\triangle ACD)} = \frac{BD}{CD}$$

(iii) [Triangles having equal height]

$$\therefore \frac{AB}{AC} = \frac{BD}{DC}$$

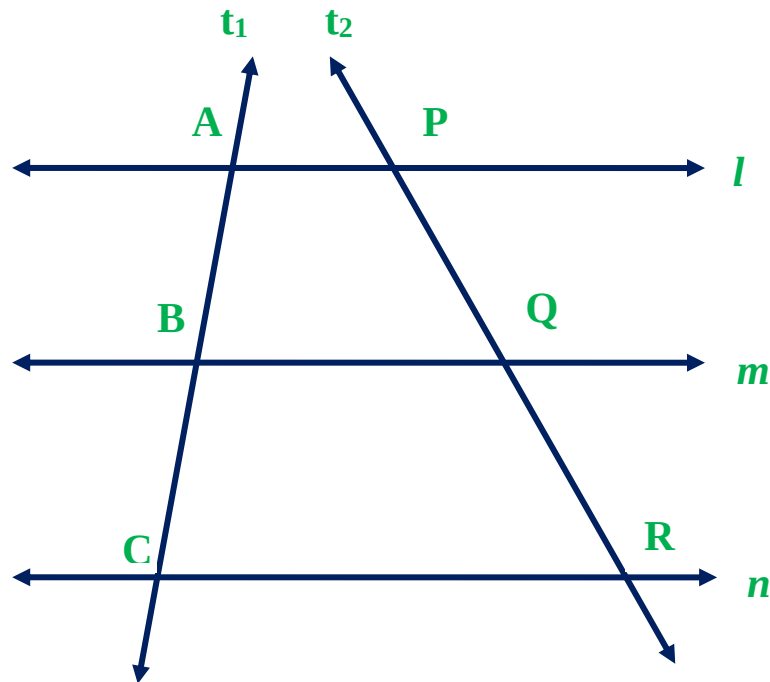
[From (ii) and (iii)]

Q. 35

- i. Draw three parallel lines.
- ii. Label them as l, m, n.
- iii. Draw transversals t1 and t2.
- iv. AB and BC are intercepts on transversal t1.
- v. PQ and QR are intercepts on transversal t2.
- vi. Find ratios $\frac{AB}{BC}$ and $\frac{PQ}{QR}$

AB = 1.5 cm, BC = 2.1 cm, PQ = 1.7 cm, QR = 2.3 cm
You will find that they are almost equal. Verify that they are equal.

SOLUTION:



$$\frac{AB}{BC} = \frac{1.5}{2.1} = 0.714 = 0.7$$

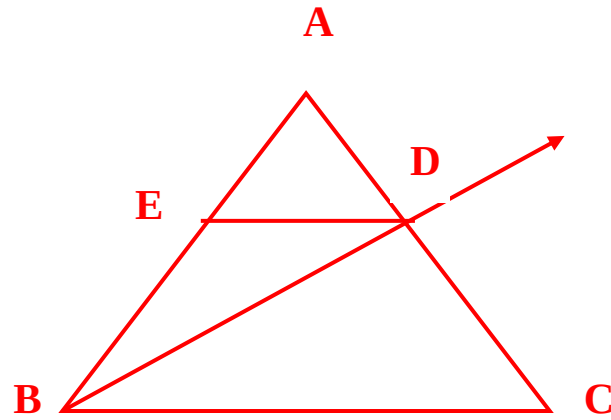
$$\frac{PQ}{QR} = \frac{1.7}{2.3} = 0.739 = 0.7$$

$$\therefore \frac{AB}{BC} = \frac{PQ}{QR}$$

Q. 36

In $\triangle ABC$, ray BD bisects $\angle ABC$. $A - D - C$, side DE

$\parallel$ side BC , $A - E - B$, then prove that $\frac{AB}{BC} = \frac{AE}{EB}$



SOLUTION:

In $\triangle ABC$, ray BD bisects $\angle B$... Given

$$\therefore \frac{AB}{BC} = \frac{AD}{DC} \quad \dots \text{(i) Angle bisector theorem}$$

In $\triangle ABC$, $DE \parallel BC$... Given

$$\therefore \frac{AE}{EB} = \frac{AD}{DC} \quad \dots \text{(ii) Basic proportionality theorem}$$

$$\therefore \frac{AB}{BC} = \frac{AE}{EB} \quad \dots \text{From (i) \& (ii)}$$

Q. 37

$\triangle LMN \sim \triangle PQR$, $9 \times A(\triangle PQR) = 16 \times A(\triangle LMN)$. If $QR = 20$, then find MN .

SOLUTION:

$$9 \times A(\Delta PQR) = 16 \times A(\Delta LMN) \text{ [Given]}$$

$$\therefore \frac{A(\Delta LMN)}{A(\Delta PQR)} = \frac{9}{16} \quad \dots \text{ (i)}$$

Now, $\Delta LMN \sim \Delta PQR$ [Given]

$$\therefore \frac{A(\Delta LMN)}{A(\Delta PQR)} = \frac{MN^2}{QR^2} \quad \dots \text{ (ii) [Theorem of areas}$$

of similar triangles]

$$\therefore \frac{MN^2}{QR^2} = \frac{9}{16} \quad \dots \text{ [From (i) and (ii)]}$$

$$\therefore \frac{MN}{QR} = \frac{3}{4} \quad \dots \text{ [Taking square root of both sides]}$$

$$\therefore \frac{MN}{20} = \frac{3}{4}$$

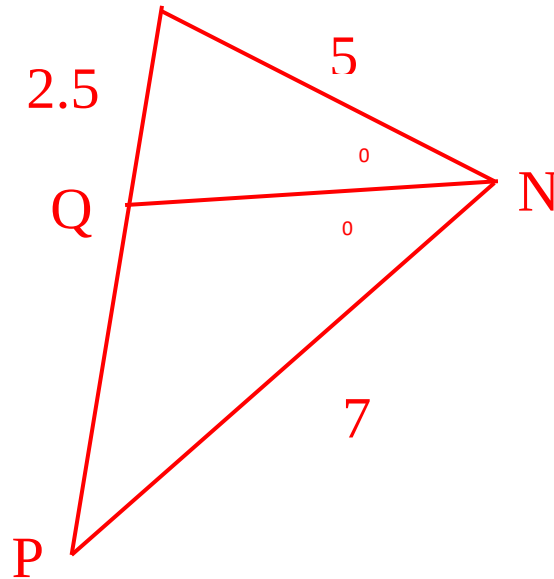
$$\therefore MN = \frac{20 \times 3}{4}$$

$$\therefore MN = 15 \text{ units}$$

Ans: $MN = 15$ units

Q. 38

In $\triangle MNP$, NQ is a bisector of $\angle N$. If $MN = 5$, $PN = 7$, $MQ = 2.5$, then find $P\widehat{M}$

**SOLUTION:**

In $\triangle MNP$, ray NQ bisects $\angle MNP$

$\therefore$ By property of triangle bisector of triangle,

$$= \frac{MQ}{QP}$$

$$\therefore \frac{MN}{NP} = \frac{MQ}{QP}$$

$$\therefore \frac{5}{7} = \frac{2.5}{QP}$$

$$\therefore \frac{5}{7} = \frac{2.5}{QP}$$

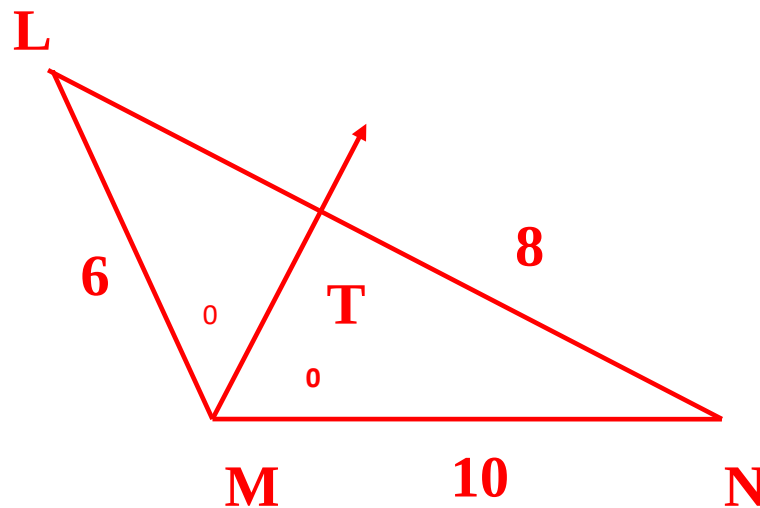
$$\therefore QP = \frac{7 \times 2.5}{5}$$

$$\therefore QP = 3.5$$

Ans.: $QP = 3.5$

Q. 39

In $\triangle LMN$, ray MT bisects $\angle LMN$. If $LM = 6$, $MN = 10$, $TN = 8$ then find LT



SOLUTION:

In $\triangle LMN$, ray MT bisects $\angle LMN$

$\therefore$ By property of angle bisector of triangle,

$$\frac{LM}{MN} = \frac{LT}{TN}$$

$$\therefore \frac{6}{10} = \frac{LT}{8}$$

$$\therefore LT \times 10 = 6 \times 8$$

$$\therefore LT = \frac{6 \times 8}{10}$$

$$\text{Ans.: } LT = 4.8$$

Q. 40

$\Delta LMN \sim \Delta PQR$, $9 \times A(\Delta PQR) = 16 \times A(\Delta LMN)$

If $QR = 20$, then, find MN

SOLUTION:

$\Delta LMN \sim \Delta PQR$

$$9 \times A(\Delta PQR) = 16 \times A(\Delta LMN)$$

$$\therefore \frac{A(\Delta LMN)}{A(\Delta PQR)} = \frac{9}{16}$$

$$\text{Now, } \frac{A(\Delta LMN)}{A(\Delta PQR)} = \frac{MN^2}{QR^2}$$

{Theorem of area of similar triangles}

$$\therefore \frac{9}{16} = \frac{MN^2}{QR^2}$$

$$\therefore \frac{MN}{QR} = \frac{3}{4}$$

(Taking square roots of both sides)

$$\therefore \frac{MN}{20} = \frac{3}{4}$$

$$\therefore MN = \frac{20 \times 3}{4}$$

$$\therefore MN = 15$$

Ans.: MN = 15

Q. 41

A (Δ ABC) and A (Δ DEF) are equilateral triangles.

If A (Δ ABC) : A(Δ DEF) = 1 : 2 and AB = 4. Find DE.

SOLUTION:

A (Δ ABC) and A (Δ DEF) are equilateral triangles.

$$\therefore \angle A = \angle B = \angle C = \angle D = \angle E = \angle F$$

(Angles of equilateral triangles)

In $\triangle ABC$ and $\triangle DEF$

$$\angle A \cong \angle D \quad \dots \text{(Each measures } 60^\circ)$$

$$\angle B \cong \angle E$$

$$\therefore \triangle ABC \sim \triangle DEF \quad \dots \text{(AA test of similarity)}$$

By theorem of areas of similar triangle

$$\frac{A(\triangle ABC)}{A(\triangle DEF)} = \frac{AB^2}{DE^2} \quad \dots \quad (1)$$

$$A(\triangle ABC) : A(\triangle DEF) = 1 : 2 \text{ and } AB = 4$$

$$\text{(Given)} \quad \dots \quad (2)$$

$$\therefore \frac{1}{2} = \frac{4^2}{DE^2}$$

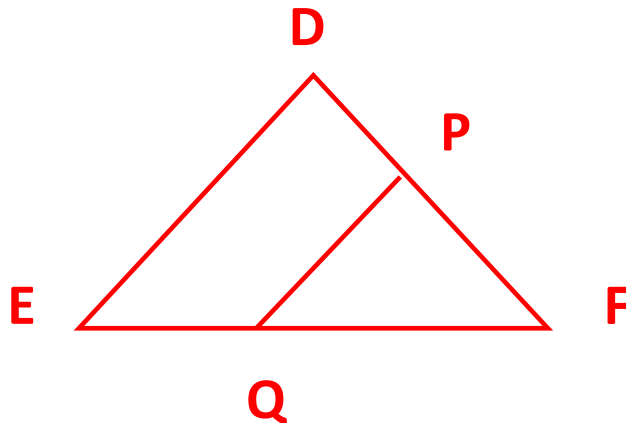
$$\therefore DE^2 = 4^2 \times 2$$

$$\therefore DE = 4\sqrt{2} \quad \dots \text{(Taking square roots of both sides)}$$

$$\text{Ans.: } DE = 4\sqrt{2}$$

Q. 42

In figure seg PQ $\parallel$ seg DE A (Δ PQF) = 20 units,
 PF = 2 DP, then find A ($\square$ DPQE) by completing the
 following activity



SOLUTION:

A (Δ PQF) = 20 units, PF = 2DP,

Let us assume DP = x

$$\therefore \text{PF} = 2x$$

$$\text{DF} = \text{DP} + \boxed{\text{PF}} = \boxed{x} + \boxed{2x} = 3x$$

In Δ FDE and Δ FPQ

$$\angle \text{FDE} = \angle \boxed{\text{FPQ}} \dots\dots\dots(\text{Corresponding angles})$$

$$\angle \text{FED} = \angle \boxed{\text{FPQ}} \dots\dots\dots(\text{Corresponding angles})$$

$$\therefore \triangle FDE \sim \triangle FPQ$$

$$\therefore \frac{A(\triangle FDE)}{A(\triangle FPQ)} = \frac{DF^3}{PF^2} = \frac{(3X)^3}{(2X)^2} = \frac{9}{4}$$

$$A(\triangle FDE) = \frac{9}{4} A(\triangle FPQ) = \frac{9}{4} \times \boxed{20} = \boxed{45 \text{ units}}$$

$$A(\square DPQE) = A(\triangle FDE) - A(\triangle FPQ)$$

$$= \boxed{45} - \boxed{20}$$

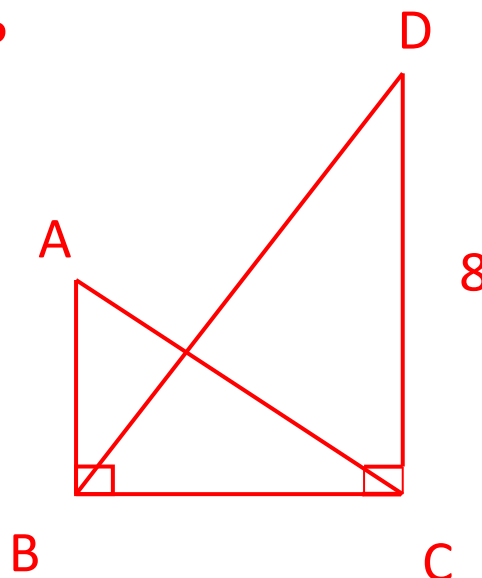
$$= \boxed{25}$$

(Note: Answers are in given green colour in the boxes inserted)

Q. 43

In figure $\angle ABC = \angle DCB = 90^\circ$ $AB = 6$, $DC = 8$;

Then $\frac{A(\triangle ABC)}{A(\triangle DCB)} = ?$



SOLUTION:

$\triangle ABC$ and $\triangle DCB$ have same base BC

Areas of triangle with equal bases are proportional to their corresponding heights

$$\therefore \frac{A(\triangle ABC)}{A(\triangle DCB)} = \frac{AB}{DC}$$

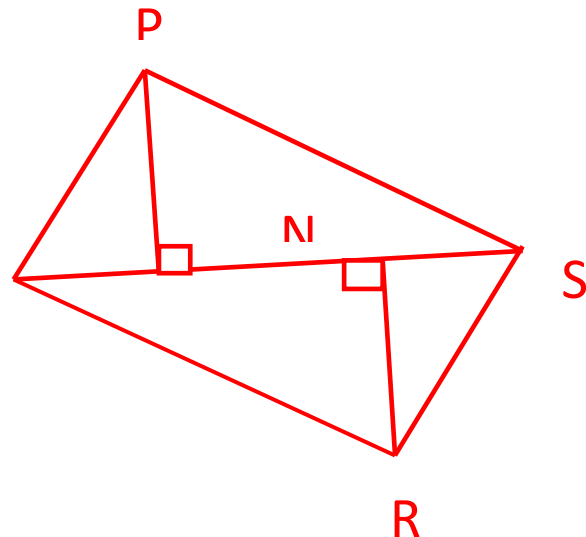
$$\therefore \frac{A(\triangle ABC)}{A(\triangle DCB)} = \frac{6}{8}$$

$$\therefore \frac{A(\triangle ABC)}{A(\triangle DCB)} = \frac{3}{4}$$

Ans. $\frac{A(\triangle ABC)}{A(\triangle DCB)} = \frac{3}{4}$

Q. 44

In figure, $PM = 10$ cm, $A(\triangle PQS) = 10$ cm, $A(\triangle QRS) = 100$ cm, then find NR



SOLUTION:

ΔPQS and ΔQRS have same base QS.

Areas of triangles with equal bases are proportional to their corresponding heights.

$$\therefore \frac{A(\Delta PQS)}{A(\Delta QRS)} = \frac{PM}{RN}$$

$$\therefore \frac{100}{110} = \frac{10}{NR}$$

$$\therefore NR = \frac{110 \times 10}{100}$$

$$\therefore NR = 11\text{cm}$$

Ans : NR = 11cm

Q. 45

Ratio of areas of two triangles with equal heights is 2:3. If base of the similar triangle is 6 cm then what is the corresponding base of the bigger triangle?

SOLUTION:

Let the areas of triangles be A_1 and A_2

Let their respective bases be b_1 and b_2

$A_1 : A_2 = 2:3$ and $b_1 = 6 \text{ cm}$... (Given)

The triangles are of equal height.

Area of triangle with equal heights is proportional to their corresponding bases.

$$\therefore \frac{A_1}{A_2} = \frac{b_1}{b_2}$$

$$\therefore \frac{2}{3} = \frac{6}{b_2}$$

$$\therefore b_2 = 9 \text{ cm}$$

Ans.: The corresponding base of the bigger triangle is 9 cm.

Q. 46

In $\triangle PQR$, seg PM is a median. Angle bisectors of $\angle PQM$ & $\angle PMR$ intersect side PQ and side PR in

points X and Y respectively. Prove that $XY \parallel QR$.
Complete the proof by filling in the boxes.

SOLUTION:

In $\triangle PQM$ ray MX is bisector of $\angle PMQ$

$$\frac{\boxed{PM}}{\boxed{MQ}} = \frac{\boxed{PX}}{\boxed{XQ}}$$

$$\therefore \frac{2}{3} = \frac{6}{b_2} \quad \dots\dots \text{(I) theorem of angle bisector}$$

In $\triangle PMR$ ray MY is bisector of $\angle PMR$, then

$$\frac{\boxed{PM}}{\boxed{MQ}} = \frac{\boxed{PY}}{\boxed{YR}}$$

$\dots\dots$ (II) theorem of angle bisector

But

$$\frac{MP}{MQ} = \frac{MP}{MR} \quad \dots\dots \text{M is the mid point of QR}$$

Hence $MQ = MR$

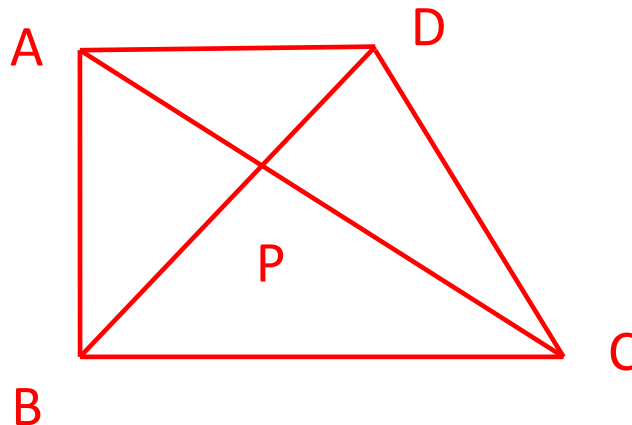
$$\therefore \frac{PX}{XQ} = \frac{PY}{YR}$$

$\therefore XY \parallel QR$ (Converse of basic proportionality theorem)

Ans.: Given in text boxes

Q. 47

In $\square ABCD$ seg $AD \parallel$ seg BC . Diagonal BD intersect each other in point P . Then show that $\frac{AP}{PD} = \frac{PC}{BP}$



SOLUTION:

seg $AD \parallel$ seg BC and line DB is transversal,

$\angle ADP \cong \angle CBP$ (Alternate angle theorem)..... (1)

In $\triangle ADP$ and $\triangle CBP$

$\angle ADP \cong \angle CBP$ {from (1)}

$\angle APD \cong \angle CPB$... (Vertically opposite triangles)

$\therefore \triangle ADP \sim \triangle CBP$ (AA test of similarity)

$\therefore \frac{AP}{CP} = \frac{PD}{BP}$...(Corresponding sides of similar triangles in proportion)

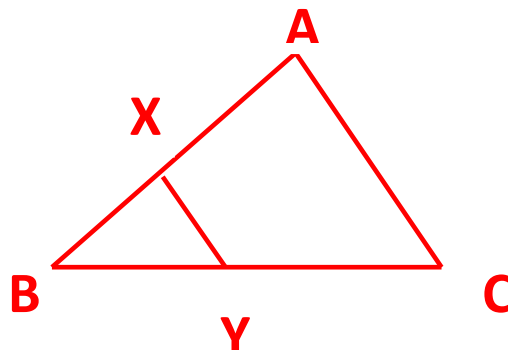
$$\therefore \frac{AP}{PD} = \frac{PC}{BP}$$

$$\text{i.e. } \frac{AP}{PD} = \frac{PC}{BP}$$

$$\text{Ans.: } \frac{AP}{PD} = \frac{PC}{BP} \text{ proved}$$

Q. 48

In figure XY: seg AC. If $2AX = 3BX$ and $XY = 9$, complete the activity to find the value of AC



SOLUTION:**Activity**

$$2AX = 3 BX$$

$$\therefore \frac{AX}{BX} = \frac{\boxed{3}}{\boxed{2}}$$

$$\therefore \frac{AX + BX}{\quad} = \frac{\boxed{3} + \boxed{2}}{\quad} \quad (\text{by componendo})$$

$$\therefore \frac{BX}{AB} = \frac{\boxed{5}}{\boxed{2}}$$

$\triangle BCA \sim \triangle BYX$ {A A test of similarity}

$$\therefore \frac{BA}{BX} = \frac{AC}{XY}$$

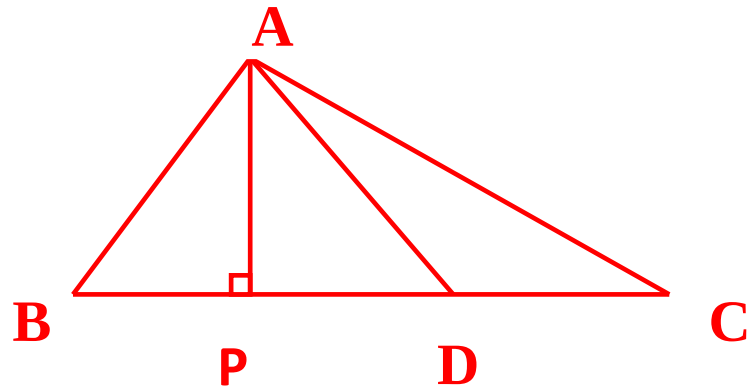
...(Corresponding sides of similar triangle)

$$\therefore \frac{\boxed{5}}{\boxed{2}} = \frac{AC}{9}$$

$$\therefore AC = \boxed{22} \quad \text{..... (From (1))}$$

Q. 49

In $\triangle ABC$ point D on side BC is such that $DC = 6$, $BC = 15$. Find $A(\triangle ABD) : A(\triangle ABC)$ and $A(\triangle ABD) : A(\triangle ADC)$

**SOLUTION:**

Point A is common vertex of $\triangle ABD$, $\triangle ADC$ & $\triangle ABC$ their bases are collinear. Hence, heights of these triangles are equal.

$$BC = 15, DC = 6, \therefore BD = BC - DC = 15 - 6 = 9$$

$$\frac{A(\triangle ABD)}{A(\triangle ABC)} = \frac{BD}{BC} \quad \dots \text{heights equal hence areas}$$

proportional to bases.

$$\frac{A(\triangle ABD)}{A(\triangle ABC)} = \frac{9}{15}$$

$$= \frac{3}{5}$$

$$\frac{A(\triangle ABD)}{A(\triangle ADC)} = \frac{BD}{DC} \dots\dots \text{heights equal hence areas}$$

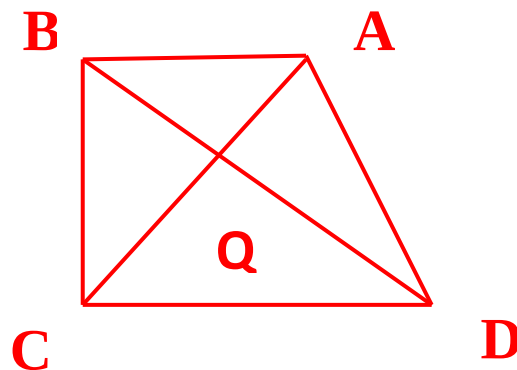
proportional to bases.

$$\frac{A(\triangle ABD)}{A(\triangle ADC)} = \frac{9}{6} = \frac{3}{2}$$

$$\text{Ans: } \frac{A(\triangle ABD)}{A(\triangle ADC)} = \frac{3}{2}$$

Q. 50

Diagonals of quadrilateral ABCD intersect in point Q. If $2QA = QD$, then prove that $DC = 2 AB$. Given $2QA = QC$, $2QB = QD$



SOLUTION:

$$2QA = QC \quad \therefore \frac{QA}{QC} = \frac{1}{2} \quad \dots\dots\dots (1)$$

$$2QB = QD \quad \therefore \frac{QB}{QD} = \frac{1}{2} \quad \dots\dots\dots (2)$$

$$\therefore \frac{QA}{QC} = \frac{QB}{QD} \quad \dots\dots\dots \text{from (1) and (2)}$$

In $\triangle AQB$ & $\triangle CQD$

$$\frac{QA}{QC} = \frac{QB}{QD} \quad \dots\dots\dots \text{proved}$$

$$\frac{XY}{MN} = \frac{14}{21} = \frac{2}{3}$$

$\angle AQB \cong \angle CQD$opposite angles

$\therefore \triangle AQB \sim \triangle CQD$ (SAS test of similarity)

$$\therefore \frac{AQ}{CQ} = \frac{QB}{QD} = \frac{AB}{CD} \quad \dots\dots \dots \text{corresponding side are}$$

proportional

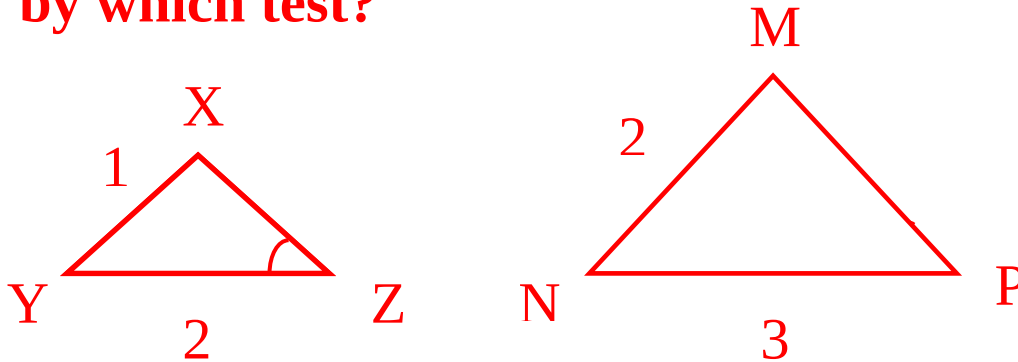
$$\text{But } \frac{AQ}{CQ} = \frac{1}{2} \quad \therefore \frac{AQ}{CQ} = \frac{1}{2}$$

$$\therefore 2AB = CD$$

$2AB = CD$ proved

Q. 51

Can we say that the two triangles in the figures are similar, according to the information given? If yes, by which test?



SOLUTION:

$\triangle XYZ$ & $\triangle MNP$,

$$\frac{XY}{MN} = \frac{14}{21} = \frac{2}{3}$$

$$\frac{YZ}{NP} = \frac{20}{30} = \frac{2}{3}$$

It is given that $\angle Z \cong \angle P$

But $\angle Z$ and $\angle P$ are not included angle by sides which are not in proportion

$\therefore \triangle XYZ$ & $\triangle MNP$ can not be said to be similar

Ans: $\triangle XYZ$ & $\triangle MNP$ can not be said to be similar