

4. Construction of Triangles

Extra Question

Q.1 Construct ΔABC in which $\angle ABC = 72^\circ$, $BC = 6.5\text{cm}$ and $AB + BC = 8\text{ cm}$

Solution: As shown in the rough figure first we draw seg $BC = 6.5\text{ cm}$ of length .on the ray making an angle of 72° With seg BC mark point D such that

$$BD = AB + AC = 8\text{ cm}$$

Now we have to locate point A on ray BD

$$BA + AD = BA + AC = 8\text{ cm}$$

$$AD = AC$$

Point A is on the Perpendicular bisector of seg CD .

The point of intersection of ray BD and the perpendicular

Bisector of seg CD at point A .

Steps of construction:

I) Draw seg BC of length 6.5 cm

II) Draw ray BQ such that $\angle CBQ = 72^\circ$

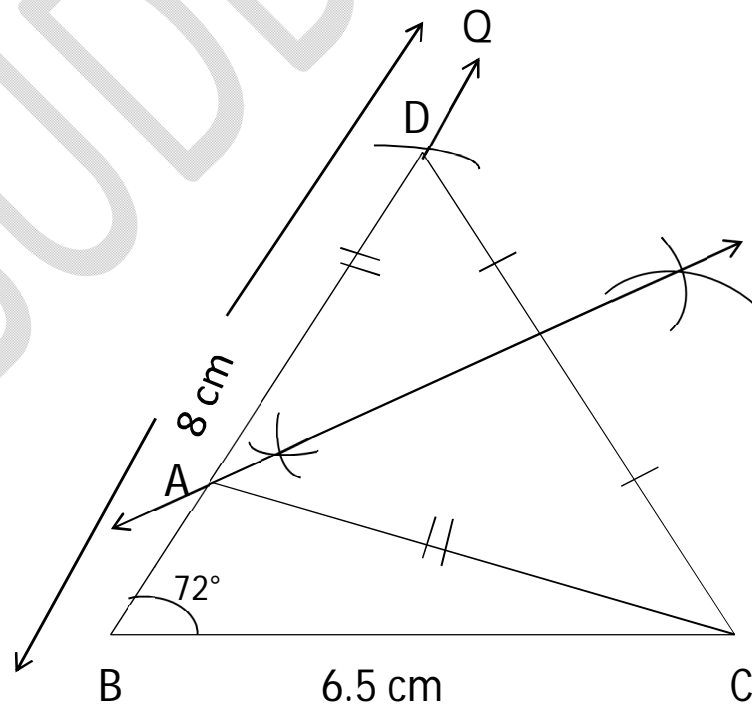
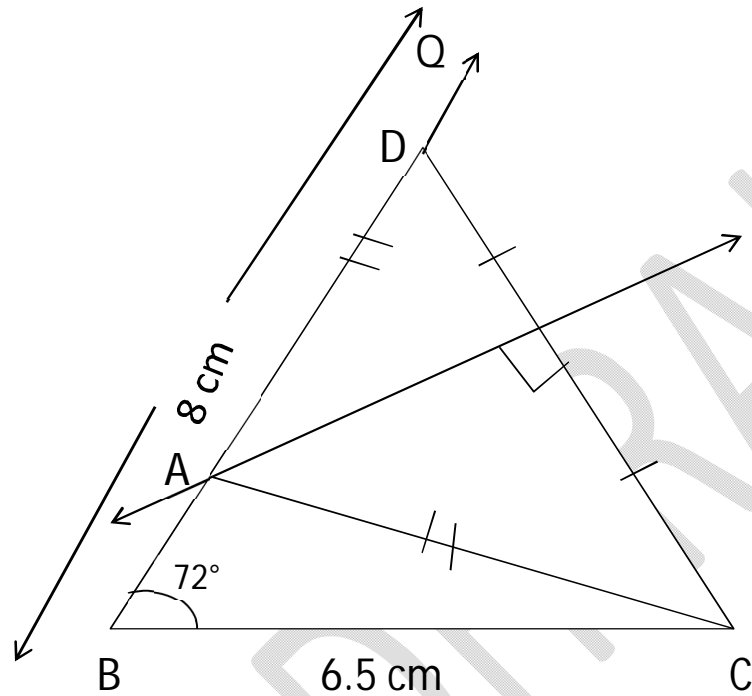
III) Mark point D on ray BQ at 8 cm from point B .

IV) Join points C and D

V) Draw perpendicular bisector of seg CD and let it

intersect ray BQ name the intersection point as Point A
VI) Draw seg AC.

ΔABC is required triangle.



Q.2) Construct ΔPQR , $PQ = 3.9 \text{ cm}$, $QR + PR = 7.9 \text{ cm}$ $\angle P = 67^\circ$

Solution: As shown in the rough figure, first we draw seg $PQ = 3.9 \text{ cm}$ of length on the ray making an angle of 67°

With seg PQ mark point B such that

$$PB = PR + RQ = 7.9 \text{ cm}$$

Now we have to locate point R on ray PB

$$PR + RB = PR + RQ = 7.9 \text{ cm}$$

$$RB = RQ$$

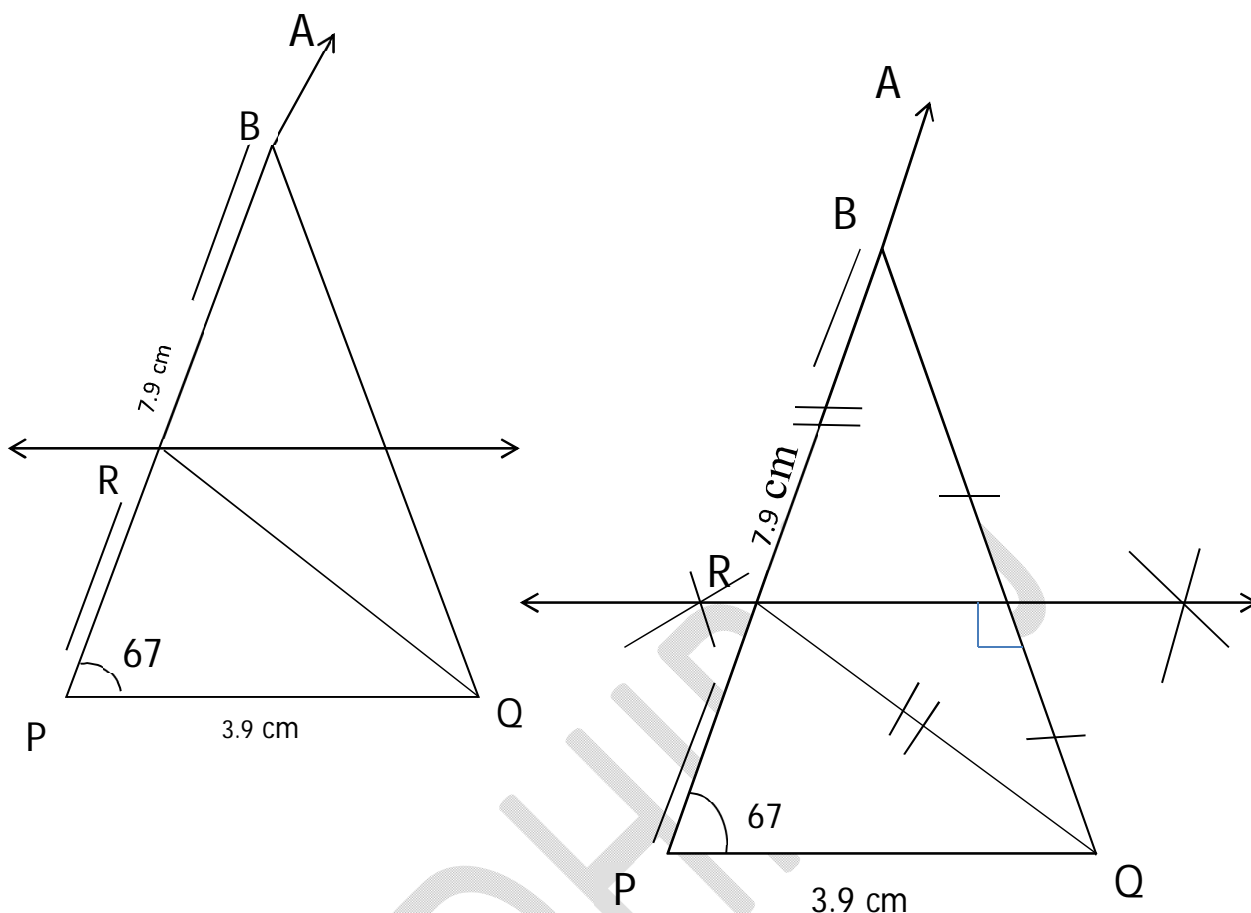
\therefore Point R is on the perpendicular bisector of seg BQ

\therefore The point of intersection of ray PB and the perpendicular bisector of seg BQ at Point R .

Steps of construction:

- i) Draw seg PQ of length 3.9 cm
- ii) Draw ray PA such that $\angle QPA = 67^\circ$
- iii) Mark point P on ray PA at 7.9 cm from point B .
- iv) Join point Q and D .
- v) Draw perpendicular bisector of seg BQ and let it intersect ray PB . Name the intersection point as point R .
- vi) Draw seg RQ

ΔPQR is required triangle.



Q. 3) Construct $\triangle ABC$ $BC = 6$ cm $\angle ABC = 70^\circ$, and

$$AB + BC = 10.5 \text{ cm}$$

Solution: As shown in the rough figure, first we draw seg $BC = 6$ cm of length. on the ray making an angle of 70°

With seg BC , mark point M such that

$$BM = AB + AC = 10.5 \text{ cm}$$

Now we have to locate point A on ray BM

$$BA + AM = BA + AC = 10.5 \text{ cm}$$

$$AM = AC$$

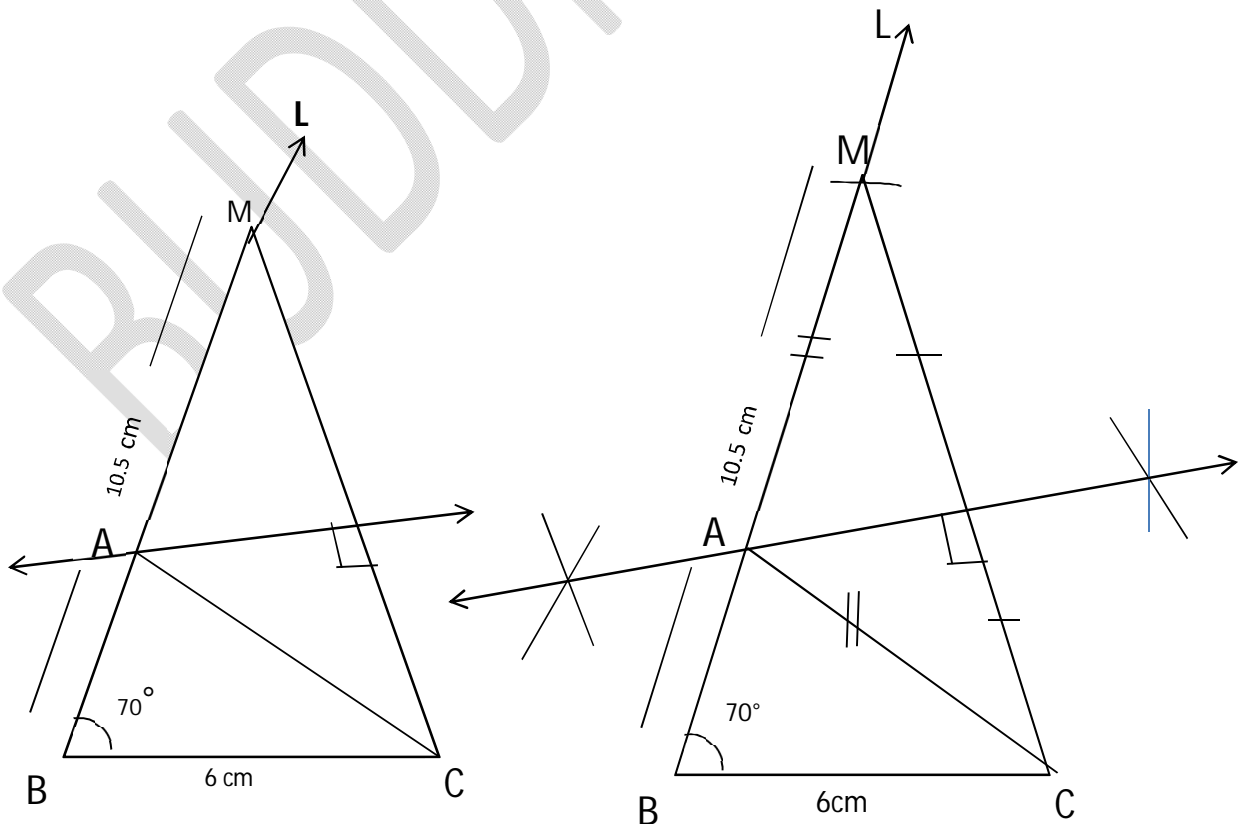
Point A is on the perpendicular bisector of seg QB .

The point of intersection of ray BM and the
Perpendicular bisector of seg AM is point A.

Steps of construction:

- I) Draw seg BC of length 6 cm
- II) Draw ray BL such that $\angle ABC = 70^\circ$
- III) Mark point M on ray BL at 10.5 cm from point B.
- IV) Join points C and M
- V) Draw perpendicular bisector of seg CM and let it intersect ray BM . name the intersection point as Point A
- VI) Draw seg AC.

ΔABC is a required triangle



Q.4) Construct ΔBAD $AD = 5.7\text{cm}$, $\angle BAD = 120^\circ$, and
 $AB = 4.5\text{ cm}$

Solution: As shown in the rough figure ,first we draw seg $AD = 5.7\text{ cm}$ of length . on the ray making an angle of 120°

With seg AD , mark point B such that

$$AF = EA + ED = 4.5\text{ cm}$$

Now we have to locate point B on ray AF

$$AE + EB = EA + ED = 4.5\text{ cm}$$

$$EB = ED$$

Point B is on the perpendicular bisector of seg DB .

The point of intersection of ray AB and the

Perpendicular bisector of seg DB is point E

Steps of construction:

I) Draw seg AD of length 4.5 cm

II) Draw ray AF such that $\angle BAD = 120^\circ$

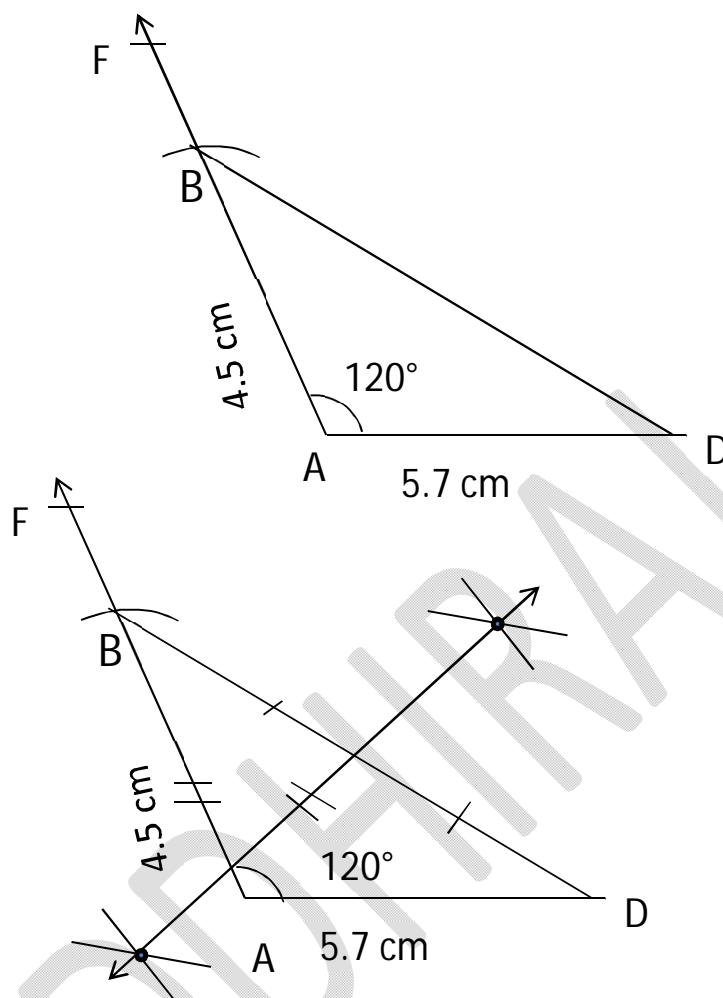
III) Mark point A on ray AF at 4.5 cm from point B .

IV) Join points D and B

V) Draw perpendicular bisector of seg BD and let it intersect ray AF . name the intersection point as Point E

VI) Draw seg ED .

ΔBAD is a required triangle



Q.5) Construct ΔGMB $MB = 4.6\text{cm}$, $GM + BG = 8.2\text{ cm}$

And $\angle m = 45^\circ$

Solution: As shown in the rough figure ,first we draw seg $MB = 4.6\text{ cm}$ of length . on the ray making an angle of 45°

With seg MB , mark point G such that

$$MG = MC + CB = 8.2\text{ cm}$$

Now we have to locate point C on ray MG

$$MC + CG = MC + CB = 8.2\text{ cm}$$

$$CG = CB$$

Point C is on the perpendicular bisector of seg BG.

The point of intersection of ray MG and the

Perpendicular bisector of seg BG is point C

Steps of construction:

I) Draw seg MB of length 4.6 cm

II) Draw ray MD such that $\angle m = 45^\circ$

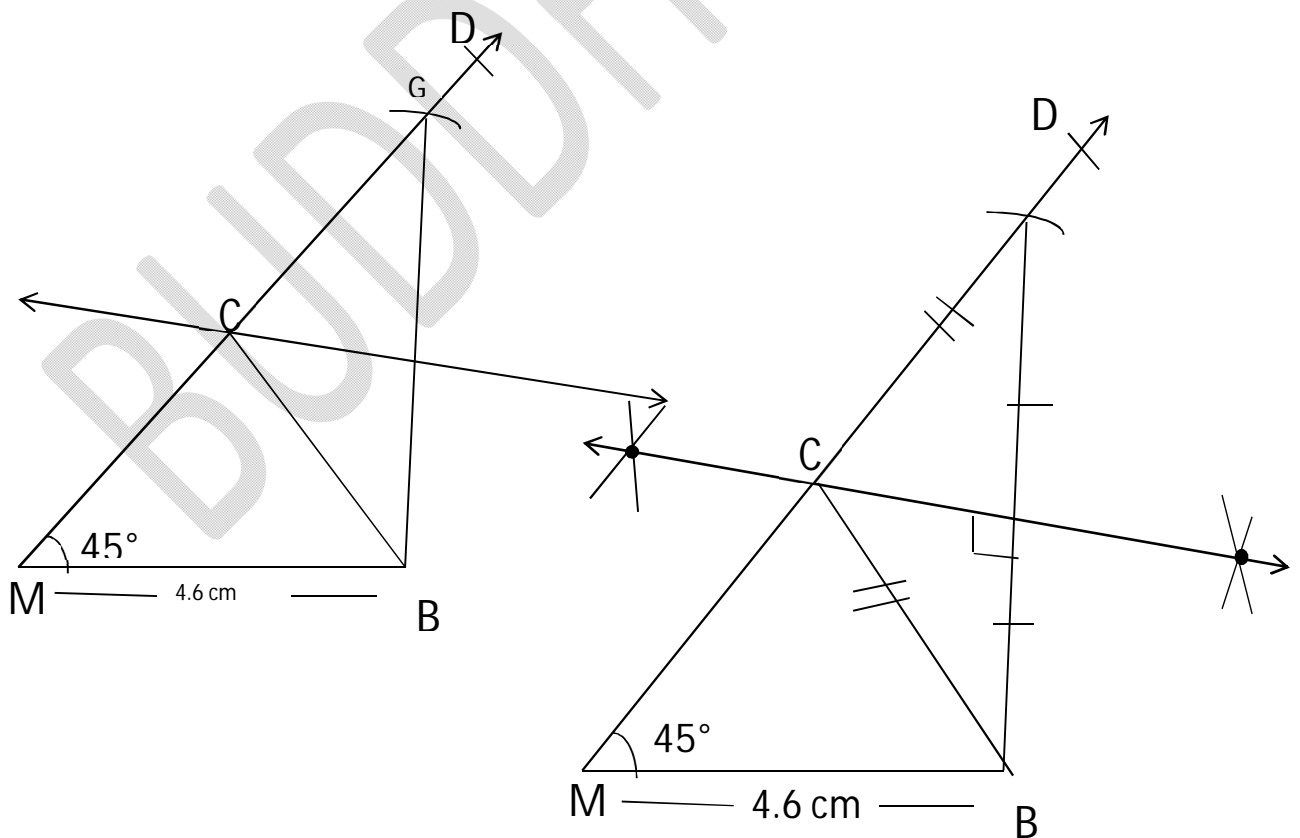
III) Mark point M on ray GM at 8.2 cm from point C.

IV) Join points B and G

V) Draw perpendicular bisector of seg BG and let it

intersect ray MD . name the intersection point as Point C

VI) Draw seg CB. ΔGMB is a required triangle



Q.6) Construct ΔABC in which $BC = 3.2$ cm, $\angle ACB = 45^\circ$ and perimeter of ΔABC is 12 cm

Solution: Perimeter of $\Delta ABC = AB + BC + AC$

$$12 = AB + 3.2 + AC$$

$$\therefore AB + AC = 12 - 3.2$$

$$\therefore AB + AC = 9.8$$

In ΔABC

$$BC = 3.2 \text{ cm}, \angle ACB = 45^\circ \quad AB + AC = 9.8$$

As shown in the rough figure, first we draw seg $CB = 3.2$ cm of length. on the ray making an angle of 45°

With seg CB , mark point D such that

$$BD = AC + AB = 9.8 \text{ cm}$$

Now we have to locate point A on ray BD

$$CA + CD = CA + CB = 9.8 \text{ cm}$$

$$CD = CB$$

Point A is on the perpendicular bisector of seg BD .

The point of intersection of ray CD and the

Perpendicular bisector of seg BD is point A

Steps of construction:

I) Draw seg BC of length 3.2 cm

II) Draw ray CT such that $\angle BCT = 45^\circ$

III) Mark point D on ray CT such that $l(C, D) = 6.8 \text{ cm}$

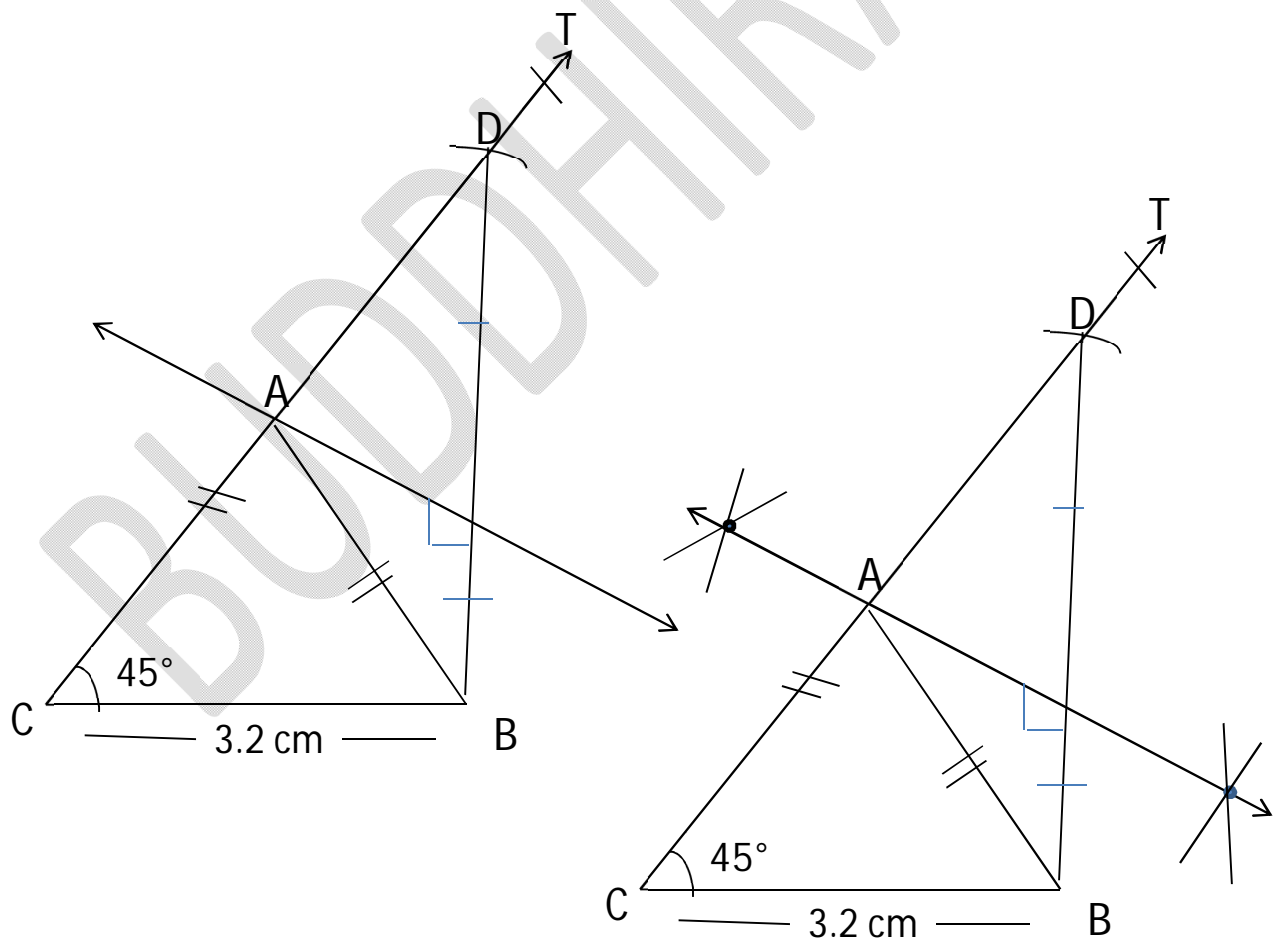
IV) Join points D and B

V) Draw perpendicular bisector of seg DB

Intersecting ray CT .Name the point as A.

VI) Join the point A and B

Hence ΔABC is a required triangle



Q. 7) Construct ΔLMN , $MN = 4.2$ cm, $\angle m = 78^\circ$, and
 $\angle M + \angle N = 8.5$ cm

Solution: As shown in the rough figure ,first we draw seg MN
 $= 4.2$ cm of length .on the ray making an angle of
 78°

With seg MN , mark point K such that

$$MK = LM + LN = 8.5 \text{ cm}$$

Now we have to locate point L on ray MK

$$ML + LK = ML + LN = 8.5 \text{ cm}$$

$$LK = LN$$

Point L is on the perpendicular bisector of seg MK .

The point of intersection of ray MK and the

Perpendicular bisector of seg NK is point L .

In given $MN = 4.2$ cm, $\angle m = 78^\circ$

Take Point K on ray MS such that

$$MK = LM + LK = 8.5 \text{ cm} \quad \text{----- i)}$$

By theorem of perpendicular bisector of segmet,

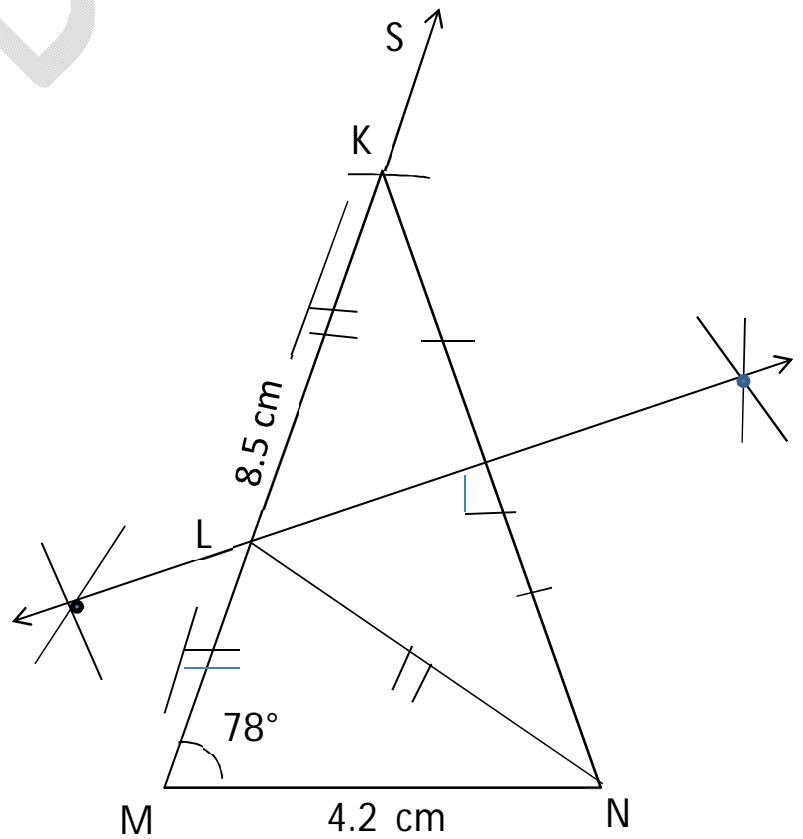
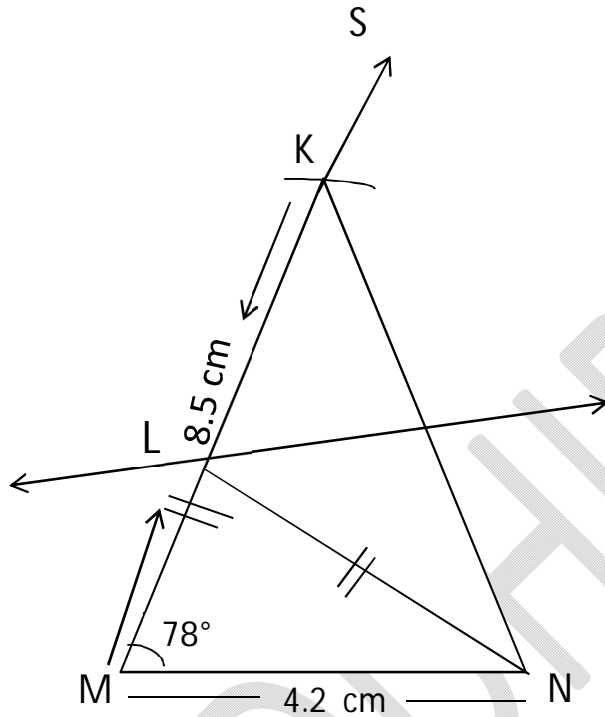
point L lies on perpendicular bisector of seg KN .

$$\therefore KL = LN \quad \text{----- II)}$$

$$LM + LK = 8.5 \text{ cm} \quad \text{From I)}$$

$$LM + LN = 8.5 \text{ cm} \quad \text{from II)}$$

$\triangle LMN$ is required triangle.



Q.8) Construct ΔABC , $AC = 4.8$ cm, $\angle A = 70^\circ$, and

$$AB + BC = 7 \text{ cm.}$$

Solution: As shown in the rough figure ,first we draw seg $AC = 4.8$ cm of length .on the ray making an angle of 70°

With seg AC , mark point D such that

$$AQ = BA + BC = 7 \text{ cm}$$

Now we have to locate point B on ray AQ

$$AB + BQ = AB + BC = 7 \text{ cm}$$

$$BQ = BC$$

Point B is on the perpendicular bisector of seg CQ .

The point B of intersection of ray and the

Perpendicular bisector of seg CQ is point B

$$\text{Given } AC = 4.8 \text{ cm}, \angle A = 70^\circ$$

Take point Q on ray AP such that

$$AQ = BA + BQ = 7 \text{ cm} \text{ ----- (I)}$$

By theorem of perpendicular bisector of segment point A lies on perpendicular bisector of seg QC .

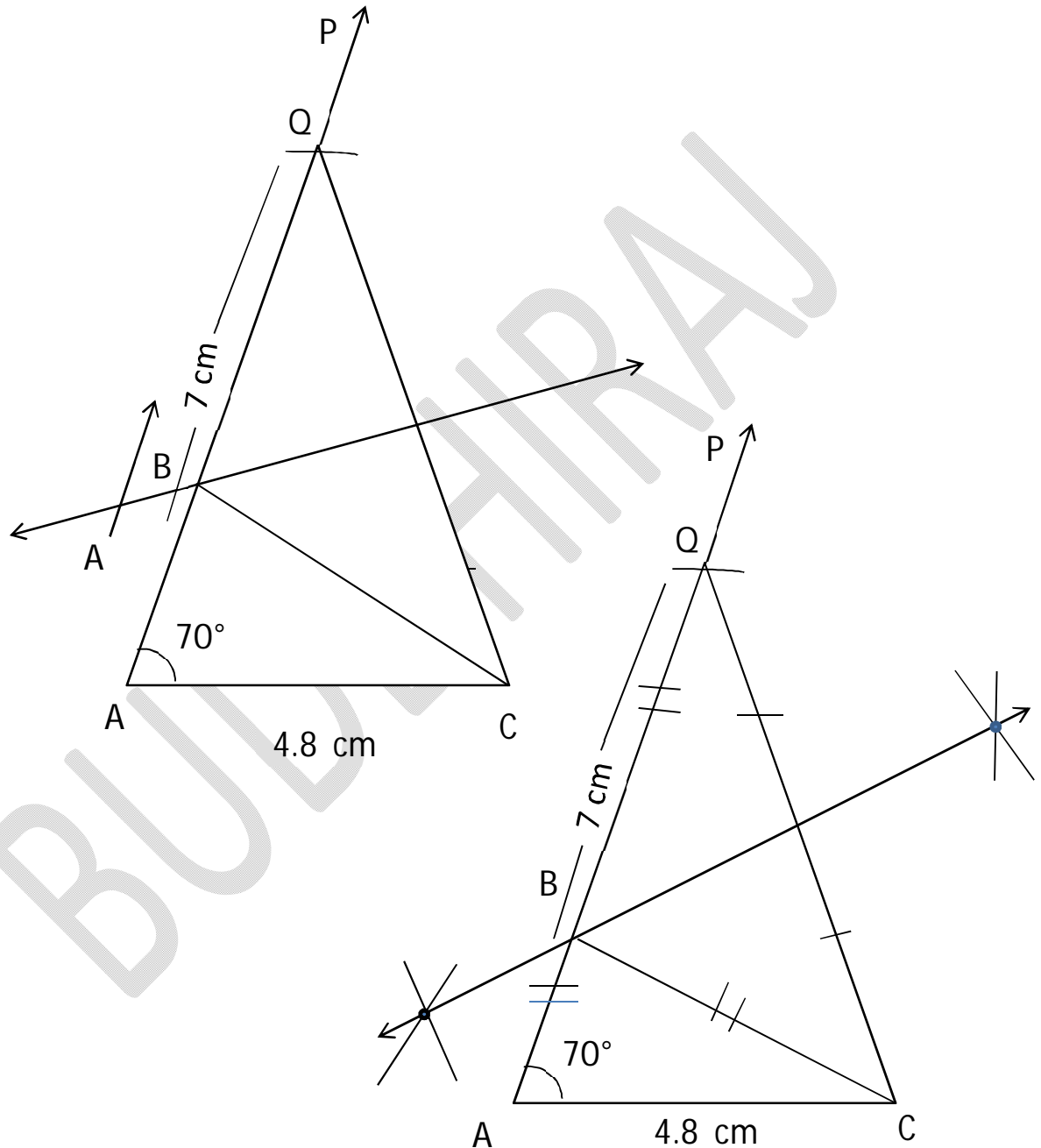
$$\therefore BQ = BC \text{ ----- (II)}$$

$$\text{Now } AQ = 7 \text{ cm}$$

$$BA + BQ = 7 \text{ cm} \quad \text{----- (from I)}$$

$$BA + BC = 7 \text{ cm} \quad \text{----- (from II)}$$

$\therefore \Delta ABC$ is required triangle.



Q.9) Construct ΔPQR , $QR = 6.3 \text{ cm}$, $\angle Q = 75^\circ$, and $PQ + PR = 9 \text{ cm}$.

Solution: As shown in the rough figure ,first we draw seg QR
 = 6.3 cm of length .on the ray making an angle of
 75° With seg QR, mark point B such that

$$QB = PQ + PR = 9 \text{ cm}$$

Now we have to locate point P on ray QB

$$QP + PB = QP + PR = 9 \text{ cm}$$

$$PB = PR$$

Point P is on the perpendicular bisector of seg RB.

The point of intersection of ray QB and the
 Perpendicular bisector of seg RB is point P

$$\text{Given } QR = 6.3 \text{ cm}, \angle Q = 75^\circ$$

Take point B on ray QA such that

$$QB = PQ + PB = 9 \text{ cm} \text{ ----- (I)}$$

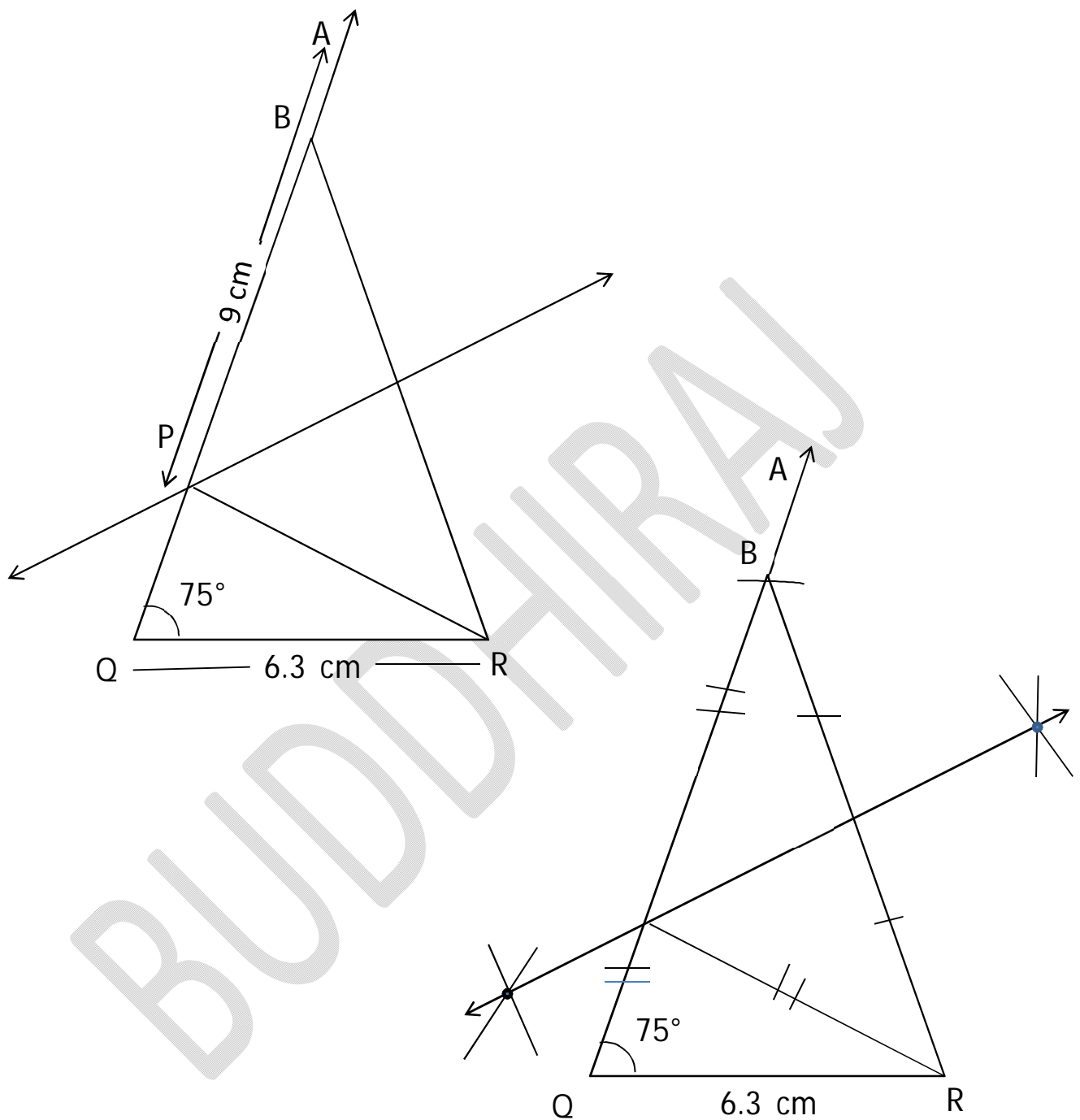
By theorem of perpendicular bisector of segment point P lies
 on perpendicular bisector of seg BR.

$$\therefore PB = BR \text{ ----- (II)}$$

$$PQ + PB = 9 \text{ cm} \text{ ----- (from I)}$$

$$PQ + PR = 9 \text{ cm} \text{ ----- (from II)}$$

ΔPQR is required triangle.



Q.10) Construct $\triangle DEF$, $EF = 4.8$ cm, $\angle E = 50^\circ$, and
 $DE + DF = 8.3$ cm.

Solution: As shown in the rough figure, first we draw seg EF
 $= 4.8$ cm of length. on the ray making an angle of

50° With seg EF, mark point B such that

$$EB = DE + EF = 8.3 \text{ cm}$$

Now we have to locate point D on ray EB

$$ED + DB = ED + DF = 8.3 \text{ cm}$$

$$DB = DF$$

Point D is on the perpendicular bisector of seg FB.

The point of intersection of ray EB and the

Perpendicular bisector of seg FB is point D

$$\text{Given } EF = 4.8 \text{ cm}, \angle E = 50^\circ$$

Take point B on ray EA such that

$$EB = DE + DB = 8.3 \text{ cm} \text{ ----- (I)}$$

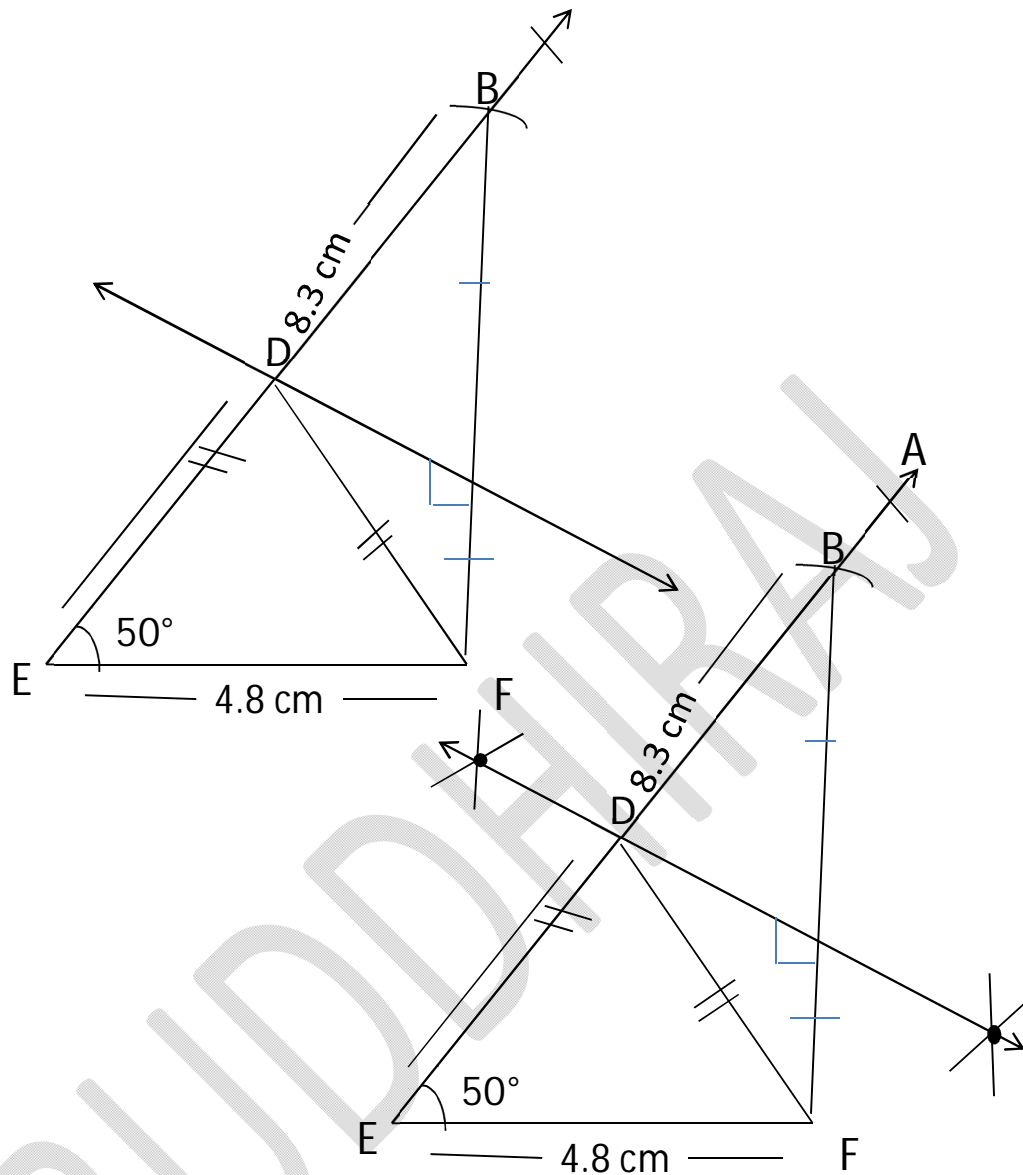
By theorem of perpendicular bisector of segment point D lies on perpendicular bisector of seg DB.

$$\therefore DB = DF \text{ ----- (II)}$$

$$DE + DB = 9 \text{ cm} \text{ ----- (from I)}$$

$$DE + DF = 9 \text{ cm} \text{ ----- (from II)}$$

$\therefore \triangle DEF$ is required triangle



Q.11) Construct ΔLMN , $MN = 8.5$ cm, $\angle LMN = 40^\circ$, and $LM - LN = 3$ cm. construct ΔLMN .

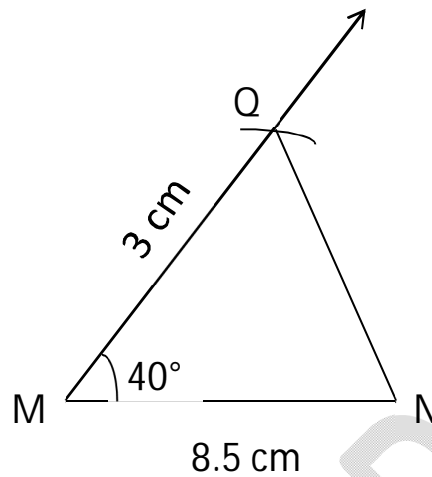
Solution: $LM - LN = 3$ cm

$LM > LN$.

First draw seg MN of 8.5 cm

We can draw ray MP such that $\angle NMP = 40^\circ$ take

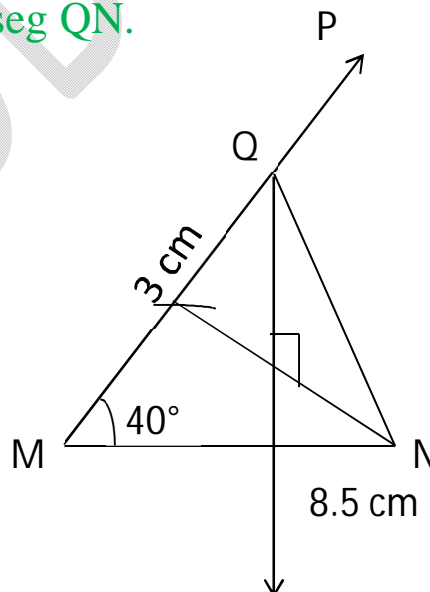
Point Q on ray MP such that $MQ = 3$ cm join Q and N



Now, $LM - LN = 3$ cm

Point L is on the perpendicular bisector of seg QN.

Point L is the point of intersection of ray MP and the perpendicular bisector of seg QN.



$\angle Q = \angle N$ ----- (I)

Now, $MQ = 3$ cm

$$LM - LQ = 3 \text{ cm}$$

$$LM - LN = 3 \text{ cm} \quad \text{----- (from I)}$$

$\triangle LMN$ is required triangle. $MN = 8.5 \text{ cm}$

$$\angle LMN = 40^\circ \text{ and } LM - LN = 3 \text{ cm}$$

Steps of construction:

I) Draw seg MN of length 8.5 cm

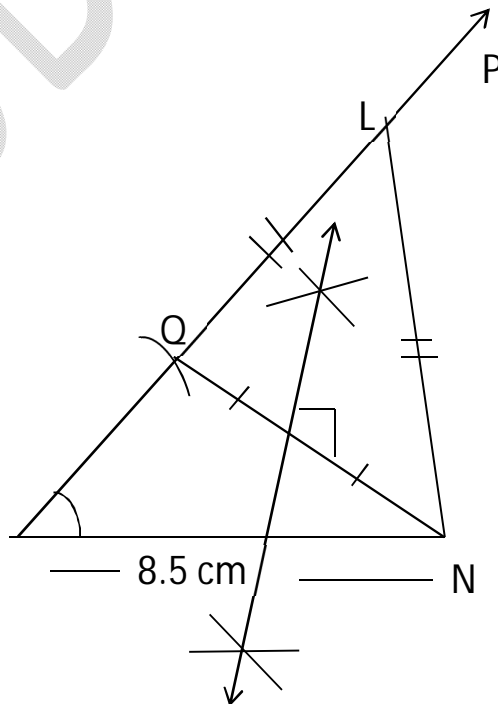
II) Draw ray MP such that $\angle PMN = 40^\circ$

III) Draw an arc on ray MP of radius 3 cm and name it as Point Q

IV) Draw QN

V) Draw perpendicular bisector of NQ name the Point L where it intersects ray MP

VI) Join LN .



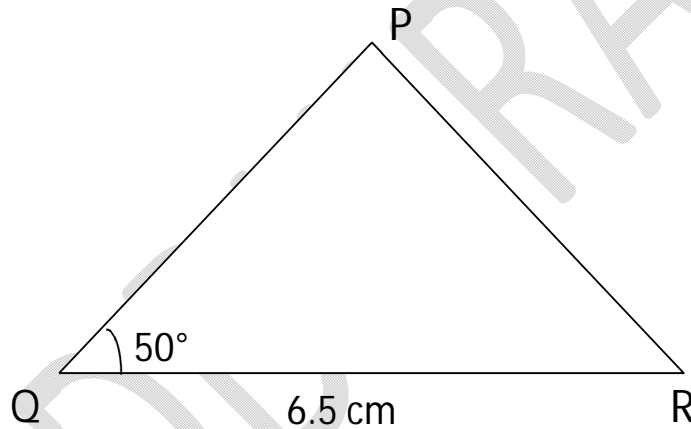
Q.12) Construct ΔPQR , $QR = 6.5$ cm, $\angle Q = 50^\circ$, and $PQ - PR = 3$ cm.

Solution: $PQ - PR = 3$ cm

$PQ > PR$

First draw seg QR of 6.5 cm

We can draw ray QT such that $\angle TQR = 50^\circ$



Point T is on ray RQ . Take point D on opposite ray of Ray QT such that

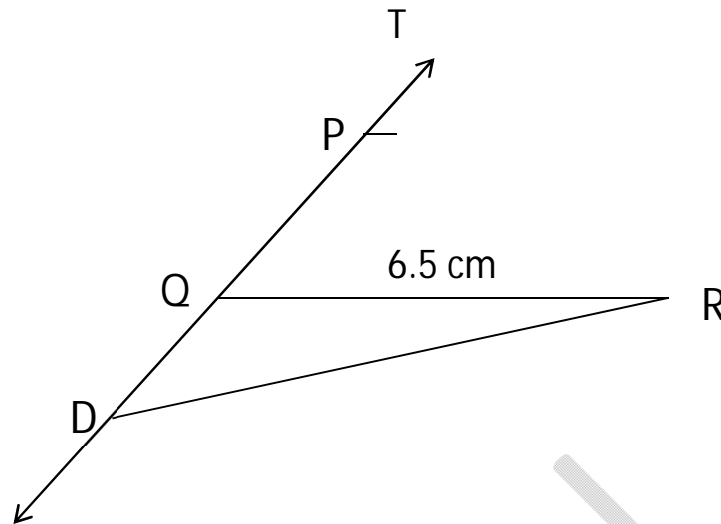
$QD = 3$ cm

Now, $PD = PQ + QD = PQ + 3 = PR$

($\therefore PQ - PR = 3$ cm)

$\therefore PD = PR$

\therefore Point P is on the perpendicular bisector of seg RD .



Steps of construction:

I) Draw seg QR of length 6.5 cm

II) Draw ray QT such that $\angle Q = 50^\circ$

III) Take Point D on the opposite ray QS of ray QT

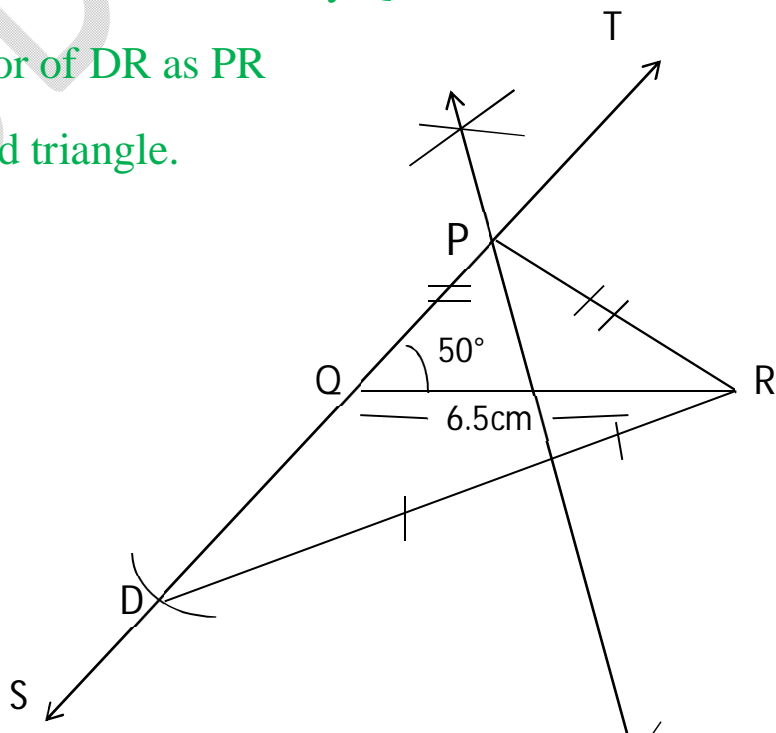
Such that $QD = 3$ cm

IV) Construct perpendicular bisector of seg DR

V) Name the point of intersection of ray QT and the

Perpendicular bisector of DR as PR

ΔPQR is the required triangle.



Q.13) Construct ΔPQR , $QR = 6 \text{ cm}$, $\angle Q = 40^\circ$, and

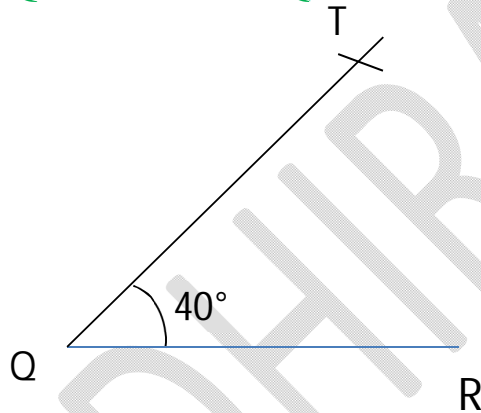
$$PR - PQ = 2 \text{ cm}.$$

Solution : $PR - PQ = 2 \text{ cm}$.

$$PR > RQ$$

First draw seg. QR of 6 cm

We can draw ray QT such that $\angle Q = 40^\circ$



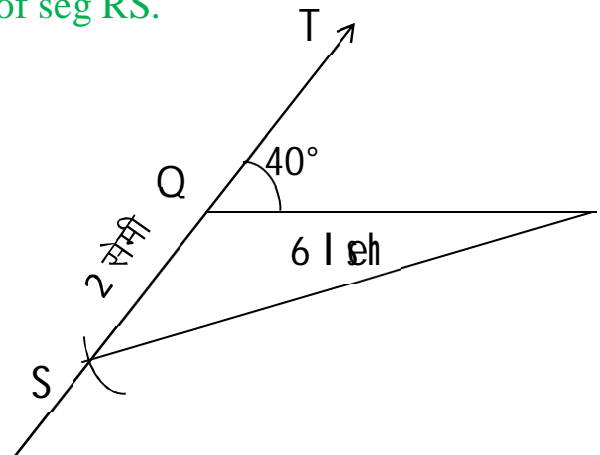
Point P is on ray QT Take point S on opposite ray of ray QT such that.

$$QS = 2 \text{ cm}$$

$$\text{Now, } PS = PQ + QD = PQ + 2 = PR$$

$$(\because PR - PQ = 2 \text{ cm}) \therefore PS = PR$$

Point P is on the perpendicular bisector of seg RS .



Steps of construction:

I) Draw QR of length 6 cm

II) Draw ray QT such that $\angle RQT = 40^\circ$

III) Take point Q on the opposite ray QX of ray QT

Such that QS = 2 cm

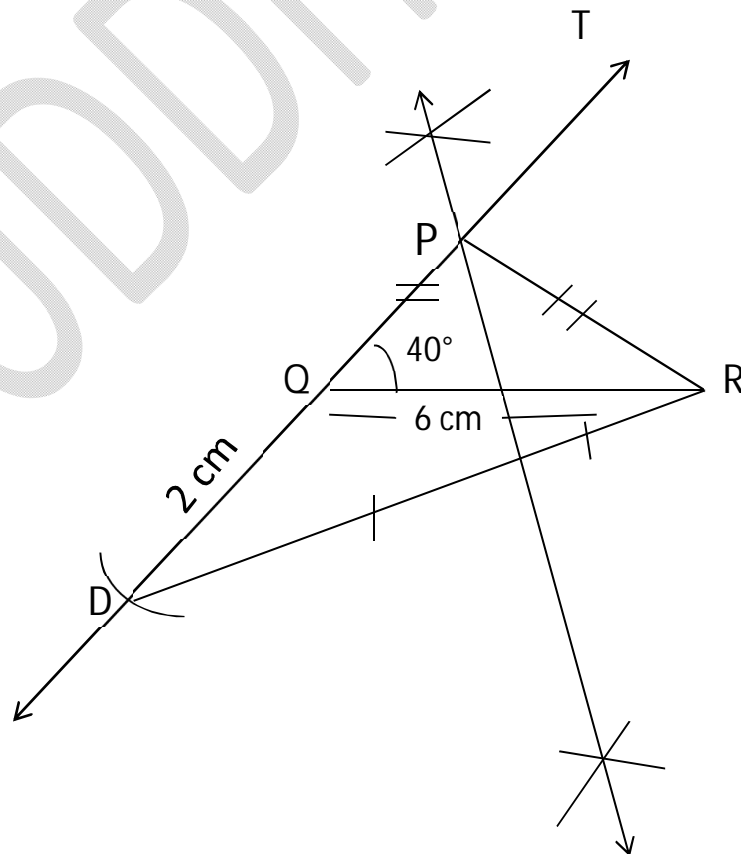
IV) construct perpendicular bisector of seg QR

V) Name the point of intersection of ray QT and

Perpendicular bisector of SR as P

V) Draw seg PR.

ΔPQR is required triangle.



Q.14) Construct ΔABC , $BC = 6.5\text{ cm}$, $\angle ABC = 45^\circ$, and
 $AC - AB = 2.5\text{ cm}$.

Solution : $BC = 6.5\text{ cm}$, $AC - AB = 2.5\text{ cm}$.

$$AC > AB$$

First we draw the length of seg 6.5 cm and

$$\angle ABC = 45^\circ$$

Draw opposite ray of ray BX , take point y and

$BY = 2.5\text{ cm}$ join point y and c .

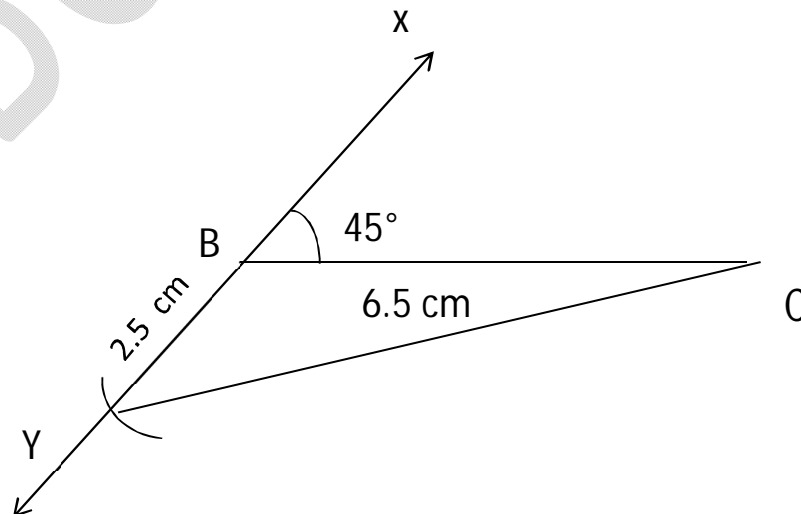
Now, Point A is on the perpendicular bisector of seg AC

\therefore Point A is the point of intersection of ray BX and the
 Perpendicular bisector of seg AC .

$$AY = AC \text{ ----- (I)}$$

$$\text{Now, } AY - AB = 2.5\text{ cm}$$

$$AC - AB = 2.5\text{ cm} \quad (\text{From I})$$



Steps of construction:

I) Draw BC of length 6.5 cm

II) Draw ray BX, $\angle CBX = 45^\circ$

III) Draw BY of opposite ray of ray BX.

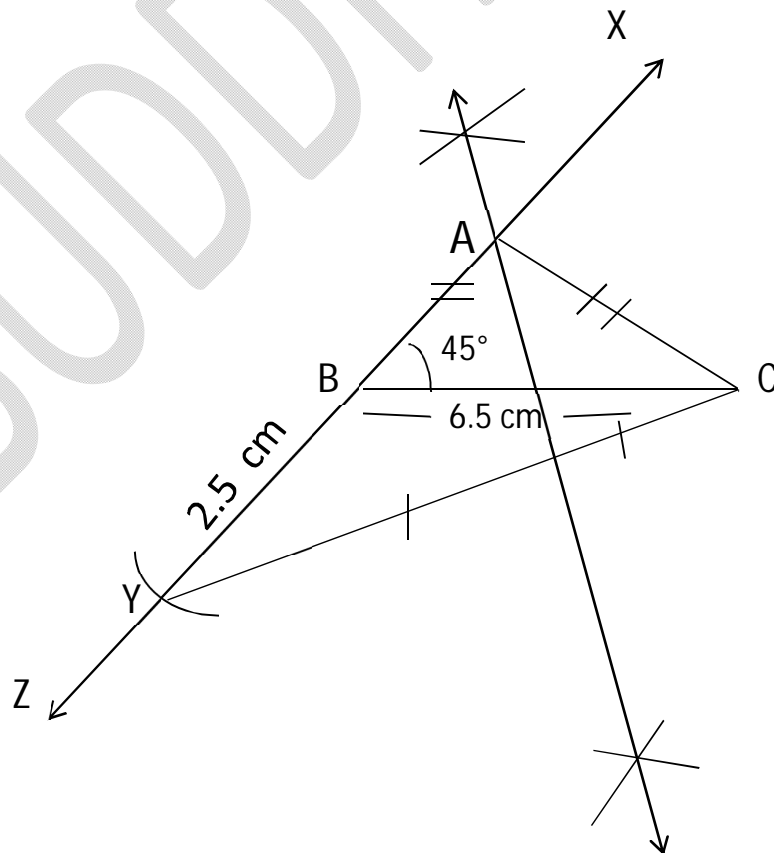
Such that BY = 2.5 cm

IV) Construct perpendicular bisector of seg YC.

V) Name the point of intersection of ray BX and the Perpendicular bisector of YC as A

VI) Join point A and C

ΔABC is the required triangle.



Q.15) Construct ΔRST , $ST = 7.2$ cm, $\angle RST = 85^\circ$, and
 $RS - RT = 3.5$ cm.

Solution : $ST = 7.2$ cm, $RS - RT = 3.5$ cm. $RS > RT$

First we draw the length of seg 7.2 cm and
 $\angle RST = 85^\circ$

Draw opposite ray of ray SA, take point B and

$SB = 3.5$ cm join point y and T.

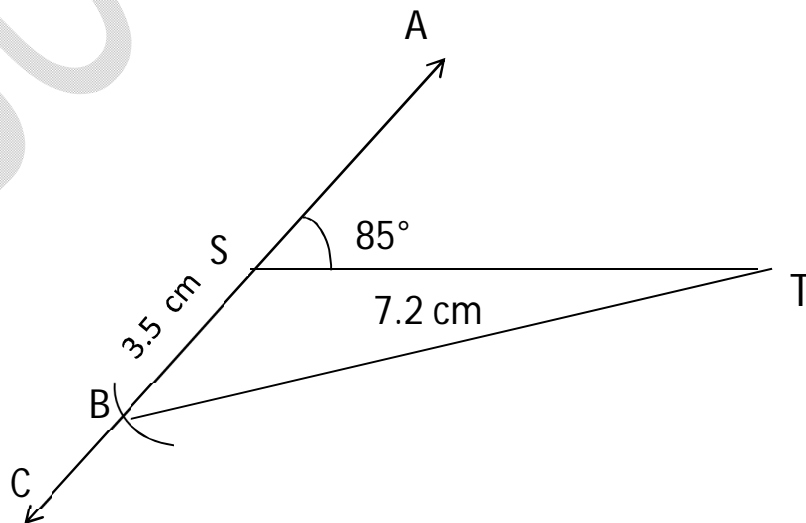
Now, Point R is on the perpendicular bisector of seg RT

\therefore Point A is the point of intersection of ray SA and the
 Perpendicular bisector of seg RT

$RB = RT$ ----- (I)

Now, $RB - RS = 3.5$ cm

$RT - RS = 3.5$ cm (From I)



Steps of construction:

I) Draw ST of length 7.2 cm

II) Draw ray ST, $\angle S = 85^\circ$

III) Draw SC of opposite ray of ray SA.

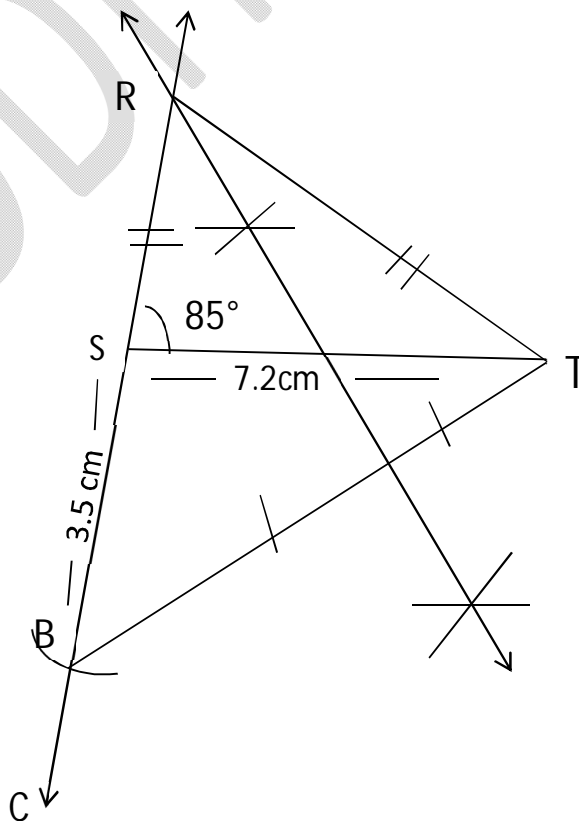
Such that SB = 3.5 cm

IV) Construct perpendicular bisector of seg BT.

V) Name the point of intersection of ray SA and the Perpendicular bisector of BT as R

VI) Draw seg RT

ΔRST is the required triangle.



Q.16) Construct ΔKSL , $SL = 6 \text{ cm}$, $\angle S = 55^\circ$, and

$$KL - KS = 2.2 \text{ cm.}$$

Solution : $SL = 6 \text{ cm}$, $KL - KS = 2.2 \text{ cm}$. $KL > KS$

First we draw the length of seg SL 6 cm and

$$\angle S = 55^\circ$$

Draw opposite ray of ray SP , take point Q and

$SQ = 2.2 \text{ cm}$ join point Q and L .

Now, Point K is on the perpendicular bisector of seg KL

\therefore Point K is the point of intersection of ray SP and the

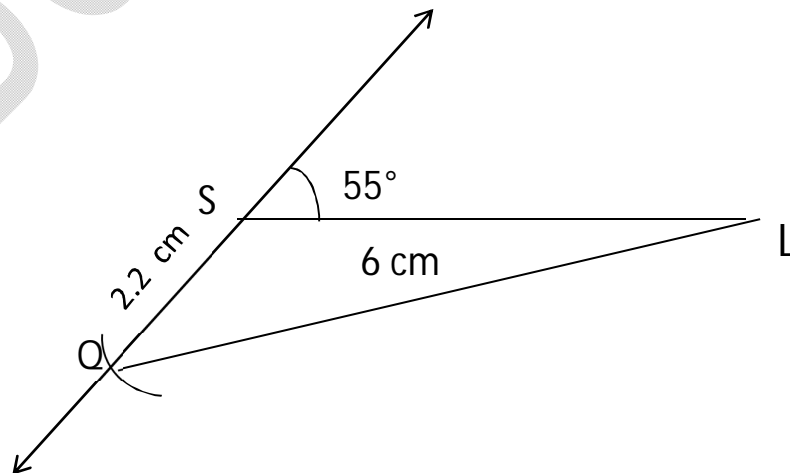
Perpendicular bisector of seg KL

$$KS = KL \text{ ----- (I)}$$

Now, $SQ = 2.2 \text{ cm}$

$$KQ - KS = 2.2 \text{ cm}$$

$$KL - KS = 2.2 \text{ cm} \quad (\text{From I})$$



Steps of construction:

I) Draw SL of length 6 cm

II) Draw ray SP, $\angle S = 55^\circ$

III) Draw SR of opposite ray of ray SP.

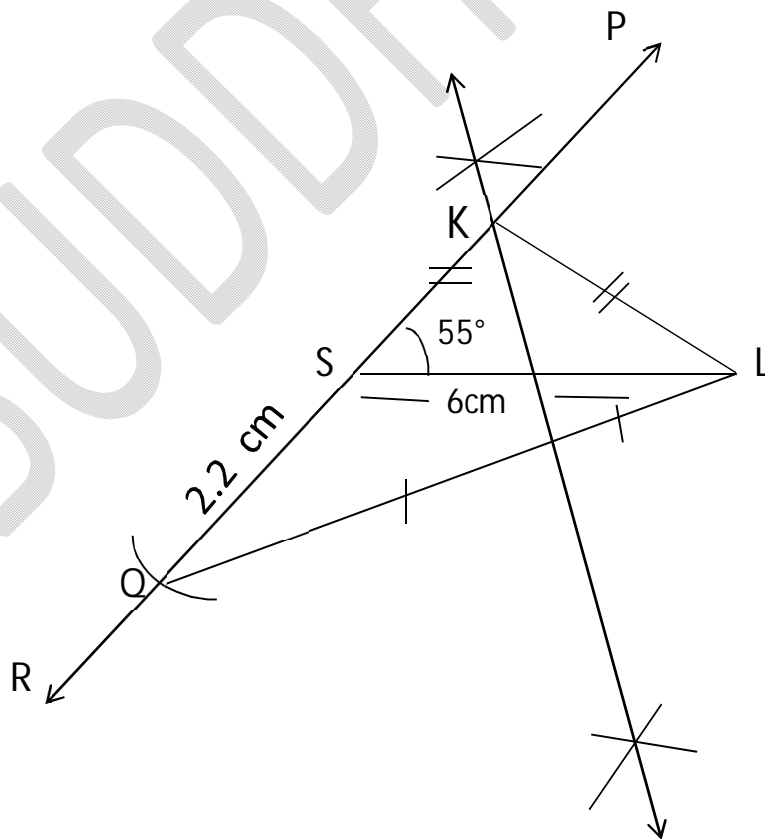
Such that SQ = 2.2 cm

IV) Construct perpendicular bisector of seg QL.

V) Name the point of intersection of ray SP and the Perpendicular bisector of QL as K

VI) Draw seg KL

ΔKSL is the required triangle



Q.17) Construct ΔRMN , $RM = 6 \text{ cm}$, $\angle NRM = 70^\circ$, and
 $RN - MN = 2.8 \text{ cm}$.

Solution : $RM = 6 \text{ cm}$, $RN - MN = 2.8 \text{ cm}$. $RN > MN$

First we draw the length of seg $RM = 6 \text{ cm}$ and
 $\angle R = 70^\circ$

Draw opposite ray of ray RA , take point B and

$RB = 2.8 \text{ cm}$ join point B and M .

Now, Point N is on the perpendicular bisector of seg BM

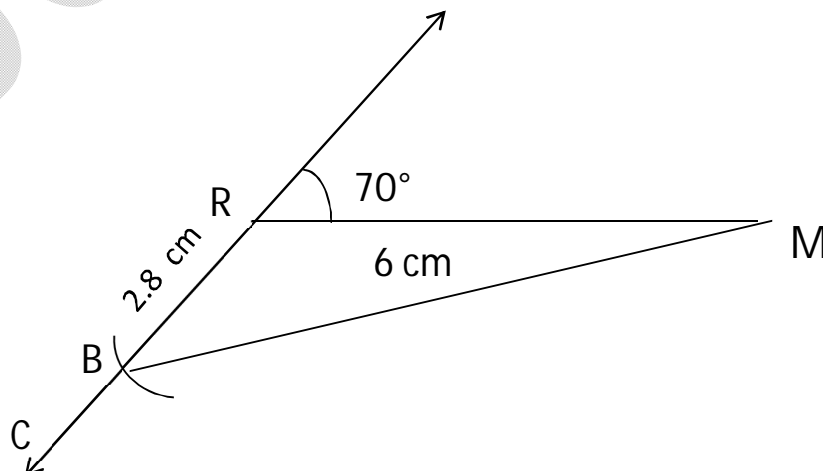
\therefore Point R is the point of intersection of ray RA and the
 Perpendicular bisector of seg BM .

$$NB = NM \text{ ----- (I)}$$

$$\text{Now, } RB = 2.8 \text{ cm}$$

$$NB - NR = 2.8 \text{ cm}$$

$$NM - NR = 2.8 \text{ cm} \quad (\text{From I})$$



Steps of construction:

I) Draw RM of length 6 cm

II) Draw ray RA ,such that $\angle NRM = 70^\circ$

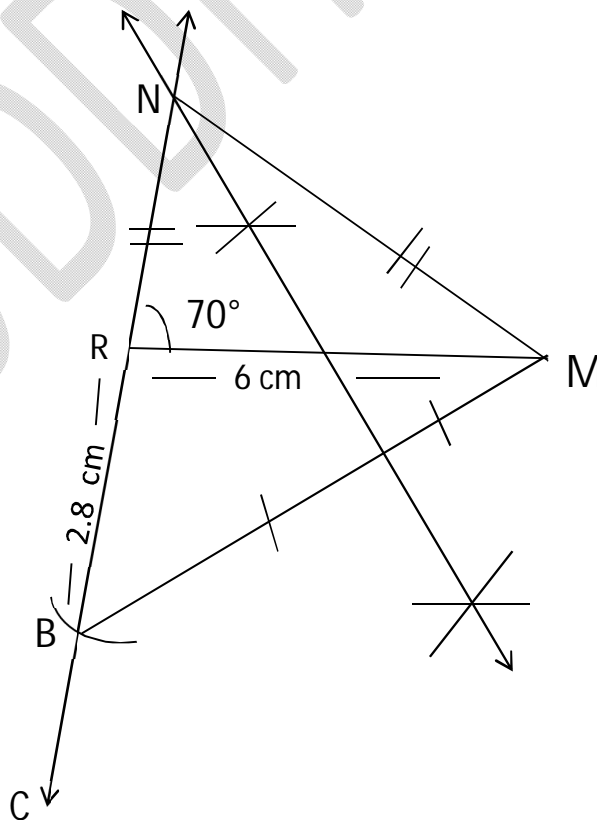
III) Take point RC on the opposite ray RA if ray such
That $RB = 2.8$ cm

IV) Construct perpendicular bisector of seg BM.

V) Name the point of intersection of ray RA and the
Perpendicular bisector of BM as N

VI) Draw seg NM

ΔRMN is the required triangle



Q.18) Construct ΔPQR , $QR = 5.5$ cm, and $\angle ACB = 48^\circ$, and
Perimeter of triangle is 12 cm.

Solution: $QR = 5.5$ cm

Perimeter of $\Delta PQR = 12$ cm

$$PQ + QR + PR = 12$$

$$PQ + PR = 12 - 5.5 \text{ cm}$$

$$PQ + PR = 6.5 \text{ cm}$$

Sum of any two sides of a triangle must be greater than its third side.

$\therefore \Delta PQR$ with this measurement is not possible.

Q.19) Construct ΔABC , $AB = 5.8$ cm, $\angle BAC = 105^\circ$, and
 $AC - BC = 2.9$ cm.

Solution : $AB = 5.8$ cm, $AC - BC = 2.9$ cm. $AC > BC$

First we draw the length of seg $AB = 6$ cm and
 $\angle BAC = 105^\circ$

Draw opposite ray of ray AT , take point S and

$AS = 2.9$ cm join point S and B .

Now, Point C is on the perpendicular bisector of seg CB

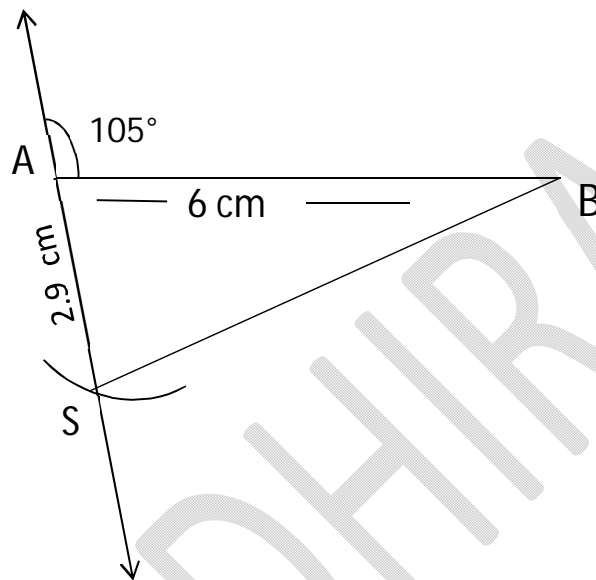
\therefore Point A is the point of intersection of ray AT and the
Perpendicular bisector of seg CB .

$$CS = CB \text{ ----- (I)}$$

$$\text{Now, } AS = 2.9 \text{ cm}$$

$$CS - CA = 2.9 \text{ cm}$$

$$CB - CA = 2.9 \text{ cm} \quad (\text{From I})$$



Steps of construction:

I) Draw AB of length 5.8 cm

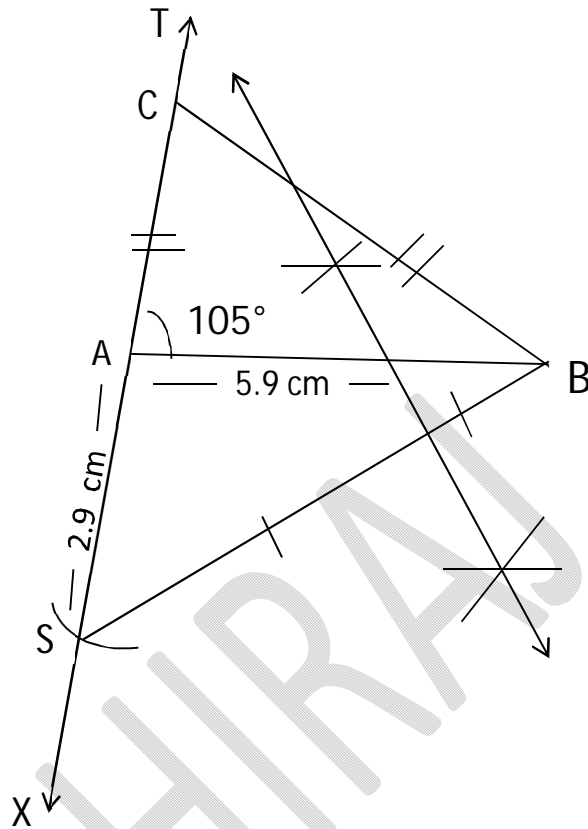
II) Draw ray RA ,such that $\angle BAC = 105^\circ$

III) Take point AX on the opposite ray AT of ray such
That SA= 2.9 cm

IV) Construct perpendicular bisector of seg SB.

V) Name the point of intersection of ray AT and the
Perpendicular bisector of SB as C

VI) Draw seg CB



Q.20) Construct ΔPQR , $\angle Q = 70^\circ$, $\angle R = 50^\circ$, and
 $PQ + QR + RP = 10 \text{ cm}$.

Solution: In this construction. Instead of length of each side
 Perimeter of the triangle is given.

First draw ST having length equal to perimeter of
 ΔPQR

Points Q and R must be on seg ST such that $S-Q-R-T$

To locate point P , we have to draw ΔPQS

Such that $PR = RT$

$PR = RT$, point R must be perpendicular bisector of
Seg PT

Similarly, $PR = RT$, point R must be perpendicular
bisector of seg PT.

$\angle PQR$ is an exterior angle ΔPQS and $\angle PRQ$ is an
Exterior angle of ΔPRT .

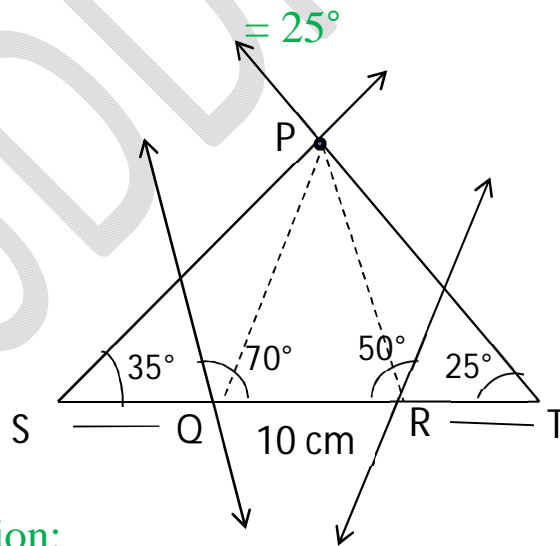
\therefore By theorem of remote interior angle of a triangle.

$$\angle PQR = 2 \angle S \quad \text{and} \quad \angle PRQ = 2 \angle T$$

$$\therefore \angle S = \frac{1}{2} \angle PQR \quad \therefore \angle T = \frac{1}{2} \angle PRQ$$

$$\therefore \angle S = \frac{1}{2} \times 70^\circ \quad \therefore \angle T = \frac{1}{2} \times 50^\circ$$

$$= 35^\circ \quad = 25^\circ$$



Steps of construction:

I) Draw seg ST of 10 cm

II) Draw a ray making an angle of 35° at point S

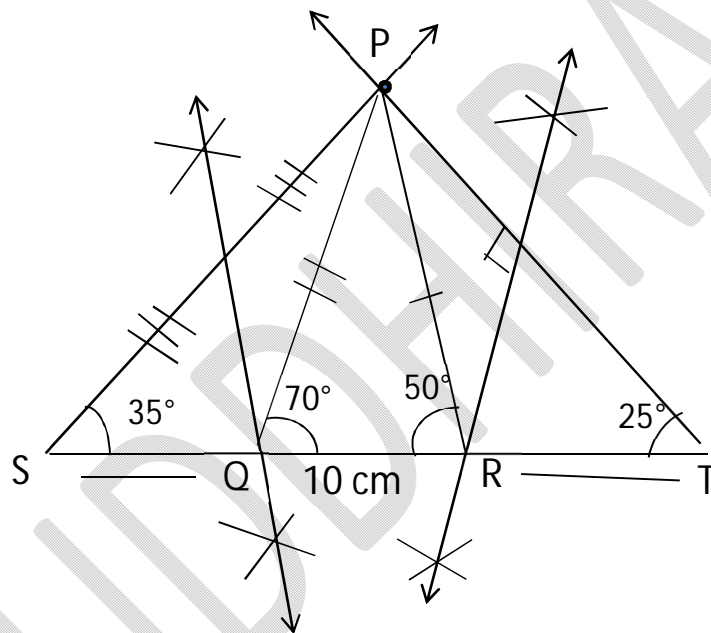
III) Draw a ray making an angle of 25° at point T

IV) Name the point of intersection of the two rays As P.

V) Draw the perpendicular bisectors of seg PS and Seg PT. Name the points as Q and R respectively, where the perpendicular bisector intersect line ST

VI) Draw seg PQ and seg PR

ΔPQR is the required triangle.



Q.21) Construct ΔABC , $\angle B = 70^\circ$, $\angle C = 50^\circ$, and

$$AB + BC + AC = 11.3 \text{ cm.}$$

Solution: In this construction, instead length of each side,

Perimeter of the triangle is given.

First draw seg XY having length equal to

Perimeter of ΔABC

Points B and C must be on seg XY such that X-B-C-Y

To locate point A, we have to draw ΔABX such that

$AB = BX$ and $\angle AXT$ such that $AC = CT$

Similarly, for $AB = BX$ and point B must be on

Perpendicular of seg AX

$\angle ABC$ is an exterior angle of ΔAYB and $\angle ACB$ is an

Exterior angle of ΔACT

\therefore By theorem of remote interior angle of a triangle.

$$\angle ABC = 2 \angle X \quad \text{and} \quad \angle ACB = 2 \angle Y$$

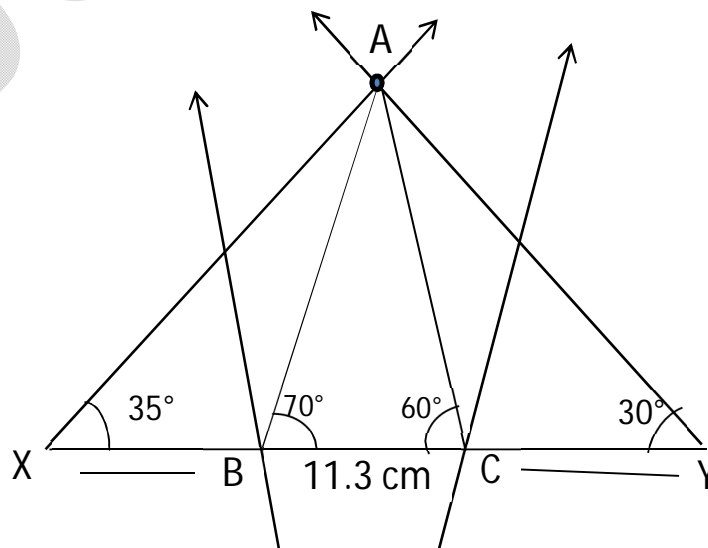
$$\therefore \angle X = \frac{1}{2} \angle ABC \quad \therefore \angle Y = \frac{1}{2} \angle ACB$$

$$\therefore \angle X = \frac{1}{2} \times 70^\circ \quad \therefore \angle Y = \frac{1}{2} \times 60^\circ$$

$$\angle X = 35^\circ \quad \therefore \angle Y = 30^\circ$$

We can construct ΔAXY such $XY = 11.3$ cm

$$\angle X = 35^\circ \quad \angle Y = 30^\circ$$



Q.22) Construct ΔLMN , $\angle M = 80^\circ$, $\angle N = 48^\circ$, and
 $LM + MN + NL = 9 \text{ cm}$.

Solution: In this construction, instead length of each side,
 Perimeter of the triangle is given.

First draw seg AB having length equal to

Perimeter of ΔLMN

Points M and N must be on seg AB such that A-M-N-B

To locate point L, we have to draw ΔLMA such that

$LA = LB$ and $\angle ALB$ such that $LN = NB$

$LM = MA$ and point M must be on perpendicular
 bisector of seg LB

Similarly

$\angle LMN$ is an exterior angle of ΔLMA and $\angle LNM$ is an

Exterior angle of ΔLNB

\therefore By theorem of remote interior angle of a triangle.

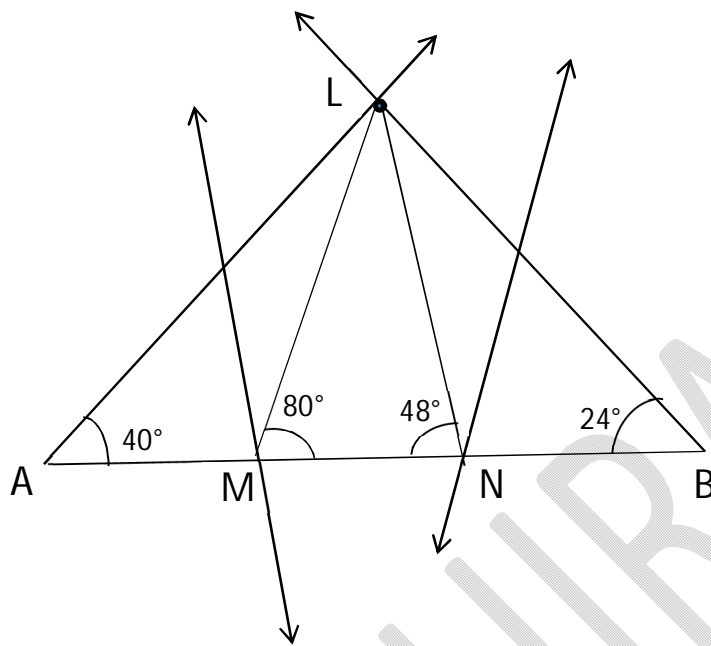
$$\angle LMN = 2 \angle A \quad \text{and} \quad \angle LNM = 2 \angle B$$

$$\therefore \angle A = \frac{1}{2} \angle LMN \therefore \angle B = \frac{1}{2} \angle LNM$$

$$\therefore \angle A = \frac{1}{2} \times 80^\circ \quad \therefore \angle B = \frac{1}{2} \times 48^\circ$$

$$\angle A = 40^\circ \quad \therefore \angle B = 24^\circ$$

We can construct ΔLAB such $\angle A = 40^\circ$ $\angle B = 24^\circ$



Steps of construction:

I) Draw seg AB of 9 cm

II) Draw a ray making an angle of A at 40°

III) Draw a ray making an angle of B at 24°

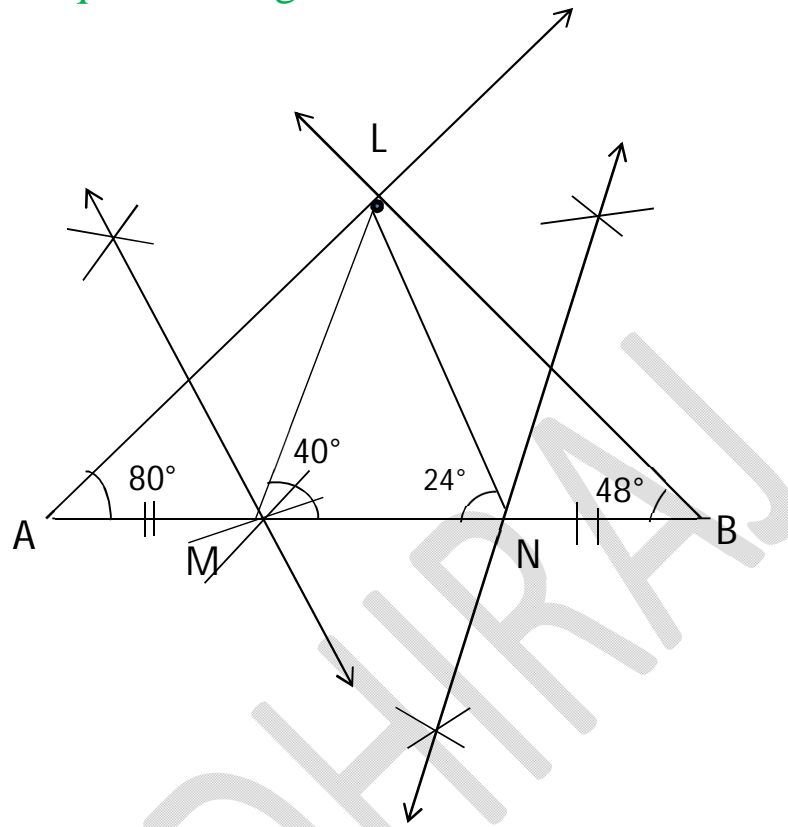
IV) Name the point of intersection of the two rays

As AL and BL

V) Draw the perpendicular bisectors of seg LA and Seg LB. Name the points as M and N respectively, where the perpendicular bisector intersect line

VI) Draw seg LM and seg LN

ΔLMN is the required triangle.



Q.23) Construct ΔABC , $\angle B = 70^\circ$, $\angle C = 50^\circ$, and

Perimeter of triangle is 12 cm

Solution: First draw seg DE is 12 cm

$\angle B = 70^\circ$, and $\angle C = 50^\circ$,

$\angle ABC$ is an exterior angle of ΔADB and

$\angle ACB$ is an exterior angle of ΔACE

\therefore By theorem of remote interior angle of triangle

$$\angle ABC = 2 \angle D \quad \text{and} \quad \angle ACB = 2 \angle E$$

$$\therefore \angle D = \frac{1}{2} \angle ABC \quad \therefore \angle E = \frac{1}{2} \angle ACB$$

$$\therefore \angle D = \frac{1}{2} \times 70^\circ$$

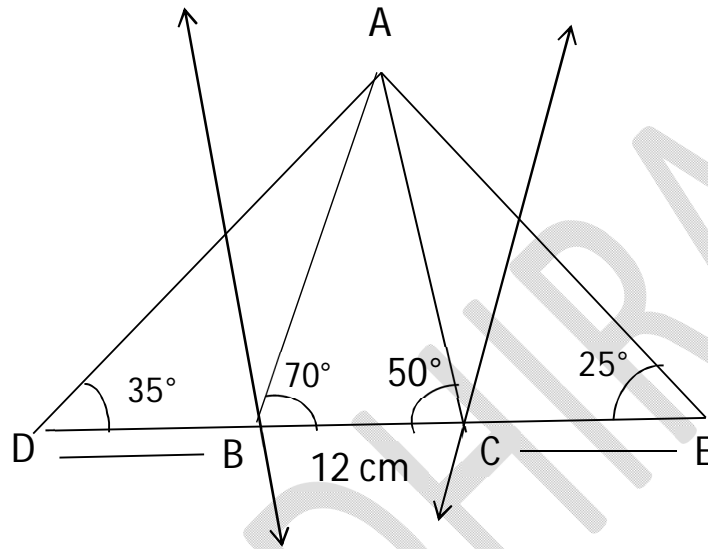
$$\therefore \angle E = \frac{1}{2} \times 50^\circ$$

$$\angle D = 35^\circ$$

$$\therefore \angle E = 25^\circ$$

We can construct ΔADE such that $DE = 12$ cm

$$\angle D = 35^\circ, \quad \angle E = 25^\circ$$



Steps of construction:

I) Draw seg AB of 12 cm

II) Draw a ray making an angle of 35° at point D

III) Draw a ray making an angle of 25° at point E

IV) Name the point of intersection of the two rays

As A

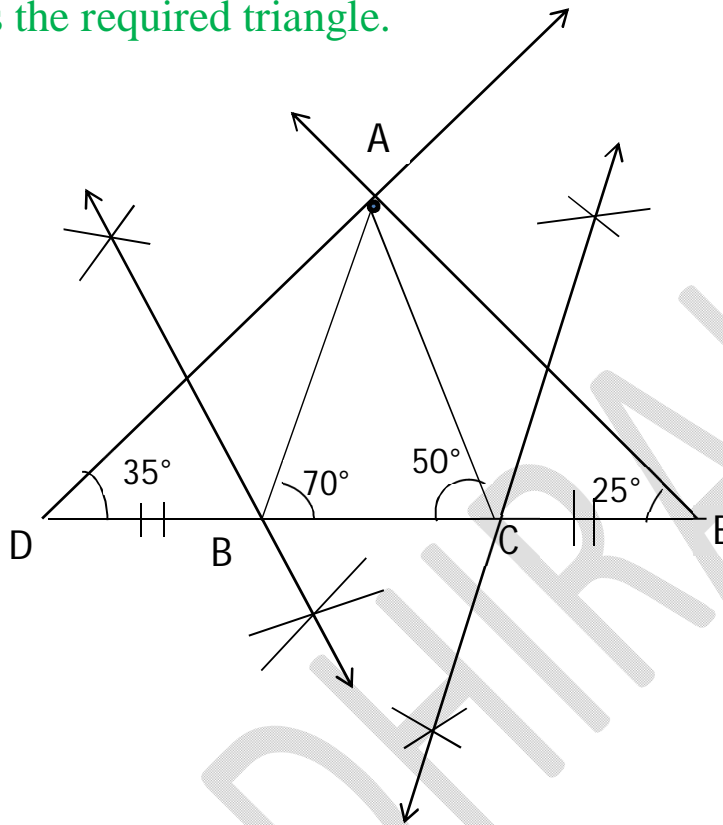
V) Draw the perpendicular bisectors of seg AD and

Seg AE. Name the points as B and C respectively,

where the perpendicular bisector intersect line DE

VI) Draw seg AB and seg DE

ΔABC is the required triangle.



Q.24) Construct ΔLMN , base of each angle is 80° then

Perimeter of triangle is 11 cm.

Solution: First draw seg PQ is 11 cm

Base of each angle = MN is 80°

Means $M = 40^\circ$ and $N = 40^\circ$

$\angle LMN$ is an exterior angle of ΔLPM and

$\angle LNM$ is an exterior angle of ΔLNQ

\therefore By theorem of remote interior angle of triangle

$\angle LMN = 2 \angle P$ and $\angle LNM = 2 \angle Q$

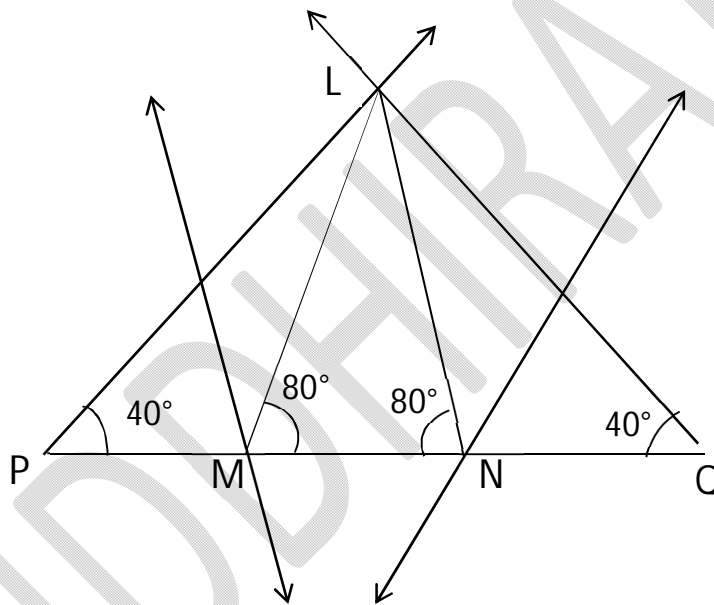
$$\therefore \angle P = \frac{1}{2} \angle LMN \quad \therefore \angle Q = \frac{1}{2} \angle LNM$$

$$\therefore \angle P = \frac{1}{2} \times 80^\circ \quad \therefore \angle Q = \frac{1}{2} \times 80^\circ$$

$$\angle P = 40^\circ \quad \therefore \angle Q = 40^\circ$$

We can construct ΔLPQ such that $PQ = 11\text{cm}$

$$\angle M = 40^\circ, \quad \angle N = 40^\circ$$



Steps of construction:

I) Draw seg PQ of 11 cm

II) Draw a ray making an angle of 40° at point P

III) Draw a ray making an angle of 40° at point Q

IV) Name the point of intersection of the two rays

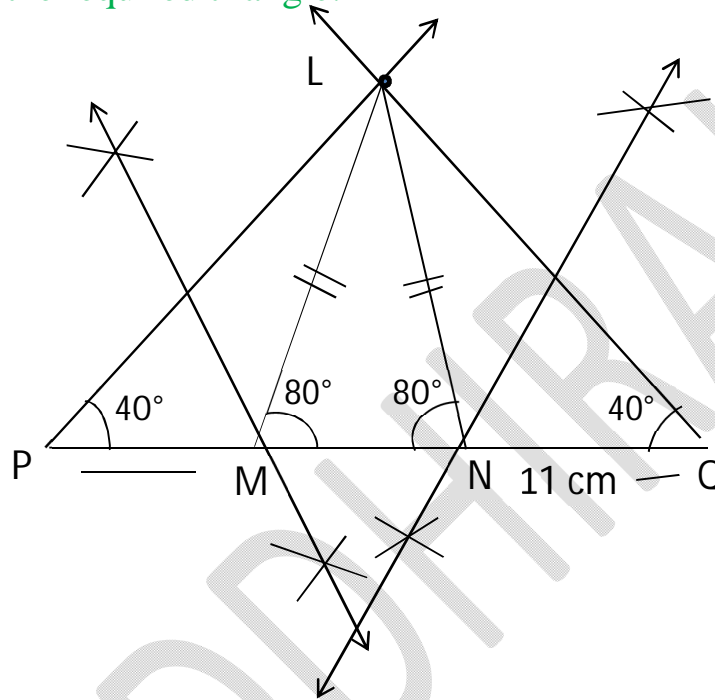
As L

V) Draw the perpendicular bisectors of seg LP and

Seg LQ. Name the points as M and N respectively,
where the perpendicular bisector intersect line PQ.

VI) Draw seg LM and seg LN

ΔLMN is the required triangle.



Q.25) The perimeter of triangle 18 cm and the ratio of
Length of its sides 3:4 :5 . construct the triangle.

Solution: Let the perimeter of ΔABC is 18 cm

$$AB : BC : AC = 3 : 4 : 5$$

Let the common multiple be 'x'

$$AB = 3x, \quad BC = 4x, \quad AC = 5x$$

Now,

$$AB + BC + AC = 18$$

$$3x + 4x + 5x = 18$$

$$12x = 18$$

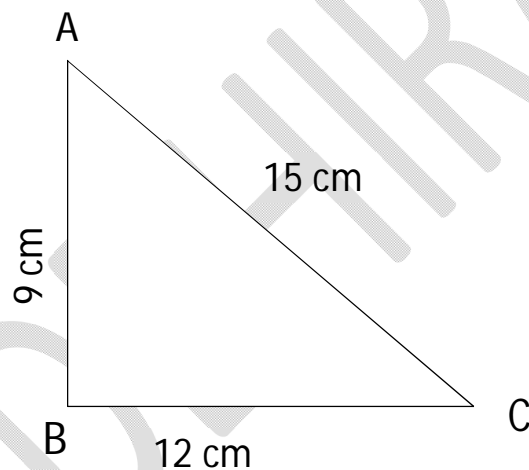
$$X = \frac{18}{12}$$

$$X = \frac{3}{2}$$

$$\therefore AB = 3x = 3 \times \frac{3}{2} = \frac{18}{2} = 9 \text{ cm}$$

$$\therefore BC = 4x = 4 \times \frac{3}{2} = \frac{24}{2} = 12 \text{ cm}$$

$$\therefore AC = 5x = 5 \times \frac{3}{2} = \frac{30}{2} = 15 \text{ cm}$$



Steps of construction:

I) Draw base $BC = 12 \text{ cm}$

II) Draw the arc of 9 cm radius taking B as center.

III) Draw the arc 15 cm radius taking with center C .

IV) Let the arc are intersect at point A .

ΔABC is the required triangle.

