

Miscellaneous Problems : Set 1

1. Solve the following :

(i) $(-16) \times (-5)$

Solution : $(-16) \times (-5) = 80$

(ii) $(72) \div (-12)$

Solution :

$$\begin{aligned} 72 \div (-12) &= \frac{1 \times 72}{(-1) \times 12} \\ &= \frac{1 \times 12 \times 6}{(-1) \times 12} \\ &= \frac{1}{(-1)} \times 6 \\ &= (-1) \times 6 \\ &= -6 \end{aligned}$$

(iii) $(-24) \times (2)$

Solution :

$(-24) \times 2 = -48$

(iv) $125 \div 5$

Solution :

$$\begin{aligned} 125 \div 5 &= \frac{125}{5} \\ &= \frac{5 \times 25}{5} \\ &= 5 \times 5 \\ &= 25 \end{aligned}$$

(v) $(-104) \div (-13)$

Solution :

$$\begin{aligned} (-104) \div (-13) &= \frac{(-104)}{(-13)} \\ &= \frac{(-1) \times 104}{(-1) \times 13} \\ &= \frac{1 \times 8 \times 13}{13} \\ &= 1 \times 8 \\ &= 8 \end{aligned}$$

(vi) $25 \times (-4)$

Solution :

$$25 \times (-4) = -100$$

2. Find the prime factors of the following numbers and find their LCM and HCF.

(i) 75, 135

Solution :

75, 135

$$75 = 3 \times 25$$

$$= \underline{3} \times \underline{5} \times 5$$

$$135 = 3 \times 45$$

$$= \underline{3} \times \underline{5} \times 9$$

$$= \underline{3} \times \underline{5} \times 3 \times 3$$

$$\therefore \text{LCM} = 3 \times 3 \times 3 \times 5 \times 5 = 675$$

$$\therefore \text{HCF} = 3 \times 5 = 15$$

(ii) 114, 76

Solution :

114, 76

$$114 = 2 \times 57$$

$$= \underline{2} \times 3 \times \underline{19}$$

$$76 = 2 \times 38$$

$$= \underline{2} \times 2 \times \underline{19}$$

$$\therefore \text{LCM} = 2 \times 2 \times 3 \times 19 = 228$$

$$\therefore \text{HCF} = 2 \times 19 = 38$$

(iii) 153, 187

Solution :

153, 187

$$153 = 3 \times 51$$

$$= 3 \times 3 \times \underline{17}$$

$$187 = 11 \times \underline{17}$$

$$\therefore \text{LCM} = 3 \times 3 \times 11 \times 17 = 1683$$

$$\therefore \text{HCF} = 17$$

(iv) 32, 24, 48

Solution :

32, 24, 48

$$32 = 2 \times 16$$

$$= 2 \times 2 \times 8$$

$$= 2 \times 2 \times 2 \times 4$$

$$= \underline{2} \times \underline{2} \times \underline{2} \times 2 \times 2$$

$$24 = 2 \times 12$$

$$= 2 \times 2 \times 6$$

$$= \underline{2} \times \underline{2} \times \underline{2} \times \underline{3}$$

$$48 = 2 \times 24$$

$$= 2 \times 2 \times 12$$

$$= 2 \times 2 \times 2 \times 6$$

$$= \underline{2} \times \underline{2} \times \underline{2} \times 2 \times \underline{3}$$

$$\therefore \text{LCM} = 2 \times 2 \times 2 \times 2 \times 2 \times 3 = 96$$

$$\text{HCF} = 2 \times 2 \times 2 = 8$$

3. Simplify.

(i) $\frac{322}{391}$

Solution :

To reduce the number to its simplest form, we will find the common factors of 322 and 247.

Let us find their HCF by the division method.

$$\begin{array}{r}
 \overline{322)391} \quad (1 \\
 \underline{-322} \\
 69 \overline{)322} \quad (4 \\
 \underline{-276} \\
 46 \overline{)69} \quad (1 \\
 \underline{-46} \\
 23 \overline{)46} \quad (2 \\
 \underline{-46} \\
 00
 \end{array}$$

∴ HCF is 23. i.e. the numerator and denominator are both divisible by 23.

$$\therefore \frac{322}{391} = \frac{322 \div 23}{391 \div 23} = \frac{14}{17}$$

(ii) $\frac{247}{209}$

Solution :

Method (I) :

$$\frac{247}{209} = \frac{19 \times 13}{19 \times 11} = \frac{13}{11}$$

$$\therefore \frac{247}{209} = \frac{13}{11}$$

Method (II) :

To reduce the number to its simplest form, we will find the common factors of 247 and 209.

Let us find HCF of 247 and 209 by the division method.

$$\begin{array}{r}
 209 \overline{) 247} \quad (1 \\
 \underline{- 209} \\
 38 \overline{) 209} \quad (5 \\
 \underline{- 190} \\
 19 \overline{) 38} \quad (2 \\
 \underline{- 38} \\
 00
 \end{array}$$

\therefore HCF is 19 . i.e. the numerator and denominator are both divisible by 19.

$$\therefore \frac{247}{209} = \frac{247 \div 19}{209 \div 19} = \frac{13}{11}$$

(ii) $\frac{117}{156}$

Solution :

Meothod (I):

$$\frac{117}{156} = \frac{39 \times 3}{39 \times 4} = \frac{3}{4}$$

$$\therefore \frac{117}{156} = \frac{3}{4}$$

Method (II):

Let us find HCF of 117 and 156 by the division method.

$$\begin{array}{r}
 117 \overline{) 156} \quad (1 \\
 \underline{- 117} \\
 39 \overline{) 117} \quad (3 \\
 \underline{- 117} \\
 000
 \end{array}$$

\therefore HCF is 39 . i.e. the numerator and denominator are both divisible by 39.

$$\therefore \frac{117}{156} = \frac{117 \div 39}{156 \div 39} = \frac{3}{4}$$

4. Find the square root of the following numbers.

(i) 784

Solution :

$$\begin{aligned}
 784 &= 2 \times 392 \\
 &= 2 \times 2 \times 196 \\
 &= 2 \times 2 \times 2 \times 98 \\
 &= 2 \times 2 \times 2 \times 2 \times 49
 \end{aligned}$$

$$= \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{7 \times 7}$$

$$\therefore \sqrt{784} = 2 \times 2 \times 7 = 28$$

\therefore The square root of 784 is 28.

(ii) 225

Solution :

$$225 = 3 \times 75$$

$$= 3 \times 3 \times 25$$

$$= \underline{3 \times 3} \times \underline{5 \times 5}$$

$$\therefore \sqrt{225} = 3 \times 5 = 15$$

\therefore The square root of 225 is 15.

(iii) 1296

Solution :

$$1296 = 2 \times 648$$

$$= 2 \times 2 \times 324$$

$$= 2 \times 2 \times 2 \times 162$$

$$= 2 \times 2 \times 2 \times 2 \times 81$$

$$= 2 \times 2 \times 2 \times 2 \times 3 \times 27$$

$$= 2 \times 2 \times 2 \times 2 \times 3 \times 3 \times 9$$

$$= \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{3 \times 3} \times \underline{3 \times 3}$$

$$\therefore \sqrt{1296} = 2 \times 2 \times 3 \times 3 = 36$$

\therefore The square root of 1296 is 36

(iv) 2025

Solution :

$$2025 = 3 \times 675$$

$$= 3 \times 3 \times 225$$

$$= 3 \times 3 \times 3 \times 75$$

$$= 3 \times 3 \times 3 \times 3 \times 25$$

$$= \underline{3 \times 3} \times \underline{3 \times 3} \times \underline{5 \times 5}$$

$$\therefore \sqrt{2025} = 3 \times 3 \times 5 = 45$$

\therefore The square root of 2025 is 45

(v) 256

Solution :

$$256 = 2 \times 128$$

$$= 2 \times 2 \times 64$$

$$= 2 \times 2 \times 2 \times 32$$

$$= 2 \times 2 \times 2 \times 2 \times 16$$

$$= 2 \times 2 \times 2 \times 2 \times 2 \times 8$$

$$= 2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 4$$

$$= \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2} \times \underline{2 \times 2}$$

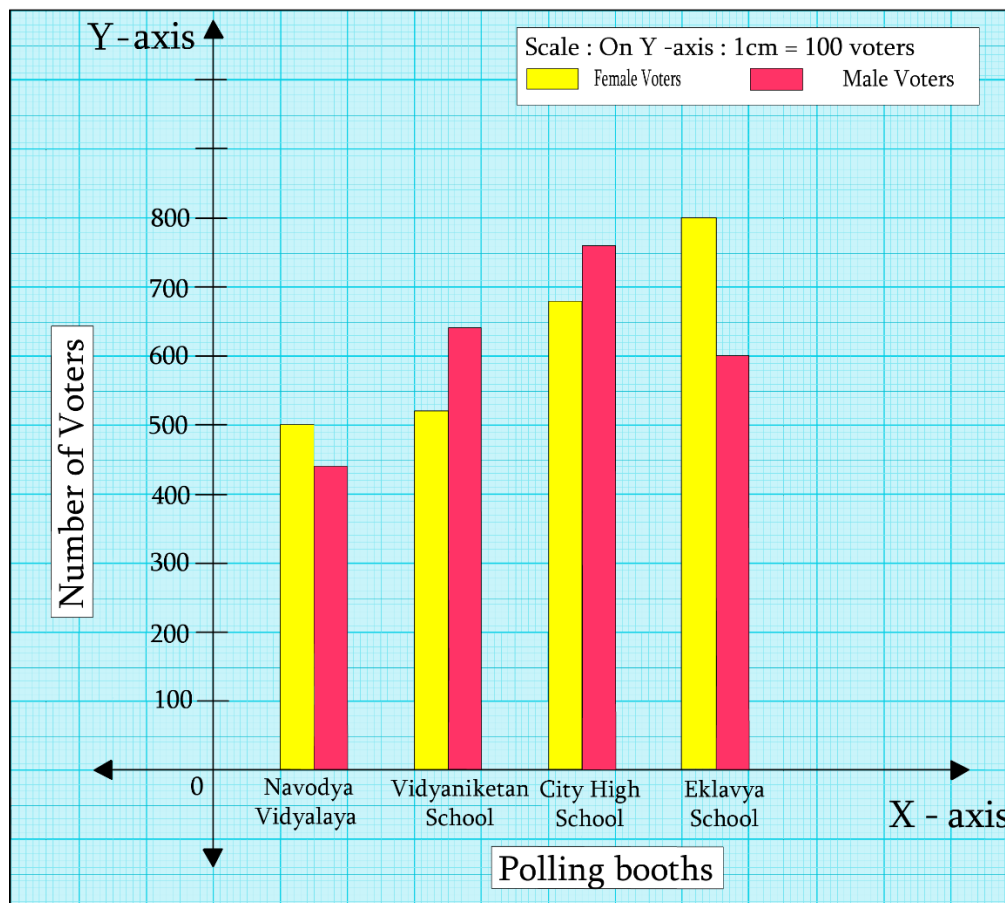
$$\therefore \sqrt{256} = 2 \times 2 \times 2 \times 2 = 16$$

\therefore The square root of 256 is 16.

5. There are four polling booths for a certain election. The numbers of men and women who cast their vote at each booth is given in the table below. Draw a joint bar graph for this data.

Polling Booths	Navodaya Vidyalaya	Vidyaniketan School	City High School	Eklavya School
Women	500	520	680	800
Men	440	640	760	600

Ans.:



6. Simplify the expressions.

(i) $45 \div 5 + 20 \times 4 - 12$

Solution :

$$\therefore 45 \div 5 + 20 \times 4 - 12$$

$$= 9 + 80 - 12$$

$$= 89 - 12$$

$$= 77$$

$$\therefore 45 \div 5 + 20 \times 4 - 12 = 77$$

(ii) $(38 - 8) \times 2 \div 5 + 13$

Solution :

$$\because (38 - 8) \times 2 \div 5 + 13$$

$$= 30 \times 2 \div 5 + 13$$

$$= 60 \div 5 + 13$$

$$= 12 + 13$$

$$= 25$$

$$\therefore (38 - 8) \times 2 \div 5 + 13 = 25$$

(iii) $\frac{5}{3} + \frac{4}{7} \div \frac{32}{21}$

Solution :

$$\because \frac{5}{3} + \frac{4}{7} \div \frac{32}{21}$$

$$= \frac{5}{3} + \frac{4}{7} \times \frac{21}{32}$$

$$= \frac{5}{3} + \frac{3}{8}$$

$$= \frac{5 \times 8 + 3 \times 3}{3 \times 8}$$

$$= \frac{40 + 9}{24}$$

$$= \frac{49}{24}$$

$$\therefore \frac{5}{3} + \frac{4}{7} \div \frac{32}{21} = \frac{49}{24}$$

$$(iv) 3 \times \{ 4 [85 + 5 - (15 \div 3)] + 2 \}$$

Solution :

$$\therefore 3 \times \{ 4 [85 + 5 - (15 \div 3)] + 2 \}$$

$$= 3 \times \{ 4 [85 + 5 - 5] + 2 \}$$

$$= 3 \times \{ 4 (85) + 2 \}$$

$$= 3 \times \{ 340 + 2 \}$$

$$= 3 \times 342$$

$$= 1026$$

$$\therefore 3 \times \{ 4 [85 + 5 - (15 \div 3)] + 2 \} = 1026$$

7. Solve.

(i) $\frac{5}{12} + \frac{7}{16}$

Solution :

$$\therefore \frac{5}{12} + \frac{7}{16} = \frac{5 \times 4}{48} + \frac{7 \times 3}{48} \dots\dots(\text{LCM of 12 and 16 is 48})$$

$$= \frac{20}{48} + \frac{21}{48}$$

$$= \frac{20 + 21}{48} = \frac{41}{48}$$

$$\therefore \frac{5}{12} + \frac{7}{16} = \frac{41}{48}$$

(ii) $3\frac{2}{5} - 2\frac{1}{4}$

Solution :

$$\therefore 3\frac{2}{5} - 2\frac{1}{4} = \frac{3 \times 5 + 2}{5} - \frac{2 \times 4 + 1}{4}$$

$$= \frac{17}{5} - \frac{9}{4}$$

$$= \frac{17 \times 4}{5 \times 4} - \frac{9 \times 5}{4 \times 5}$$

$$= \frac{68}{20} - \frac{45}{20} \dots\dots(\text{LCM of 5 and 4 is 20})$$

$$= \frac{68 - 45}{20} = \frac{23}{20}$$

$$\therefore 3 \frac{2}{5} - 2 \frac{1}{4} = \frac{23}{20}$$

$$\text{(iii)} \quad \frac{12}{5} \times \frac{(-10)}{3}$$

Solution :

$$\frac{12}{5} \times \frac{(-10)}{3} = \frac{12 \times (-10)}{5 \times 3}$$

$$= \frac{3 \times 4 \times (-2) \times (5)}{5 \times 3}$$

$$= 4 \times (-2)$$

$$= -8$$

$$\therefore \frac{12}{5} \times \frac{(-10)}{3} = -8$$

(iv) $4\frac{3}{8} \div \frac{25}{18}$

Solution :

$$\begin{aligned} 4\frac{3}{8} \div \frac{25}{18} &= \frac{35}{8} \div \frac{25}{18} \\ &= \frac{35}{8} \times \frac{18}{25} \\ &= \frac{35 \times 18}{8 \times 25} \\ &= \frac{5 \times 7 \times 2 \times 9}{2 \times 4 \times 5 \times 5} \\ &= \frac{63}{20} \end{aligned}$$

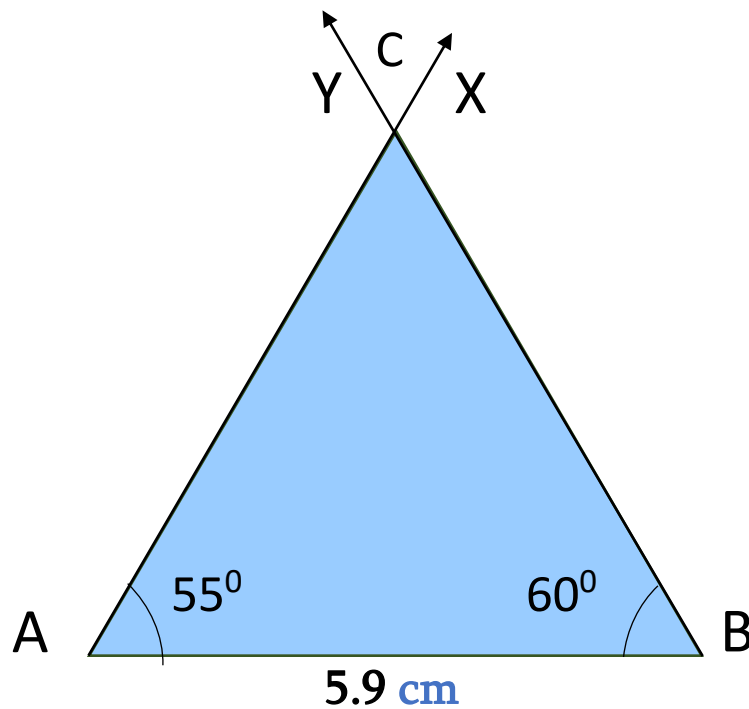
$$\therefore 4\frac{3}{8} \div \frac{25}{18} = \frac{63}{20}$$

8. Construct $\triangle ABC$ such that $m\angle A = 55^\circ$, $m\angle B = 60^\circ$ and $l(AB) = 5.9$ cm.

Solution :

Given: In $\triangle ABC$,

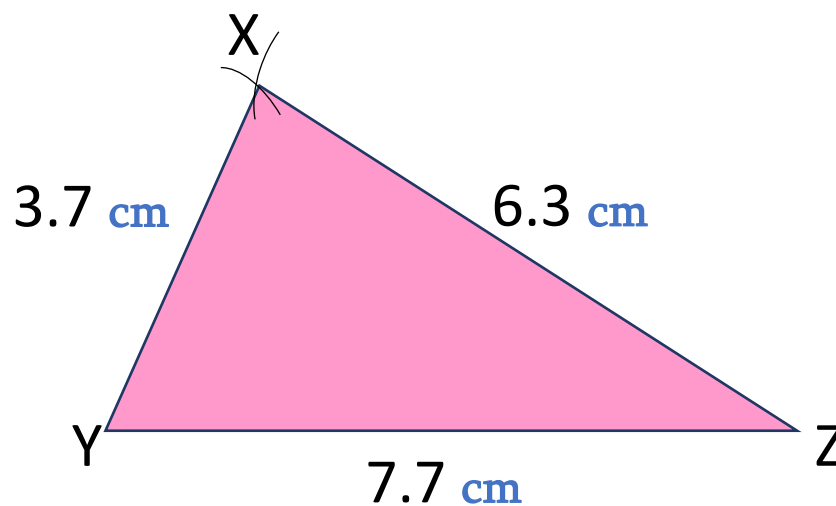
$m\angle A = 55^\circ$, $m\angle B = 60^\circ$ and $l(AB) = 5.9$ cm.



9. Construct $\triangle XYZ$ such that, $l(XY) = 3.7 \text{ cm}$,
 $l(YZ) = 7.7 \text{ cm}$, $l(XZ) = 6.3 \text{ cm}$.

Solution :

Given : In $\triangle XYZ$, $l(XY) = 3.7 \text{ cm}$, $l(YZ) = 7.7 \text{ cm}$,
 $l(XZ) = 6.3 \text{ cm}$.



10. Construct $\triangle PQR$ such that, $m\angle P = 80^\circ$, $m\angle Q = 70^\circ$, $l(QR) = 5.7$ cm.

Solution :

Given : In $\triangle PQR$ $m\angle P = 80^\circ$, $m\angle Q = 70^\circ$, $l(QR) = 5.7$ cm.

$$m\angle P + m\angle Q + m\angle R = 180^\circ$$

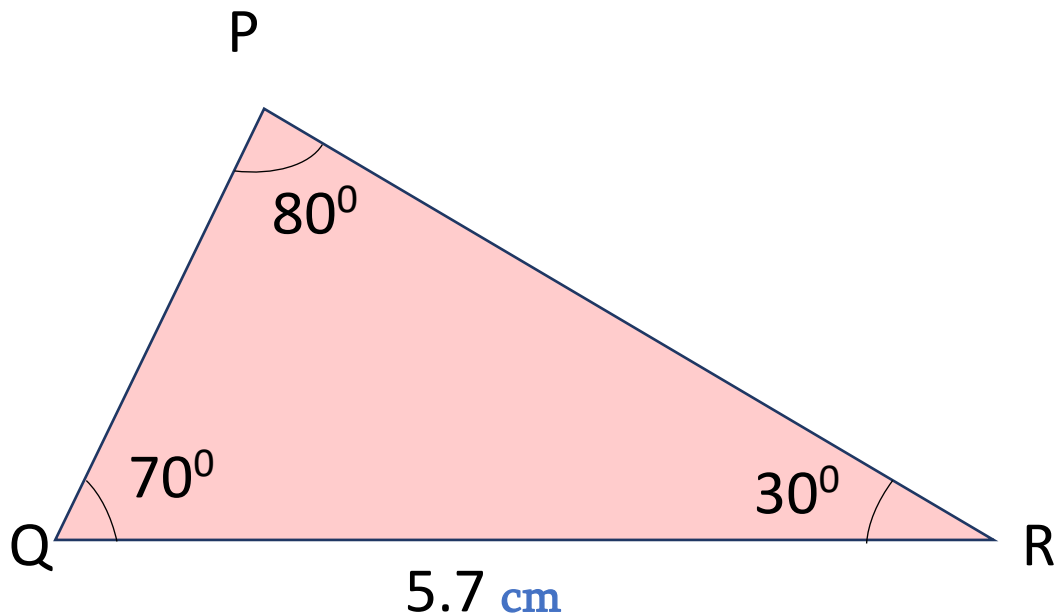
$$\therefore 80^\circ + 70^\circ + m\angle R = 180^\circ$$

$$\therefore m\angle R = 180^\circ - 80^\circ - 70^\circ$$

$$\therefore m\angle R = 180^\circ - (80^\circ + 70^\circ)$$

$$\therefore m\angle R = 180^\circ - (150^\circ)$$

$$\therefore m\angle R = 30^\circ$$



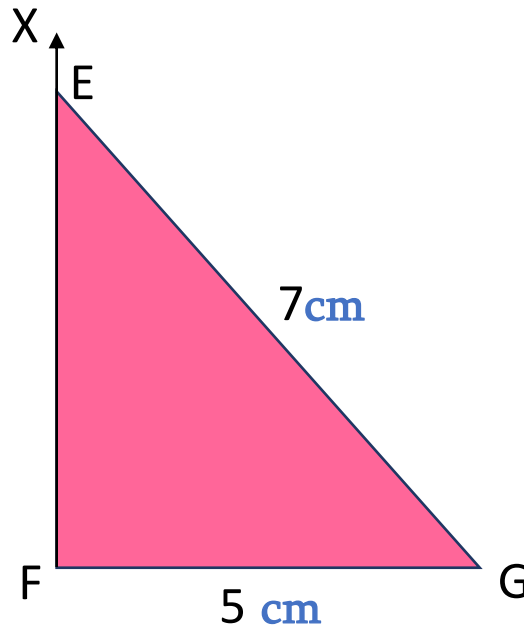
11. Construct $\triangle EFG$ from the given measures.

$l(FG) = 5 \text{ cm}$, $m\angle EFG = 90^\circ$, $l(EG) = 7 \text{ cm}$.

Solution :

Given : In $\triangle EFG$ $l(FG) = 5 \text{ cm}$, $m\angle EFG = 90^\circ$,

$l(EG) = 7 \text{ cm}$.



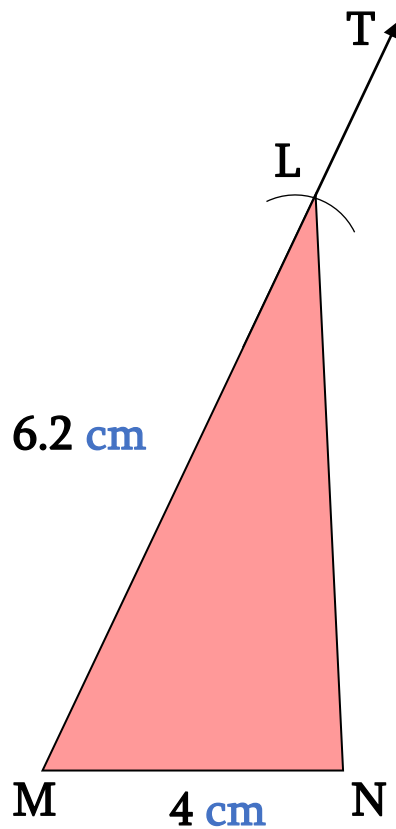
12. In $\triangle LMN$, $l(LM) = 6.2 \text{ cm}$, $m\angle LMN = 60^\circ$,

$l(MN) = 4 \text{ cm}$. Construct $\triangle LMN$.

Solution :

Given : In $\triangle LMN$, $l(LM) = 6.2 \text{ cm}$, $m\angle LMN = 60^\circ$,

$l(MN) = 4 \text{ cm}$.



13. Find the measures of the complementary angles of the following angles.

(i) 35°

Solution :

Suppose the complement of the given angle be x° .

$$\therefore 35 + x = 90$$

$$\therefore 35 + x - 35 = 90 - 35$$

$$\therefore x = 55$$

\therefore The complement of 35° is 55°

(ii) a°

Solution :

Suppose the complement of the given angle be x° .

$$\therefore a + x = 90$$

$$\therefore a + x - a = 90 - a$$

$$\therefore x = (90 - a)$$

\therefore The complement of a° is $(90 - a)^\circ$.

(iii) 22°

Solution :

Suppose the complement of the given angle be x° .

$$\therefore 22 + x = 90$$

$$\therefore 22 + x - 22 = 90 - 22$$

$$\therefore x = 68$$

\therefore The complement of 22° is 68° .

(iv) $(40 - x)^\circ$

Solution :

Suppose the complement of the given angle be a° .

$$\therefore (40 - x) + a = 90$$

$$\therefore (40 - x) + a - (40 - x) = 90 - (40 - x)$$

$$\therefore a = 90 - 40 + x$$

$$\therefore a = 50 + x$$

\therefore The complement of $(40 - x)^\circ$ is $(50 + x)^\circ$.

14. Find the measures of the supplements of the following angles.

(i) 111°

Solution :

Suppose the supplement of the given angle be a° .

$$\therefore 111 + a = 180$$

$$\therefore a = 180 - 111 = 69$$

\therefore The supplement of 111° is 69° .

(ii) 47°

Solution :

Suppose the supplement of the given angle be a° .

$$\therefore 47 + a = 180$$

$$\therefore a = 180 - 47 = 133$$

\therefore The supplement of 47° is 133° .

(iii) 180°

Solution :

Suppose the supplement of the given angle be a° .

$$\therefore 180 + a = 180$$

$$\therefore a = 180 - 180 = 0$$

\therefore The supplement of 180° is 0°

(iv) $(90 - x)^\circ$

Solution :

Suppose the supplement of the given angle be a° .

$$\therefore (90 - x) + a = 180$$

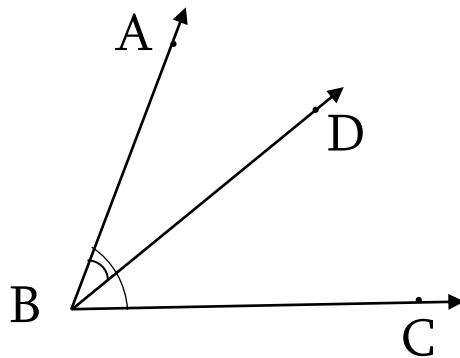
$$\begin{aligned}\therefore a &= 180 - (90 - x) \\ &= 180 - 90 + x \\ &= 90 + x\end{aligned}$$

\therefore The supplement of $(90 - x)^\circ$ is $(90 + x)^\circ$

15. Construct the following figures.

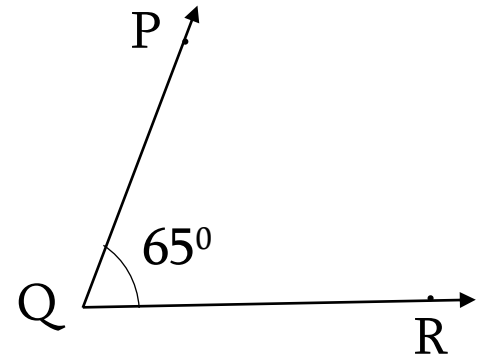
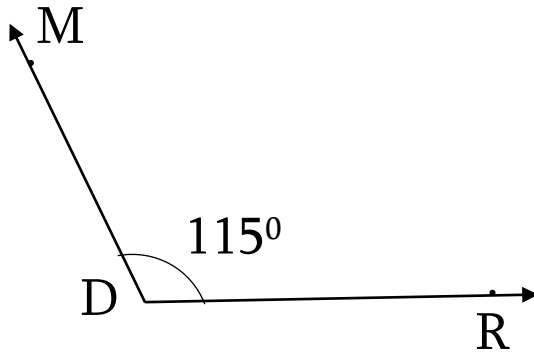
(i) A pair of adjacent angles

Ans. $\angle ABC$ and $\angle DBC$ form a pair of adjacent angles.



(ii) Two supplementary angles which are not adjacent angles.

Ans.



$$m\angle MDR = 115^\circ \text{ and } m\angle PQR = 65^\circ$$

$$m\angle PQR + m\angle MDR = 65^\circ + 115^\circ = 180^\circ$$

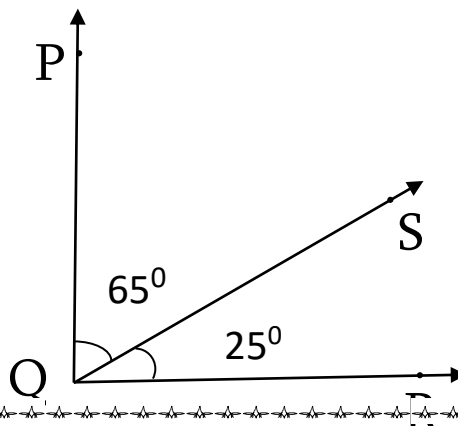
$\therefore m\angle MDR$ and $m\angle PQR$ are supplementary angles but not adjacent angles.

(iii) A pair of adjacent complementary angles.

Ans.

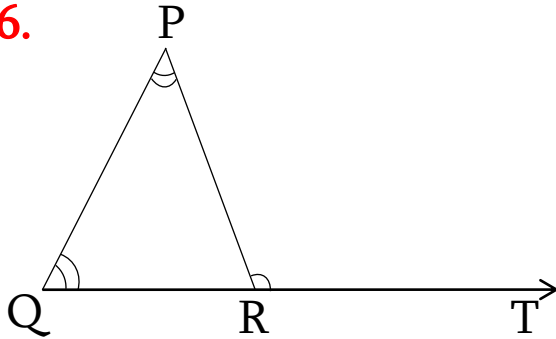
$$m\angle PQS = 65^\circ \text{ and } m\angle SQR = 25^\circ$$

$$m\angle PQS + m\angle SQR = 65^\circ + 25^\circ = 90^\circ$$



$\therefore m\angle PQS$ and $m\angle SQR$ is pair of adjacent angles which are complementary angles.

16.



In $\triangle PQR$, the measures of $\angle P$ and $\angle Q$ are equal and $m\angle PRQ = 70^\circ$. Find the measures of the following angles.

(i) $m\angle PRT$ (ii) $m\angle P$ (iii) $m\angle Q$

Solution :

$$m\angle PRQ + m\angle PRT = 180^\circ \dots (\text{Angles forming a linear pair})$$

$$\therefore 70^\circ + m\angle PRT = 180^\circ$$

$$\therefore m\angle PRT = 180^\circ - 70^\circ$$

$$\therefore m\angle PRT = 110^\circ$$

$$m\angle PRT = m\angle P + m\angle Q \quad (\text{By the exterior angle property})$$

$$\therefore 2m\angle P = 110^\circ \quad \dots (\because m\angle P = m\angle Q)$$

$$\therefore m\angle P = \frac{110^\circ}{2}$$

$$\therefore m\angle P = 55^\circ$$

Also $m\angle Q = 55^\circ$

\therefore (i) $m\angle PRT = 110^\circ$ (ii) $m\angle P = 55^\circ$ (iii) $m\angle Q = 55^\circ$

17. Simplify.

(i) $5^4 \times 5^3$

Solution :

$$5^4 \times 5^3 = 5^{4+3} \quad \dots (a^m \times a^n = a^{m+n})$$

$$\therefore 5^4 \times 5^3 = 5^7$$

(ii) $\left(\frac{2}{3}\right)^6 \div \left(\frac{2}{3}\right)^9$

Solution :

$$\left(\frac{2}{3}\right)^6 \div \left(\frac{2}{3}\right)^9 = \left(\frac{2}{3}\right)^{9-6} \quad \dots \left(\frac{a^m}{a^n} = a^{m-n}\right)$$

$$= \left(\frac{2}{3}\right)^{-3} = \left(\frac{3}{2}\right)^3 \quad \dots \left[\left(\frac{a}{b}\right)^{-m} = \left(\frac{b}{a}\right)^m\right]$$

$$= \left(\frac{3}{2}\right)^3$$

$$\therefore \left(\frac{2}{3}\right)^6 \div \left(\frac{2}{3}\right)^9 = \left(\frac{3}{2}\right)^3$$

$$\text{(iii)} \quad \left(\frac{7}{2}\right)^8 \times \left(\frac{7}{2}\right)^{-6}$$

Solution :

$$\begin{aligned} \left(\frac{7}{2}\right)^8 \times \left(\frac{7}{2}\right)^{-6} &= \left(\frac{7}{2}\right)^{8+(-6)} & \dots(a^m \times a^n = a^{m+n}) \\ &= \left(\frac{7}{2}\right)^2 \end{aligned}$$

$$\therefore \left(\frac{7}{2}\right)^8 \times \left(\frac{7}{2}\right)^{-6} = \left(\frac{7}{2}\right)^2$$

$$\text{(iv)} \quad \left(\frac{4}{5}\right)^2 \div \left(\frac{5}{4}\right)$$

Solution :

$$\begin{aligned} \left(\frac{4}{5}\right)^2 \div \left(\frac{5}{4}\right) &= \left(\frac{4}{5}\right)^2 \times \left(\frac{4}{5}\right)^1 & \dots(a^1 = a) \\ &= \left(\frac{4}{5}\right)^{2+1} & \dots(a^m \times a^n = a^{m+n}) \\ &= \left(\frac{4}{5}\right)^3 \end{aligned}$$

$$\therefore \left(\frac{4}{5}\right)^2 \div \left(\frac{5}{4}\right) = \left(\frac{4}{5}\right)^3$$

18. Find the value.

(i) $17^{16} \div 17^{16}$

Solution :

$$17^{16} \div 17^{16}$$

$$= 17^{16-16} \quad \dots (a^m \div a^n = a^{m-n})$$

$$= 17^0$$

$$= 1 \quad \dots (a^0=1)$$

$$\therefore 17^{16} \div 17^{16} = 1$$

(ii) 10^{-3}

Solution :

$$10^{-3}$$

$$= \frac{1}{10^3} \quad \dots (a^{-m} = \frac{1}{a^m})$$

$$= \frac{1}{10 \times 10 \times 10}$$

$$= \frac{1}{1000}$$

$$\therefore 10^{-3} = \frac{1}{1000}$$

(iii) $(2^3)^2$

Solution :

$$(2^3)^2$$

$$= 2^{3 \times 2}$$

$$\dots [(a^m)^n = a^{mn}]$$

$$= 2^6$$

$$= 2 \times 2 \times 2 \times 2 \times 2 \times 2$$

$$= 64$$

$$\therefore (2^3)^2 = 64$$

(iv) $4^6 \times 4^{-4}$

Solution :

$$4^6 \times 4^{-4}$$

$$= 4^{6+(-4)} \dots (a^m \times a^n = a^{m+n})$$

$$= 4^2$$

$$= 4 \times 4$$

$$= 16$$

$$\therefore 4^6 \times 4^{-4} = 16$$

19. Solve.

(i) $(6a - 5b - 8c) + (15b + 2a - 5c)$

Solution : Horizontal arrangement :

$$\begin{aligned} & 6a - 5b - 8c + 15b + 2a - 5c \\ &= (6a + 2a) + (-5b + 15b) + (-8c - 5c) \\ &= 8a + 10b - 13c \end{aligned}$$

Vertical arrangement :

$$\begin{array}{r} 6a - 5b - 8c \\ + \quad \underline{2a + 15b - 5c} \\ \hline 8a + 10b - 13c \end{array}$$
$$\therefore 6a - 5b - 8c + 15b + 2a - 5c = 8a + 10b - 13c$$

(ii) $(3x + 2y)(7x - 8y)$

Solution :

$$\begin{aligned} & (3x + 2y)(7x - 8y) \\ &= 3x(7x - 8y) + 2y(7x - 8y) \\ &= 21x^2 - 24xy + 14xy - 16y^2 \\ &= 21x^2 - 10xy - 16y^2 \\ &\therefore (3x + 2y)(7x - 8y) = 21x^2 - 10xy - 16y^2 \end{aligned}$$

$$(iii) (7m-5n) - (-4n-11m)$$

Solution :

$$(7m-5n) - (-4n-11m)$$

$$= 7m - 5n + 4n + 11m$$

$$= 7m + 11m - 5n + 4n$$

$$= 18m - n$$

$$\therefore (7m-5n) - (-4n-11m) = 18m - n$$

$$(iv) (11m-12n+3p) - (9m+7n-8p)$$

Solution :

$$(11m-12n+3p) - (9m+7n-8p)$$

$$= 11m - 12n + 3p - 9m - 7n + 8p$$

$$= 11m - 9m - 12n - 7n + 3p + 8p$$

$$= 2m - 19n + 11p$$

$$\therefore (11m-12n+3p) - (9m+7n-8p) = 2m - 19n + 11p$$

20. Solve the following equations.

(i) $4(x + 12) = 8$

Solution :

$$\therefore 4(x + 12) = 8$$

$$\therefore 4x + 48 = 8$$

$$\therefore 4x + 48 - 48 = 8 - 48$$

$$\therefore 4x = -40$$

$$\therefore x = -10$$

\therefore The value of x is -10 .

(ii) $3y + 4 = 5y - 6$

Solution :

$$\therefore 3y + 4 = 5y - 6$$

$$\therefore 4 + 6 = 5y - 3y$$

$$\therefore 10 = 2y$$

$$\therefore y = 5$$

\therefore The value of y is 5.

Multiple choice Questions

Choose the right answer from the options given after every question.

1. The three angle bisectors of a triangle are concurrent.

Their point of concurrence is called the

(i) circumcentre

(ii) apex

(iii) incentre

(iv) point of intersection.

Ans.: (iii) incentre

2. $\left[\left(\frac{3}{7}\right)^{-3}\right]^4 = \dots\dots\dots$

(i) $\left(\frac{3}{7}\right)^{-7}$

(ii) $\left(\frac{3}{7}\right)^{-10}$

(iii) $\left(\frac{7}{3}\right)^{12}$

(iv) $\left(\frac{3}{7}\right)^{20}$

Ans.: (iii) $\left(\frac{7}{3}\right)^{12}$

3. The simplest form of $5 \div \left(\frac{3}{7}\right) - \frac{1}{3}$ is

- (i) 3 (ii) 5 (iii) 0 (iv) $\frac{1}{3}$

Ans.: (i) 3

4. The solution of the equation $3x - \frac{1}{2} = \frac{5}{2} + x$ is

- (i) $\frac{5}{3}$ (ii) $\frac{7}{2}$ (iii) 4 (iv) $\frac{3}{2}$

Ans.: (iv) $\frac{3}{2}$

5. Which of the following expressions has the value 37?

- (i) $10 \times 3 + (5 + 2)$ (ii) $10 \times 4 + (5 - 3)$
(iii) $8 \times 4 + 3$ (iv) $(9 \times 3) + 2$

Ans.: (i) $10 \times 3 + (5 + 2)$
