

3. TRIANGLE

Q.1 In ΔABC , if $\angle A + \angle B = 110^\circ$ and $\angle B + \angle C = 132^\circ$, then find $\angle A$, $\angle B$ and $\angle C$.

Solution - We have $\angle A + \angle B = 110^\circ \dots\dots (1)$

$$\angle B + \angle C = 132^\circ \dots\dots (2)$$

Now,

$$\angle A + \angle B + \angle C = 180^\circ \text{ Sum of angle of triangle is } 180^\circ$$

$$110^\circ + \angle C = 180^\circ \dots\dots (\because \angle A + \angle B = 110^\circ)$$

$$\angle C = 180^\circ - 110^\circ$$

$$\angle C = 70^\circ$$

Now, from II we have,

$$\angle B + \angle C = 132^\circ$$

$$\angle B = 132^\circ - 70^\circ$$

$$\angle B = 62^\circ$$

$$\angle A + \angle B = 110^\circ \dots\dots (\text{From I})$$

$$\angle A + 62^{\circ} = 110^{\circ}$$

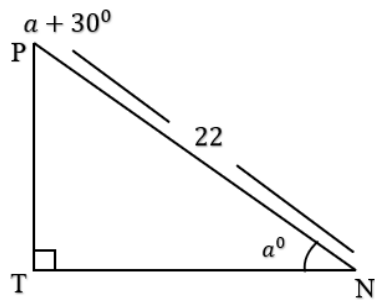
$$\angle A = 110^{\circ} - 62^{\circ}$$

$$\angle A = 48^{\circ}$$

$$\therefore \angle A = 48^{\circ}, \angle B = 62^{\circ} \text{ and } \angle C = 70^{\circ}$$

Q.2 In ΔPTN , $\angle T = 90^{\circ}$, $\angle N = a^{\circ}$, $\angle P = (a + 30)^{\circ}$

If $PN = 22$ then find PT and TN .



In ΔPTN

$$\angle P + \angle T + \angle N = 180^{\circ}$$

..... (Sum of angles of triangles is 180°)

$$\therefore (a + 30)^{\circ} + 90^{\circ} + a^{\circ} = 180^{\circ}$$

$$a + 30^{\circ} + 90^{\circ} + a^{\circ} = 180^{\circ}$$

$$2a^{\circ} + 120^{\circ} = 180^{\circ}$$

$$2a^{\circ} = 180^{\circ} - 120^{\circ}$$

$$2a^0 = 60^0$$

$$a^0 = \frac{60^0}{2}$$

$$a^0 = 30^0$$

$$\angle N = a^0 = 30^0$$

$$\angle P = (a + 30)^0 = a^0 + 30^0 = 30^0 + 30^0 = 60^0$$

ΔPTN is $30^0 - 60^0 - 90^0$ of triangle-

$$PT = \frac{1}{2} \times PN \dots\dots (\text{side opposite to } 30^0)$$

$$= \frac{1}{2} \times 22$$

$$\therefore PT = 11 \text{ units}$$

$$TN = \frac{\sqrt{3}}{2} \times PN \dots\dots (\text{side opposite to } 60^0)$$

$$= \frac{\sqrt{3}}{2} \times 22$$

$$TN = 11\sqrt{3} \text{ units}$$

$$\therefore PT = 11 \text{ units } TN = 11\sqrt{3} \text{ units}$$

Q.3 In ΔABC $AB = 5\text{ cm}$ $BC = 8\text{ cm}$ $AC = 10\text{ cm}$. Write all its angles in the descending order of their measure.

Solution – In ΔABC }

$$AB = 5\text{ cm} \quad BC = 8\text{ cm} \quad AC = 10\text{ cm}$$

$$10 > 8 > 5$$

$$\therefore AC > BC > AB \dots\dots (1)$$

Now,

$$AC > BC \dots\dots$$

$$\therefore \angle B > \angle A \dots\dots (II) \text{ (Angle opposite to greater side is greater)}$$

$$BC > AB \dots\dots \text{ From II}$$

$$\therefore \angle A > \angle C \text{----- From III (Angle opposite to greater$$

$$\therefore \angle B > \angle A > \angle C \text{----- (From II and III)}$$

Q.4 Triangle ABC has sides of length 7.8 and 9 units while ΔPQR has perimeter of 360 units. If ΔABC is similar to ΔPQR then find the sides of ΔPQR

Solution Sides of ΔABC are of 7, 8 and 9 units-

$$\text{Perimeter of } \Delta PQR = 360$$

$$\therefore x + y + z = 360 \dots\dots (i)$$

$$\Delta ABC \sim \Delta XYZ$$

$$\therefore \frac{7}{x} = \frac{8}{y} = \frac{9}{z} \dots\dots (Corresponding sides of similar triangles)$$

$$\therefore \frac{7}{x} = \frac{8}{y} = \frac{9}{z} = \frac{7+8+9}{x+y+z} \dots\dots (Property of equal ratios)$$

$$\therefore \frac{7}{x} = \frac{8}{y} = \frac{9}{z} = \frac{24}{360}$$

$$\therefore \frac{7}{x} = \frac{8}{y} = \frac{9}{z} = \frac{1}{15}$$

Now,

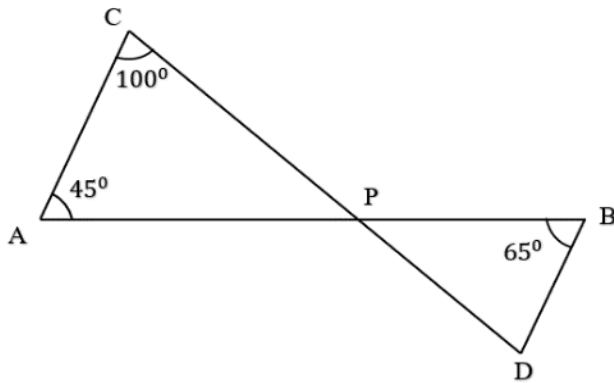
$$\frac{7}{x} = \frac{1}{15} \quad \therefore x = 7 \times 15 = 105$$

$$\frac{8}{y} = \frac{1}{15} \quad \therefore y = 8 \times 15 = 120$$

$$\frac{9}{z} = \frac{1}{15} \quad \therefore z = 9 \times 15 = 135$$

\therefore Corresponding sides of ΔPQR are 105 units , 120 units , 135 units respectively.

Q.5 In the adjoining figure, line AB and CD are intersected at point P. Then, $\angle PAC = 45^\circ$, $\angle ACP = 100^\circ$ and $\angle PBD = 65^\circ$, $\angle CPA$, $\angle DPB$ and $\angle BDP$



Solution –

Sum of angles of triangle is 180°

In $\triangle ACP$

$$\angle PAC + \angle ACP + \angle CPA = 180^\circ$$

$$45^\circ + 100^\circ + \angle CPA = 180^\circ$$

$$145^\circ + \angle CPA = 180^\circ$$

$$\angle CPA = 180^\circ - 145^\circ$$

$$\angle CPA = 35^\circ$$

$\therefore \angle DPB = \angle CPA = 35^\circ \dots$ (Vertically opposite angle)

In $\triangle PBD$

$$\angle DPB + \angle PBD + \angle BDP = 180^\circ$$

\dots (Sum of angles of a triangle)

$$35^\circ + 65^\circ + \angle BDP = 180^\circ$$

$$100^\circ + \angle BDP = 180^\circ$$

$$\angle BDP = 180^\circ - 100^\circ$$

$$\angle BDP = 80^\circ$$

$$\therefore \angle CPA = 35^\circ, \angle DPB = 35^\circ, \angle BDP = 80^\circ$$